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Cognitive bases of developmental dyscalculia

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plan

- Definition - prevalence - associations
- Genetic contribution
 - Families studies, twin studies, genetic syndromes
- General cognitive factors
 - inhibition, working memory, long-term memory
 - Finger agnosia
- Numerical factors
 - The number sense
 - The access to the magnitude representation from symbols
 - The automatic activation of number magnitude

Definition (DSM)

- *Developmental dyscalculia is a specific learning difficulty manifested by failure to achieve adequate proficiency in arithmetic despite normal intelligence, scholastic opportunities, emotional stability, and sufficient motivation.*
- *These difficulties do not result from a sensorial deficit*
- *These difficulties interfere significantly with daily life and/or school success*

A variety of difficulties

- **Writing & reading numbers**
 - Reading: 85 => *eighty-two* (Paul; Temple, 1989)
 - Writing: *fifty thousand ninety* => 50,90 (CM, Sullivan, Maracaruso & Sokol, 1996)
- **Calculation procedures**
 - Mastery of the procedures required to solve multi-digit written calculation: carrying, borrowing ... (SW, Temple, 1991)
- **« visual-spatial dyscalculia »**
 - Errors in counting random patterns of dots, problems in left-right orientation (< > + x), mastery of the positional system of the Arabic notation (41 - 14), geometry (Spiers, 1987)
- **Arithmetical facts : 3+6; 9-2; 4x6; 12:3**
 - longer RTs, immature strategies (counting all, counting on fingers), less retrieval from long-term memory, more errors (counting & retrieval)

NR, a dyscalculia of arithmetical facts

- 33 y.o. woman, normal intelligence
- Simple 1-digit additions : 15% errors
 - 1+4=4, 3+5=9
- Simple 1-digit multiplications : 39% errors
 - 5x5=35; 7x4=21, 0x5=5
- Divisions: impossible
- Count on her fingers
- => many difficulties with dealing with her money, shopping, comparing prices; did not obtain her certificate of primary school

Prevalence & associations

- Badian: 1476 American children, 7-14 y.o.
 - 3,6% difficulties in math (< pc 20 on the Stanford Achievement test),
 - 2,2% difficulties in reading
 - 2,7% difficulties in math & reading
- Lewis et al.: 1056 English children, 9-10 y.o. (NS < 85)
 - 1,3% difficulties in math
 - 3,9% difficulties in reading
 - 2,3% difficulties in math & reading
- Gross-Tsur, Manor & Shalev (1996): 3029 children from Israel, 10 y.o.
 - 6,5 % score < two grade below mean & IQ > 80)
 - 1,1:1 girls:boys
 - 26% of the dyscalculic children met the criteria of ADHD (Conners Q)
- global batteries not suited to detect specific problems, different criteria

Selection criteria

- In the clinical setting
 - Scores on a numerical test -2SD or
 - > 2 years behind and normal intelligence
- In research
 - ≠ cutoff
 - ≠ IQ

Landerl & al. (2004)	3 SD below the mean & teacher's classification, normal IQ
Jordan et al. (03)	< 35 percentile
Shalev et al. (97)	2 grades below CA, IQ > 80
Temple & al. (02)	1 year below CA

A persistent problem

- 3 year follow-up of 123 dyscalculic children (DC)
- Dyscalculic (< pc 5)
- 47% persistent dyscalculia
- 95% scored < 25 pc
- Persistent vs. Non-persistent DC
 - More attention problems
 - More anxiety problems
 - similar performance IQ (100.4 vs. 104.2)
 - equivalent verbal IQ if arith subtest is excluded
 - 46% vs 28% of siblings received arithmetic tutorials

Shalev, Manor et al. (1998), J. Pediatr.

Persisting difficulties

- 6 years follow-up
 - Among the 104 DC children
 - 40 % : score < pc 5 standardised test
 - 95% : score < pc 25
 - The profile may change
 - Difficulties in counting, difficulties in doing simple computations
 - Deficits in the retrieval of simple arithmetical facts from memory
 - Errors in complex (written) calculation
 - Difficulties to handle and understand fractions, decimals

Shalev & al. (2005). Dvptal Med & Child Neurolol

Genetic contribution: genetic syndromes

- Turner syndrome (Rovet & al., 94; Temple & al., 1998; Bruandet & al., 2004)
- Williams syndrome (Paterson & al., 1999)
- Fragile-X syndrome (Hagerman & al., 1992)
- 22q11 (Simon, 2005)

Genetic contribution: family studies

- 31 families of persistent DC (over 3years)
- 149 family members tested for DC
- DC criteria:
 - poor performance in arithmetic (pc25),
 - IQ > 85,
 - significant $\neq$ between math and IQ (> 1 SD)

⇒ half of the family members were DC
 ⇒ 10 x more than in the general population

	% of DC
mothers	67
fathers	41
siblings	53

Shalev et al. (2001)., J. Learning Dis.

Genetic contribution: family studies ADHD and dyscalculia

- ADHD : criteria of the DSM III-R
- Exclusion: major sensorimotor disabilities, psychosis, reading problems, IQ < 80

	Males-ADHD	Males no-ADHD	Females-ADHD	Females no-ADHD
Probands (n)	140	120	140	122
Siblings (n)	174	129	143	131
Parents (n)	280	239	274	238

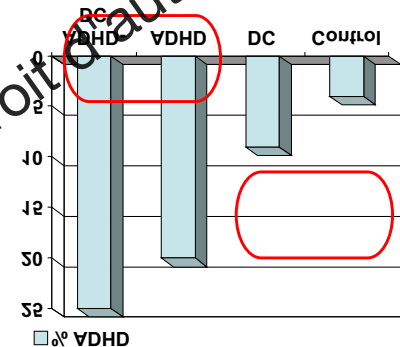
Monuteaux et al., J. Learning Dis. 2005

- Dyscalculia: discrepancy between the WRAT-R score and the one expected on the basis of IQ
 - 5.7% DC among the control probands
 - 10.7% DC among the ADHD probands
 - $\neq$ is significant ($p=.05$)

Monuteaux et al., J. Learning Dis. 2005

ADHD in relatives of probands

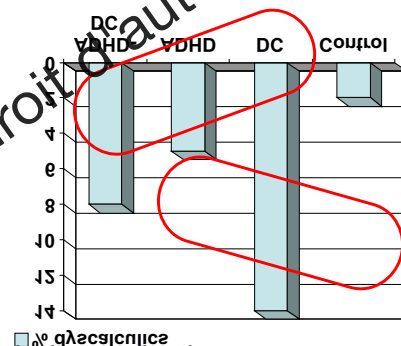
- Increased rate of ADHD in probands with ADHD (with and without dyscalculia) relative of control probands
 - ADHD-DC and ADHD $\neq$ from control ($p<.01$) and DC ($p<.05$)



Monuteaux et al., J. Learning Dis. 2005

Dyscalculia in relatives of probands

- Higher rates of dyscalculia in the relatives of dyscalculics probands (with or without ADHD) compared to the relatives of control probands
 - ADHD-DC and DC > control ($p<.05$)



« ADHD and dyscalculia are independently transmitted in families and are etiologically distinct »

Monuteaux et al., J. Learning Dis. 2005

Genetic contribution: twin studies

- Dyscalculic twins
 - 58% of monozygotic co-twins are DC
 - 39% of dizygotic co-twins are DC
 - Concordance rate is even higher when considering dyscalculic children with not reading difficulties
 - .73 vs .56 (mono and dzy)
 - .85 vs .46 (mono and dzy; no reading diff)

Alarcon & al. (1997), J. Learn. Disabilities

What are the questions ?

