

# Supporting Information for: Ab-initio Study of Oxygen Vacancy Stability in Bulk and Cerium-doped Lutetium Oxyorthosilicate

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## Abstract

We study from first principles the stability of neutral and charged oxygen vacancies in lutetium oxyorthosilicate,  $\text{Lu}_2\text{SiO}_5$ , as well as its possible modification due to the presence of  $\text{Ce}^{3+}$ , as present in commercial scintillators. We show that the neutral oxygen vacancies with the lowest formation energy form at the oxygen sites within the  $[\text{SiO}_4]$  tetrahedra instead of the interstitial oxygen site bonded exclusively to lutetium atoms. The discrepancy with a previous study is attributed to the quality of the pseudopotential. Support for these results is found by performing a bonding analysis of the oxygen sites, as well as oxygen vacancy calculations in the iso-structural  $\text{Y}_2\text{SiO}_5$  compound. In addition, we find that the incorporation of  $\text{Ce}^{3+}$  ion does not affect the stability of oxygen vacancies in  $\text{Lu}_2\text{SiO}_5$ .

**Keywords:** Scintillator, Oxygen vacancy, luminescence, ab-initio calculation

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Table 1: Lattice parameters of bulk LSO within the conventional cell.

| LSO            | $a(\text{\AA})$ | $b(\text{\AA})$ | $c(\text{\AA})$ | $\alpha$ | $\beta$ | $\gamma$ | Volume( $\text{\AA}^3$ ) |
|----------------|-----------------|-----------------|-----------------|----------|---------|----------|--------------------------|
| Exp.           | 14.28           | 6.64            | 10.25           | 90.00    | 122.22  | 90.00    | 821.74                   |
| Cal.(LDA-TM)   | 14.95           | 6.84            | 10.81           | 90.00    | 122.99  | 90.00    | 927.53                   |
| Cal.(LDA-FHI)  | 14.06           | 6.38            | 9.85            | 90.00    | 122.76  | 90.00    | 743.52                   |
| Cal.(LDA-Dojo) | 14.12           | 6.15            | 10.03           | 90.00    | 122.25  | 90.00    | 781.28                   |

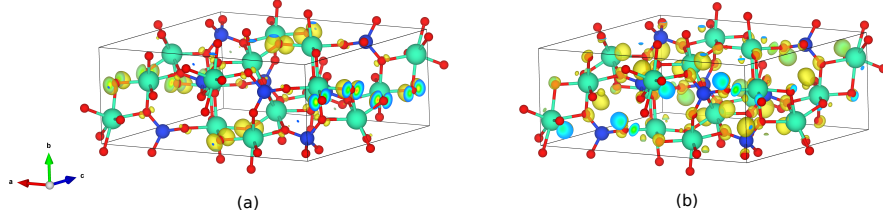


Figure 1: Charge density of (a) VBM and (b) CBM of  $\text{Lu}_2\text{SiO}_5$  at the  $\Gamma$  point. The green, blue and red spheres stand for the Lu, Si and O atoms, respectively.

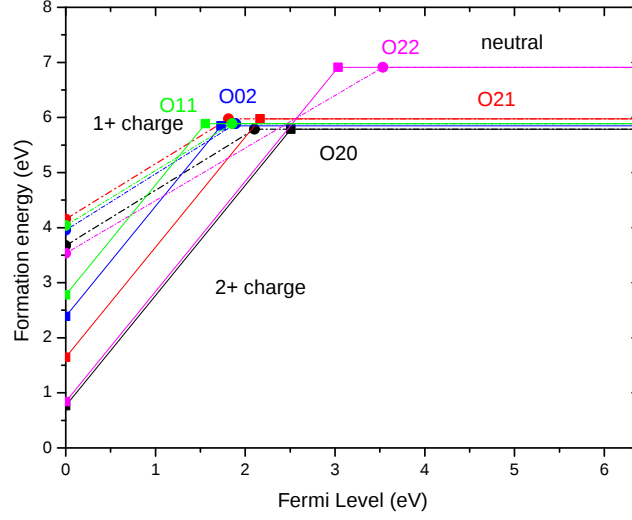


Figure 2: The corrected formation energy of oxygen vacancy with 2+, 1+ and neutral charge in  $\text{Lu}_2\text{SiO}_5$  from PBE-GGA PAW, using 63-atom supercell.

Table 2: Relaxed O-Lu and O-Si bond length of five oxygen crystallographic sites in LSO crystal. The longest O-Lu is shown in bold. [Unit: Å]

|                   | M = O <sub>20</sub> | M = O <sub>21</sub> | M = O <sub>11</sub> | M = O <sub>02</sub> | M = O <sub>22</sub> |
|-------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
| M-Lu <sub>1</sub> | 2.307               | <b>2.732</b>        | 2.254               | —                   | 2.352               |
|                   | 2.235               | 2.325               |                     |                     | 2.144               |
| M-Lu <sub>2</sub> | —                   | 2.216               | 2.237               | 2.236               | 2.271               |
|                   |                     |                     |                     | 2.224               | 2.57                |
| M-Si              | 1.615               | 1.612               | 1.624               | 1.641               | —                   |

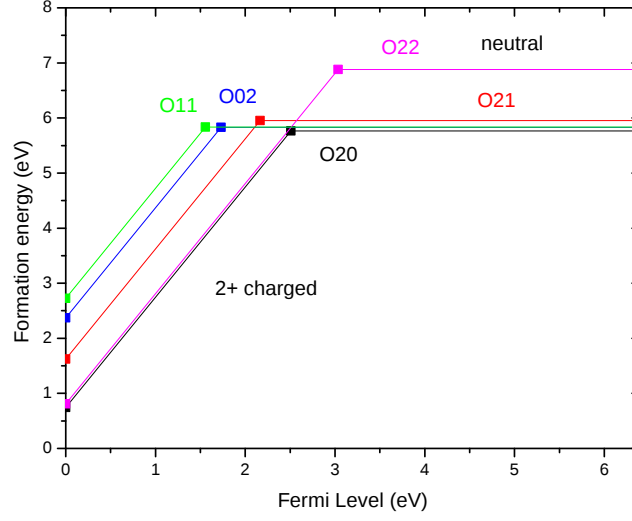


Figure 3: Formation energy of oxygen vacancy in  $\text{Lu}_2\text{SiO}_5$  from PBE-PAW, using 127-atom supercell.



Table 3: The formation energy of neutral oxygen vacancies in LSO bulk. [Unit: eV]

| case      | $E_{tot}(\text{LSO:V}_O, \text{63-atoms.})$ | $\Delta E_{f,1} \text{ (63-atom)}$ | $E_{tot}(\text{LSO:V}_O, \text{127-atom})$ | $\Delta E_{f,1} \text{ (127-atom)}$ |
|-----------|---------------------------------------------|------------------------------------|--------------------------------------------|-------------------------------------|
| $V_{O20}$ | -36516.14                                   | 5.76                               | -73475.39                                  | 5.76                                |
| $V_{O21}$ | -36515.95                                   | 5.97                               | -73475.21                                  | 5.95                                |
| $V_{O11}$ | -36516.04                                   | 5.86                               | -73475.30                                  | 5.83                                |
| $V_{O02}$ | -36516.08                                   | 5.82                               | -73475.33                                  | 5.83                                |
| $V_{O02}$ | -36515.01                                   | 6.88                               | -73474.28                                  | 6.88                                |

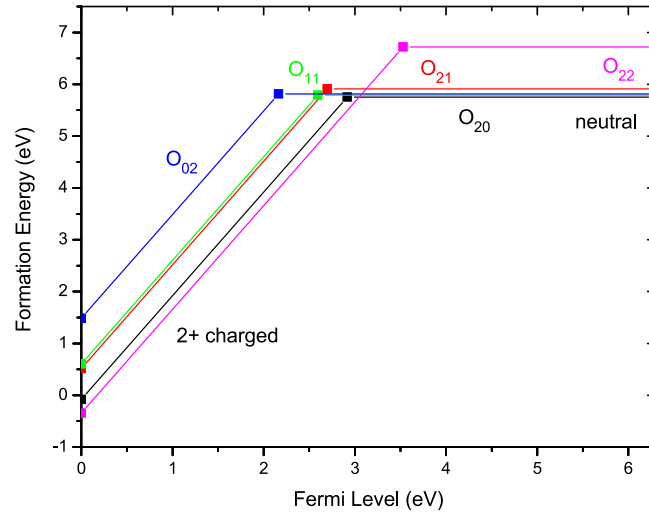


Figure 4: Formation energy of oxygen vacancy in  $\text{Y}_2\text{SiO}_5$  from PBE-PAW, using 63-atom supercell.