- Why do some children present difficulties in learning math ?
 - General cognitive factors ?
 - Specific, numerical factors ?
 - Are these reasons the same for DC and DC-RD ?

General cognitive factors: intelligence

- No problem of intelligence is one of the criteria of the DSM III
- Gross-Tsur & al. (96) selected DC children with an IQ > 80
 - IQ of DC: 98.2
 - Performance IQ: 102.4
 - Verbal IQ (no arith): 94.8
- 3 years later: persistent vs. non-persistent DC
 - Similar performance IQ (100.4 vs. 104.2)
 - Similar verbal (no arith)
- 6 years later: persistent vs. Non-persistent DC
 - ≠ in performance IQ: 98.7 vs. 104.7
 - ≠ in verbal IQ (no arith): 93.2 vs. 97.6

General cognitive factors: WM

- A frequent difficulty in DC concerns simple calculation
 - DC are slower
 - produce more errors,
 - use less mature strategies than controls
 - algorithm :
 - Counting all: $2 + 8 = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$
 - Counting on: $2 + 8 = 3, 4, 5, 6, 7, 8, 9, 10$
 - Counting min: $2 + 8 = 9, 10$
 - Retrieval: $2 + 8 = 10$
 - Support : finger - verbal - mental

Fleischner et al., 82; Geary et al., 87, Geary et al. 90

General cognitive factors: WM

- Geary's hypothesis (1993; Psych Bull)
 - To form an AF in long-term memory, one needs to co-activate in WM the problem and the answer
 - Low WM capacities would prevent the formation of these associations
- The repeated use of counting to solve a problem does not lead to the constitution of an AF (problem-answer in LTM)
 - Thevenot, Barrouillet & Fayol (2001)
 - Addition: 39/16 /55 55 = the sum? 16 (= n1 or n2 ?)
 - Compare: 39/16/25 25 in between? 16 (=n1 or n2 ?)
 - Better recognition of 16 after compare than add

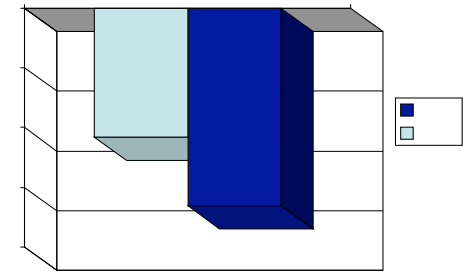
General cognitive factors: WM

- Weaker WM capacities in DC
- Poor WM is associated with immature addition strategies
- Poor WM is associated with less elaborated counting string
- Weak WM capacities may lead to some arithmetical disabilities

WM capacities in DC

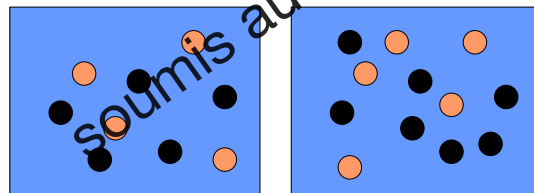
- Lower forward digit span

- Geary, Brown & Samaranayake (1999)
- Hitch & McAuley (1991)



WM capacities in DC

- Weaker central executive capacities
 - Siegel & Ryan (1989)
 - counting span <
 - listening span =



/ four /

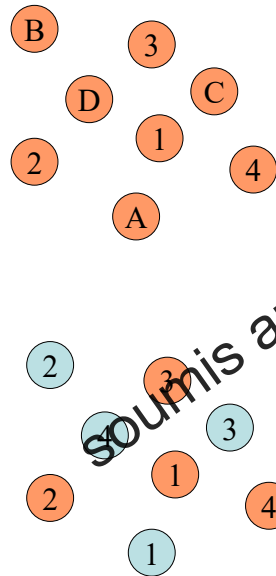
/ five /

/ four five /

WM capacities in DC : Studies controlling for reading disabilities

- Mc Lean & Hitch (1999)

- 8-9 y.o. children: DC (no reading problems) and controls
- PL
 - Forward digit span: DC < controls
 - Non-word repetition: no ≠
- VSSP
 - Corsi: DC < controls
 - Matrices: no ≠
- CE
 - trials tests: DC < controls
 - Missing items: DC < controls



Trial tests

Missing item

$$2+3 = 4+? = ?$$

WM capacities in DC



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WM capacities in DC

- Passolunghi & Siegel (2001; J. Exp Child Psych)
 - Poor / good problem solvers
 - Listening span (.05)
 - Counting span (.02)
 - Animal dual task (.002)
 - Digit span (forward) (.05)
 - Digit span backward (.05)
 - Word forward (ns)
 - Word backward (ns)
- But Geary & al (99)
 - DC, DL, DC-DL, controls
 - forward digit span: No ≠ in
 - Backward digit span: DC-DL < 3 other groups

=> Poorer WM abilities in DC, especially CE

- Low processing speed ? (Bull & Johnston, 97)
- Low inhibition of no more relevant information ? (Passolunghi & al.)

WM and calculation strategies

- Test 3 groups: DC, DC-DL, controls
- in 1st, 3d and 5th grades
- Lower counting span for DC and DC-DL in the three school levels
- Counting span is correlated with
 - More finger counting
 - Less verbal counting
 - More errors in finger counting

Geary & al. (2004) J. Exp Child Psych

WM and calculation strategies

- Test of WM capacities (PL & CE) and processing speed when entering school (grade 1, November)
- Predictive power of these measures on addition
 - PL: digit span, short-word span, long-word span, non-word repetition
 - CE: listening span
 - Processing speed: code subtest (WISC)
- 4 months later: addition
 - algorithm :
 - Counting all: $2 + 8 = 1,2,3,4,5,6,7,8,9,10$
 - Counting on: $2 + 8 = 3,4,5,6,7,8,9,10$
 - Counting min: $2 + 8 = 9,10$
 - Retrieval: $2 + 8 = 10$
 - support : finger - verbal - mental

Noël, Seron & Trovarelli (2004)

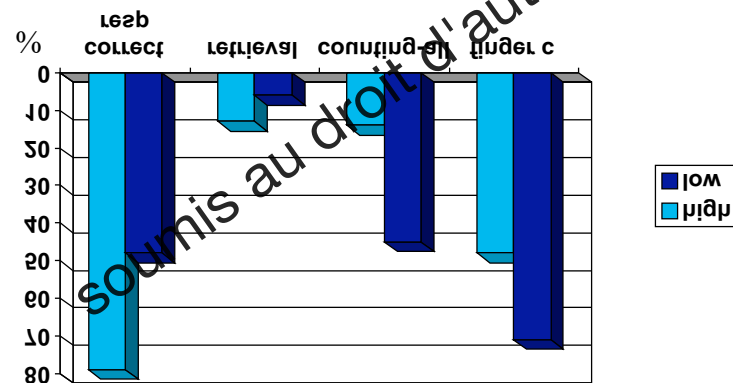
Results

- the general processing speed measure had no significant predicting power



*: $p=.05$; *: $p=.025$; **: $p<.01$; ***

Subgroups with low vs. high PL capacities



Interpretation

- Weak WM capacities => less accurate
 - => monitoring the counting string (cf. studies: Healy & Nairne, 85; Logie & Baddeley, 87):
 - => monitoring the number of counting steps
- Weak WM capacities => concrete support needed to monitor the counting steps
 - => finger counting
- Weak WM capacities => less mature counting strategies
 - Why ? Immature counting string ?

WM in learning to count ?

- PL capacities have been shown to predict vocabulary acquisition
- What about the number words ?
- Particularities
 - Number words must be recited in a specific order
 - The counting string needs to be elaborated
 - *Unbreakable list*
 - *Breakable chain (start counting from $n \neq 1$)*
 - *Unbreakable chain (counts number words)*
 - *Bidirectional chain (recite in both directions)*

WM in learning to count ?

Predictions

- Phonological loop capacities are related to
 - Development of the number vocabulary
 - Development of the counting string (order)
- Central executive capacities are related to
 - The level of elaboration of the counting string
 - Ability to use counting to solve additions

WM in learning to count ?

Method

- Population
 - 4 y.o. Children (38) & 5 y.o. Children (42)
- Evaluation of
 - Counting level
 - Count as far as you can
 - Number fluency
 - Count from 1 up to a number
 - Count x steps from a given number
 - WM capacities
 - Storage: word span and nonword repetition / Corsi span
 - CE: reverse order word span / short-words span with categorical restitution

WM in learning to count ?

Results

- Split of the population in two subgroups
 - Those with lower memory spans than expected for their age
 - Those with higher memory spans than expected for their age
- No $\neq$ when groups are based on the VSSP measure
- $\neq$ when groups are based on the PL or the CE measures

soumis au droit d'auteur

Low WM: a way to DC ?

- Weak WM capacities =>
 - Smaller number vocabulary
 - Less extended number string
 - Lower level of elaboration of the counting string
 - Less mature counting strategies in addition
 - Weaker abilities to monitor counting for calculation
 - More calculation errors
 - Use of external support
 - Poor conditions for establishing an association in LTM between a problem and the correct answer

General cognitive factors: inhibition

- DC have low CE capacities because they can not suppress no more relevant information from WM (Passolunghi & Siegel, 2001, 2004)
- DC is often associated with ADHD (inhibition problem)
- DC's problems with AF (slow RTs and more errors) could be due to their difficulty to deal with interference in the AF network

General cognitive factors: inhibition

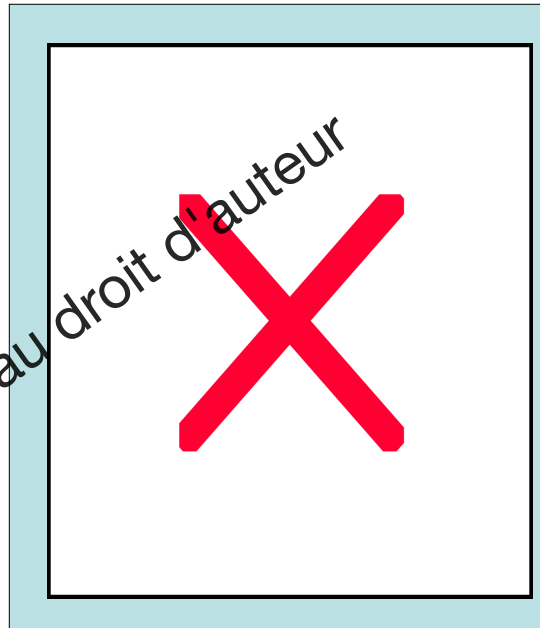
- AF are stored in a long-term memory network with many interference
 - Errors are often table-related ($8 \times 4 = 24$)
 - There can also be naming errors ($2 \times 8 = 28$)
 - There is an operation effect ($4 + 5 = 20$)

=> inhibition is needed to deal with that interference

Inhibition = Active suppression mechanism that prevents irrelevant information from disrupting cognitive processing (Harnishfeger, 1995)

Network Interference Model
Campbell (1984, 1995)

- the presentation of a problem activated many different responses



General cognitive factors: inhibition

- Barrouillet, Fayol & Lathulière (1997)
 - Adolescents with learning difficulties in math
 - Multiple choice task
 - $4 \times 6 = 18, 24, 28, 30$ (table-related foils) 74% cr
 - $4 \times 6 = 21, 24, 25, 27$ (table-unrelated foils) 83% cr
 - $4 \times 6 = 22, 23, 24, 26$ (non-table foils) 82% cr
 - => more difficulties when foils are table-related
 - But children with very low IQ (mean of 75), no control group
- Bull & Scerif (2001)
 - 7 y.o. Children: significant correlation between math performance and a numerical Stroop (222, 333: say how many symbols) but not with a Colour Stroop (blue)

General cognitive factors: inhibition

- Inhibition has $\neq$ functions (Friedman & Miyake, 2004)
 - Controlling interference from external distracters
 - Inhibiting dominant responses
 - Suppression of non-relevant information
- $8 \times 4 \Rightarrow$
 - => 16, 24, 32
 - => 16, 20, 24, 28, 32, 36
 - => selecting 32 but inhibiting 16 or 24
 - => inhibition of the dominant response ?

- **Learning disabled:** 11 y.o, n=15; IQ 98 ± 9 ; > 2 years behind in math and reading
- **Controls:** 11 y.o., n=15; IQ 104 ± 12 ; no learning problems

- Inhibition of external distracters
 - Flankers letters: Congruent - Incongruent
 - Flankers digits: DDDDDDD GGGDGGG
- Inhibition of a dominant response
 - Colour Stroop: 2222222 1112111
 - Digit Stroop: red blue
 - 22 33

Congruity effects



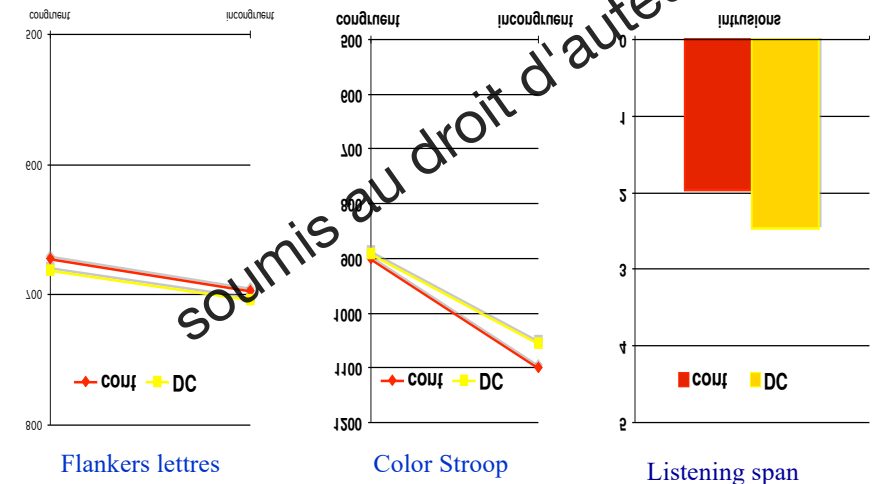
General cognitive factors: inhibition

- Problem for inhibiting information that are no more relevant for the task at hand ?
- When learning AF
 - $6 + 3 = 8, 9$
 - Keep in WM the problem and the last number produced (the response) but inhibiting the intermediate results

General cognitive factors: inhibition

- **Math disabled:** 10 y.o., $n=20$; $IQ\ 98,4 \pm 7$; $<pc15\ math >pc50\ reading$
- **Controls:** 10 y.o., $n=20$; $IQ=101 \pm 9$; $>pc\ 50\ math\ \&\ reading$
- Congruent - Incongruent
 - Inhibition of external distractors
 - Flankers letters: DDDDDDD GGGDGGG
 - Inhibition of a dominant response
 - Stroop colour: red blue
 - Suppression of irrelevant information
 - The crone if for the king.
Horses live in nests.
Wrong answer: crone - nests

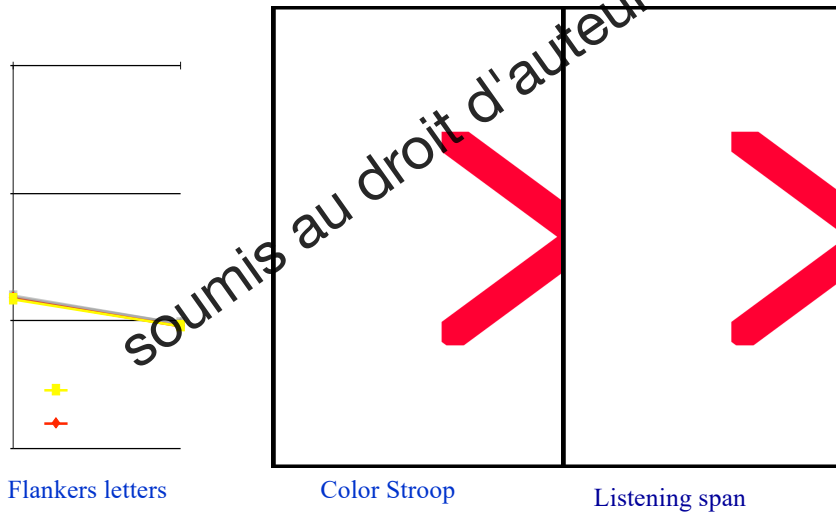
Controls vs. DC



Contrôles vs. Weak in arihmetical facts

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Fluency in multiplication (1' test): < pc 25



General cognitive factors: inhibition ?

- When considering DC children with adequate IQ (DC only, DC-dyslexics or DC for AF), there was not sign of inhibition deficiency in any of the three functions of inhibition
 - Inhibiting external distractors
 - Inhibiting dominant responses
 - Inhibiting no more relevant information
- same conclusion by van der Sluis et al. (2004). *J. of Experimental Child Psychology*.

General cognitive factors: Long-term memory

- DC children have difficulties to store and retrieve AF in LTM
- AF might be stored in a verbal format in LTM (Dehaene, 1992)
 - DC children are slower
 - in speeded naming tasks (Geary & al., 91; Kirby & Becker, 1988) but not always (Geary & Brown, 1991)
 - DC children are slower to count (Hitch & McAuley, 1991)
 - Significant correlation between articulation speed and frequency of AF retrieval in LTM (Bull & Johnson, 1997)

=> Geary et al. (2000): hypothesis of a deficit in retrieving verbally coded information from LTM

- Associate a multiplication to its product
- Associate a verbal expression to its ending word
- Associate a capital to its country
- Associate a form to another similar form (speed of processing, of selecting an answer, no retrieval from LTM)

Faits arithmétiques	Verbal expression	Association pays - capitale	Association perceptive
2 x 3	avoir la chair de	PARIS	□
6 x 8	poule canard	FRANCE SUISSE	○ □

Mussolin & Noël

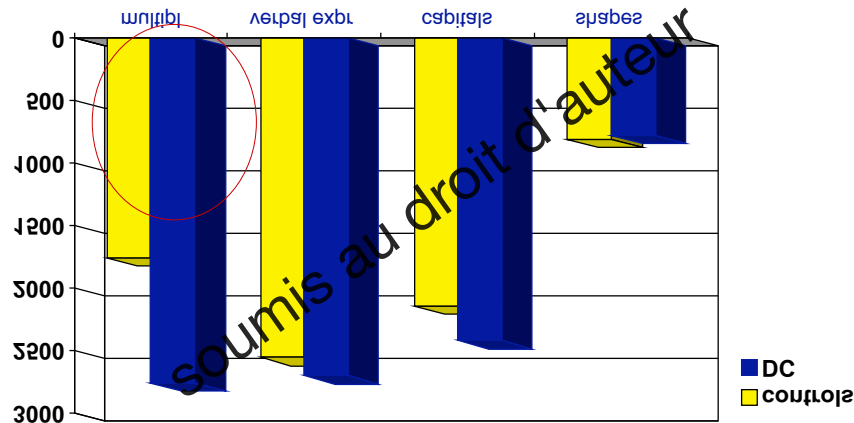
General cognitive factors: Long-term memory

- If deficit is **specific**, the only $\neq$ between the 2 groups is for the multiplication
- If deficit is in **learning verbal association** then $\neq$ could be seen in multiplication and verbal expressions
- If deficit is in learning **« arbitrary associations »** then $\neq$ could be seen in multiplication and in country/capitals
- If they are **globally slower**, $\neq$ should be seen in all the tasks

General cognitive factors: Long-term memory

- Population
 - 18 DC children (score < 40 au KRT)
 - 18 controls (score > 40 au KRT)
 - No reading problems (tests L3 et LUM)
 - IQ > 85
 - Two groups paired on age, sex, IQ and education

Mussolin & Noël

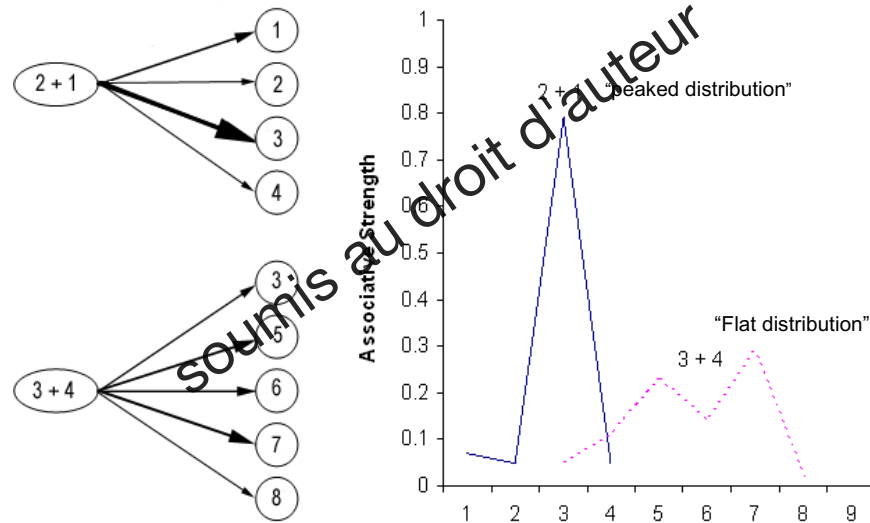


=> Specific difficulties in accessing AF from LTM, why ?

Siegler's Distribution of Associations Model (1988, 2000)

- ♦ Developmental model
- ♦ Each time an answer is generated in response to a problem, an association between this problem and that answer is created in LTM
- ♦ => problems are associated to the appropriate response as well to errors
- ♦ The associative strength between a problem and an answer increases with the frequency of production of that answer
- ♦ What is really important is the relative associative strength,
 - ♦ The associative strength of a given answer relative to the associative strengths of all answers to that problem
- ♦ This determines whether this answer will be the one retrieved and the speed to retrieve it

Distribution of Association



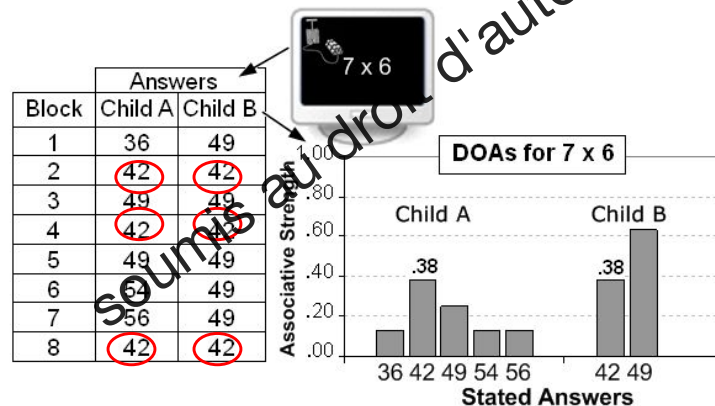
DOA in DC ?

- 3 groups
 - DC 4th grade
 - Control -same age
 - Control - Ability-Matched
- DC criteria
 - Mental arith test < p. 35
 - Reading test > p. 31
 - IQ > 85
- DC and ability matched have the same score on a multiplication fluency task

	DC	Age-Matched	Ability-Matched
N	11	11	11
Age (in months)	117.09 (3.48)	115.91 (3.27)	105.00 (4.60)
IQ	102.11 (8.90)	102.64 (9.21)	102.11 (8.11)
LVS-Mental Arithmetic	37.18 (7.64)	54.82 (2.04)	
Multiplication Fluency	30.55 (8.21)	54.36 (14.62)	30.27 (8.04)

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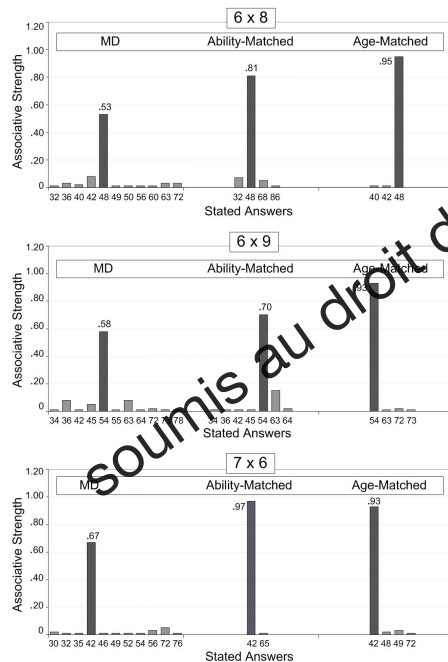
12 multiplications presented 8 times
Stressing the speed of responses (within 3 sec)



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- Speed for accurate responses:
 - DC = ability matched > controls same age
- Errors: more errors and flatter distributions for DC than ability matched, and controls of the same age

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DOA in DC ?

- Flatter distribution in DC than in ability-matched
- More aberrant associations
 - non-table errors
 - very distant operand-related errors
- Many competitors => weaker relative associative strength with the correct response
 - => less retrieval of correct responses
 - => Slower retrieval of correct responses
- => no need to resort to an hypothesis
 - of weaker active inhibition capacities
 - of a general problem to access information in LTM
- Why do DC children build these flat DOA ? Weak WM ?

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General cognitive factors: finger agnosia ?

- “*whenever a counting technique (...) exists at all, finger-counting has been found (...)*” Dantzig
- Common ethymological roots : “digit” - “digital”; “five” - “fingers”
- Fingers are used to count (one finger for one object) and to touch the objects we count
- Fingers can be used to access the magnitude of number words
 - Which is bigger, three or five ?
 - => recite the number names, raise one finger more each time, compare the collections of fingers
- Fingers are used to calculate: add - subtract
- Fingers are used in a regular order => configurations to represent numerosities => help accessing the cardinal meaning of a number words

General cognitive factors: finger agnosia ?

- Gerstmann syndrome (1924)
 - Lesion on the dominant parietal lobe: acalculia, finger agnosia, left-right disorientation & agraphia
- Kinsbourne & Warrington (69)
 - 8 children with finger agnosia, 6 of them were at least 2 years behind their age in mathematics
- Fayol, Barrouillet & Marinthe (98)
 - Neuropsychological test including finger gnosia in 189 children (5;9 y.o.) predicts mathematical performance 1 and 3 years later
- Noël (2005)
 - Finger agnosia at 6 years better predicts math skills one year later than processing speed

General cognitive factors: finger agnosia ?

- Population: 98 children (6 y.o.):
 - 16 with low scores in finger gnosis
 - 16 with high scores in finger gnosis
- Significant $\neq$ between the two groups in the numerical tasks
 - Slower to show x with your hands
 - Less good in "Count as far as you can"
 - Slower in Arabic digits: which one come first when you count ?
 - Reduced subitizing rank
 - More errors in simple additions
- Poster: playing a musical instrument leads to better finger gnosis as well as to better numerical skills (in grade 5 but not in grade 2 after one year of practice)

Gracia-Bafalluy & Noël

General cognitive factors: finger agnosia ?

- Fingers have a critical role in the development of numerical abilities in children
- Finger gnosis predicts numerical abilities
- In case of lesion, finger agnosia can be associated with acalculia
 - "how loss of the finger sense leads to dyscalculia in skilled adults who no longer count on their fingers?" (Butterworth, 99)

General cognitive factors: finger agnosia ?

- Finger movements and finger positions, as they are used in numerical tasks, get associated with numerical meanings
- Finger and hand shapes are represented in the parietal lobe (mirror cells for planning movements of the hand and fingers)
- The number representation gets associated with finger/hand representation in the parietal lobe

Functional relationship => geographical proximity
Links in development links in acquired cases

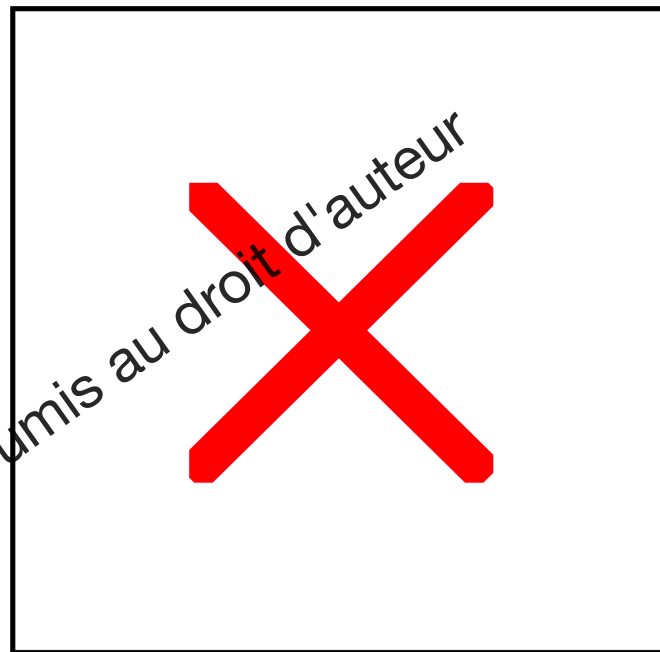
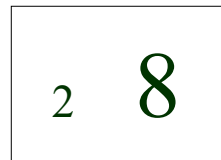
Butterworth, 1999

General cognitive factors: visual-spatial factors ?

Numerical factors: number sense

- Populations (8-9 y.o), IQ =
 - 18 control children
 - 10 RD (< pc25 in reading)
 - 10 DC (< -3ET in AF)
 - 11 DC and RD
- DC and DC-RD are slower
 - Reading 1 & 2 digit Arabic numbers ...even when controlling for colour naming speed
 - point 1-20, 45-65, 2 to 20 (by 2), 20-1
 - Dot counting
 - Comparing the magnitude of 2 Arabic digits, but not their physical size

Landerl, Bevan & Butterworth (2004) Cognition

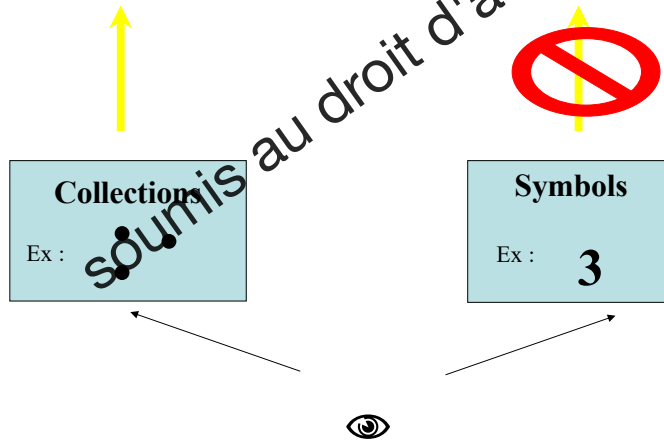
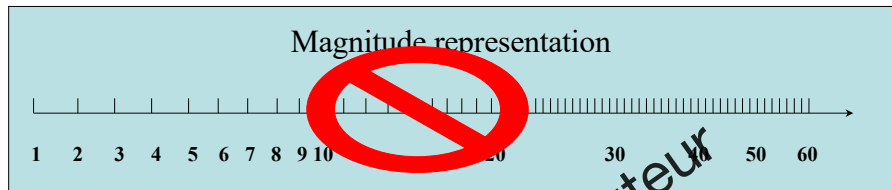


Landerl, Bevan & Butterworth (2004) : Dysfunction of the number sense

But all the tasks used require the processing of symbols
(Arabic digits or number words)

↳ Possible hypothesis

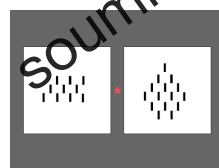
↳ Magnitude representation is intact but the problem lies in the access to this representation from symbolic codes



- processing quantities from a symbolic code

2 5

- processing quantities from collections



Easy Condition



Difficult Condition

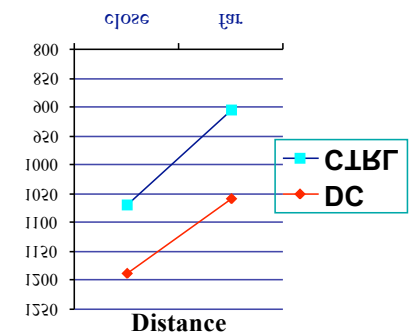
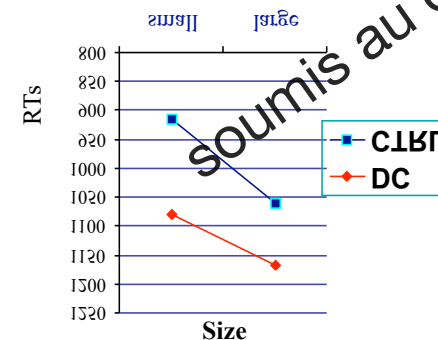
Rousselle & Noël (Cognition, 2006)

- 499 second grade children
- Selection on the basis of a collective testing
 - Writing Arabic numbers
 - Comparing Arabic numbers
 - Transcoding tokens into Arabic numbers
 - Additions & subtractions with no temporal constraints
 - Additions fluency
- if score < 15 and same evaluation by the teacher
 - 46 DC children (half were DC-RD)
 - 47 control children
- => same age (8 y.o), same intellectual level (WISC)

Comparaison of Arabic digits

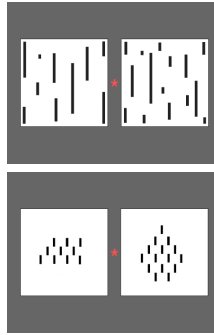
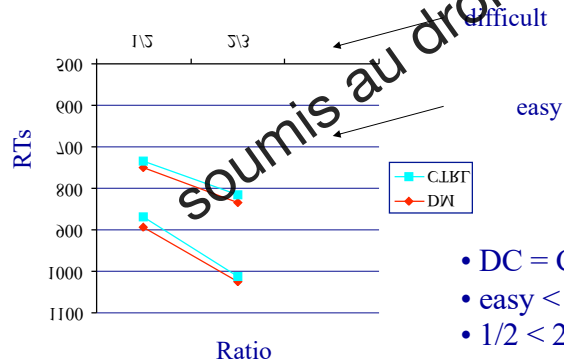
	Distance 1	Distance 3-4
small	1-2 2-3 3-4	1-4 1-5 2-5
large	6-7 7-8 8-9	5-8 5-9 6-9

- DC are globally slower
- Show reduced size and distance effects



Comparing collections

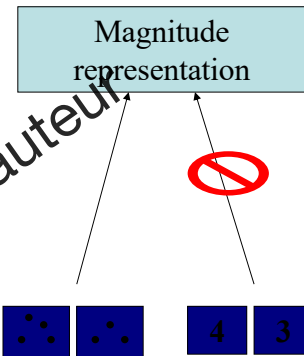
easy		difficult	
1/2	2/3	1/2	2/3
6-12	6-9	6-12	6-9
8-16	10-15	8-16	10-15
14-28	16-24	14-28	16-24



- DC = CTRL
- easy < difficult
- 1/2 < 2/3

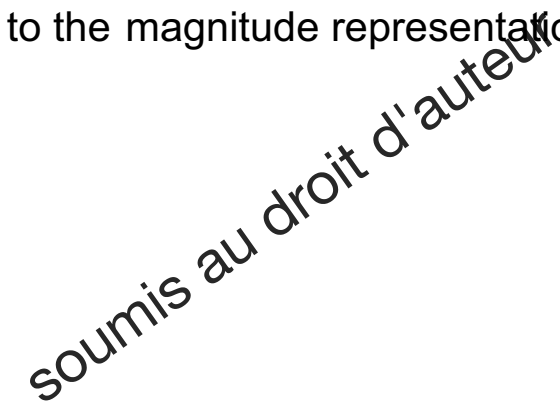


Conclusion



- ⇒ Magnitude representation is preserved
- ⇒ Difficulties in accessing magnitude representation from symbolic codes

Numerical factors: automatic access to the magnitude representation





Number comparison

- Effect of congruency
- similar in all the groups

Size comparison

- No effect of congruency

Landerl & al. 2004, Cognition

Automatic activation of magnitudes ?

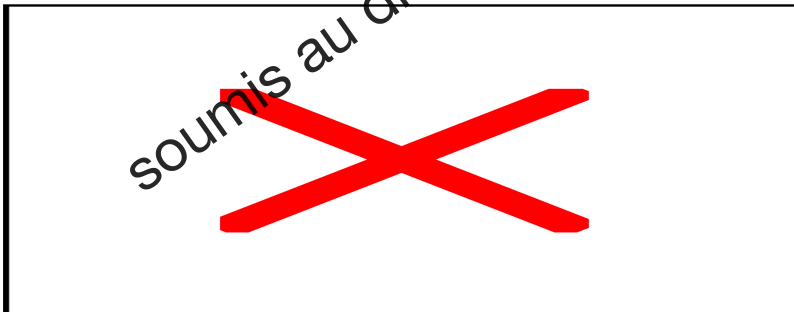
- Adults:
 - 19 who were diagnosed in the past as having dyscalculia difficulties (DC) (no dyslexia or ADD or ADHD);
 - 19 controls
- Three comparisons

Physical size	Height	Grayness
5 3	5 3	5 3

Rubinsten & Henik, 2005, Neuropsychology

Automatic activation of magnitudes ?

- Group x task x congruity ($p=.05$)
 - *Grayness*: congruity effect in controls (interference) but not in DC
 - *Height*: congruity effect in controls (interference) but not in DC
 - *Size*: group x congruity: ns; congruity effect in controls (interference & facilitation) and in DC (interference)



Rubinsten & Henik, 2005, Neuropsychology

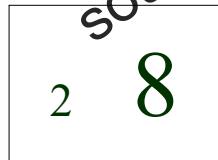
Automatic activation of magnitudes ?

- Conclusion
 - “DC group have an intact internal representation of magnitude (...) if it had been damaged, no congruity effect could have appeared in any of the tasks”
 - “people with DC have problems automatically associating internal representations of magnitude to Arabic numerals”

Rubinsten & Henik, 2005, Neuropsychology

Automatic activation of magnitudes ?

- Population
 - 17 dyscalculics adults (no dyslexia or ADD or ADHD)
 - 17 dyslexics adults
 - 1 controls adults
- Numerical Stroop
 - Numerical comparison: select the larger number
 - Physical comparison: select the digit in the bigger physical size

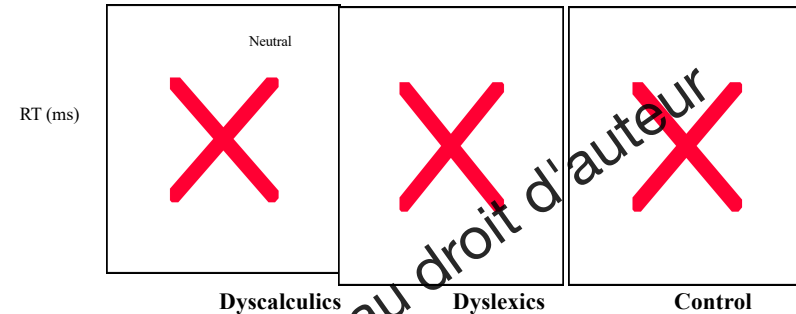


Rubinsten & Henik, in press, Educ. Psych.

Navon task:

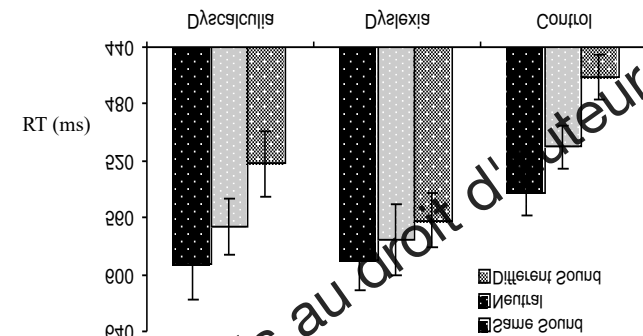
- a big Hebrew letter made of small letters with the same sound or a ≠ one
- Name the larger or the smaller letter

Rubinsten & Henik, in press, Educ. Psych



- Physical judgment was faster than numerical comparison
- This difference was larger for the dyscalculics
- Numerical comparison
 - Same congruity effect (of the irrelevant physical sizes) in the three groups
- Physical comparison
 - Smaller congruity effect in the dyscalculia group, composed only of an interference effect

Rubinsten & Henik, in press, Educ. Psych



- Responding was faster in controls
- Phonological congruity effect, but smaller in the dyslexics

Rubinsten & Henik, in press, Educ. Psych

Automatic activation of magnitudes ?

- The ability of the dyscalculia group to automatically associate Arabic numerals with their representation of magnitude is not fully automatic
- The ability of converting graphemes to phonemes would not be fully automatic in dyslexic participants

Rubinsten & Henik, in press, Educ. Psych

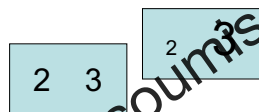
Automatic activation of magnitudes ?

- In Landerl & al., the $\neq$ between the physical judgment and the numerical judgment might have been so important that the numerical information did not have the time to interfere with the physical judgment
- In Rubinsten & Henik (in press), the $\neq$ between physical and numerical judgment was larger for dyscalculics than the other groups ... This could possibly explain their smaller congruity effect ?

Rousselle & Noël, 2006, Cognition

Automatic activation of magnitudes ?

- Paradigm used by Mussolin & Noël (J. Clin Exp Neuropsych, in press)
- Balancing the speed of physical and numerical judgment
 - Measuring the speed of numerical judgment 2 - 5
 - Measuring the speed of physical judgment 2 - 2

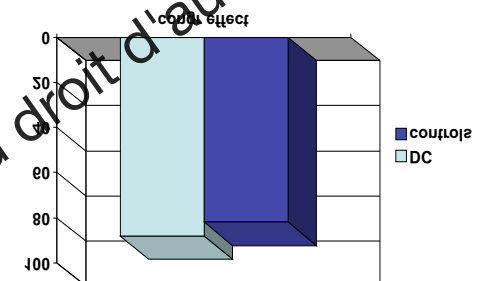
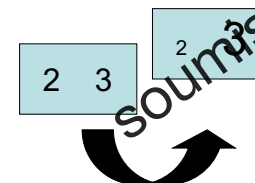


SOA : the $\neq$ between physical & numerical judgment, calculated for each individual

Rousselle & Noël, 2006, Cognition

Automatic activation of magnitudes ?

- Congruity effect
- Similar in the two groups



Rousselle & Noël, 2006, Cognition

Automatic activation of magnitudes ?

- Dyscalculic children are slow to access magnitude from numerical symbols
- But if that particularity is taken into account, they show the same automatic activation of magnitude as controls

conclusion

- General cognitive factors ?
 - Not a problem of inhibition nor of accessing information from long-term memory
 - For some DC, a problem of WM
- Numerical factors
 - Maybe not a default in the number sense
 - Maybe not a default in the automatic access to magnitude
 - Probably a default in accessing magnitude representation from symbols
 - Fingers might play a role in this connection: analogical representation, serial order, typical configurations that act as first symbols ?
- DC and DC-RD:
 - not different ... Just more difficulties for DC-RD in situation where language plays an important role

- These conclusions hold for groups of participants, not for each dyscalculics !
 - $\neq$ between control and dyscalculic children in magnitude comparison of Arabic digits
 - But only 9/42 dyscalculics have RTs > controls by 2 SD
 - 13/42 have normal RTs (< .5 SD from the controls)
- It is possible that different (cognitive) causes provoke dyscalculia

Thanks to my PhD studies and all the team !

- Laurence Rousselle
- Christophe Mussolin
- Sandrine Censabella
- Maria Gracia-Bafalluy
- Gaëlle Meert
- Sandrine Meas
- And Xavier Seron and Mauro Pesenti and ...

Kindergarten predictors of math learning disability

- 210 children studied for 4 years
- Testing in kindergarten
 - Basic math
 - Key-math test (numeration, addition, measurement & geometry)
 - TEMA: Tests of Early mathematics Ability
 - Woodcock Johnson-R Math calculation subtest (basic concepts, operations, applications)
 - Reading-related skills
 - Letter name identification;
 - RAN: rapid automatized naming (colours, numbers, objects)
 - Visual-spatial skills
 - Developmental test of visual perception
 - Stanford Binet Intelligence test
- Prediction MLD: <10 pc on both grade 2 & 3 => n=23

Mazzocco & Thompson, 2005, Learning Disabilities Research & Practice

Kindergarten predictors of math learning disability

- Predictive models based on test scores
 - Key-math (geometry & measurement subtests): 78.9% correctly classified
 - Key-math (the 4 subtests) and TEMA: 83.6% cc
 - Key-math (the 4 subtests), TEMA, visual perception test and RAN: 79.1% cc
 - o note: 4 items are always included in these models
- Prediction based on items
 - Number consistency (with fewer than 6 items)
 - Reading 1-digit numerals
 - Additions with 1-digit numbers (manipulatives)
 - Comparing 2 1-digit numbers
 - => 83.7% cc
 - But low PPV% of MLD among those who test positive (38.8%) => too much false positive (but are they also weak learners in mathematics ?)
- => best predictors : some numerical skills (not RAN on numbers, not counting larger sets (> 13) or small ones (<6)), no visual-spatial skills, no reading skills

Mazzocco & Thompson, 2005, Learning Disabilities Research & Practice

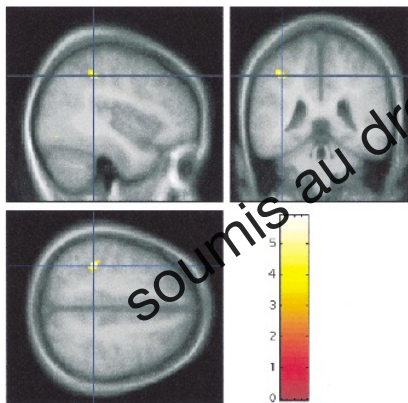
Etude de Molko et al. Neuron (2003)

- Comparaison de sujets adultes contrôles vs. porteurs d'un syndrome de Turner
- IRM structurale: altérations structurale du sillon intrapariétal droit chez Turner (longueur, profondeur)
- IRM fonctionnelle dans des tâches de calcul: variations atypiques de l'activité cérébrale en fonction de la taille des nombres.

Etude de Isaacs, Edmonds, Lucas & Badian
(2001)

- Deux groupes d'adolescents, des prématurés
 - Résultats en calculs comparables à ce qui est attendu sur base de leur intelligence
 - Résultats en calculs inférieurs à ce qui est attendu sur base de leur intelligence
- Imagerie par résonance magnétique au repos

Résultats



- Une seule région distingue les deux populations:
 - *Sulcus intrapariétal gauche*
 - Densité de matière grise inférieure chez sujets pauvres en calcul