

# Calibration of a 1D ejector model from full-scale experiments

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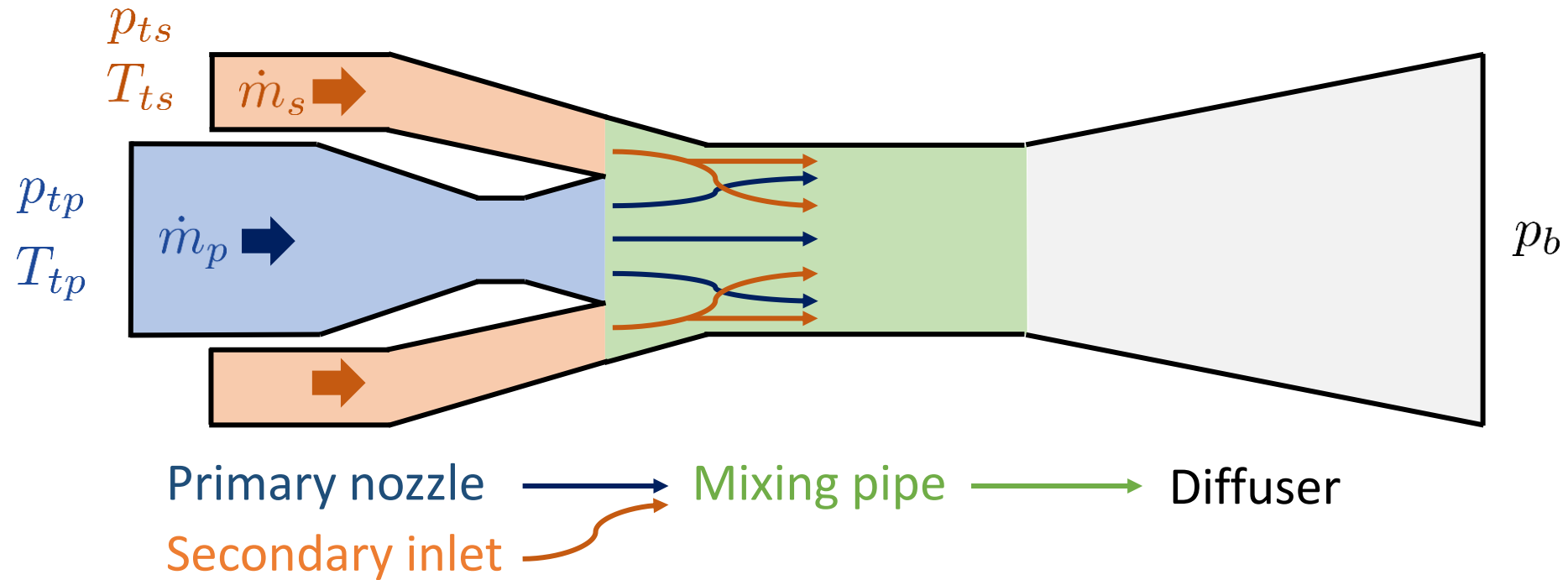
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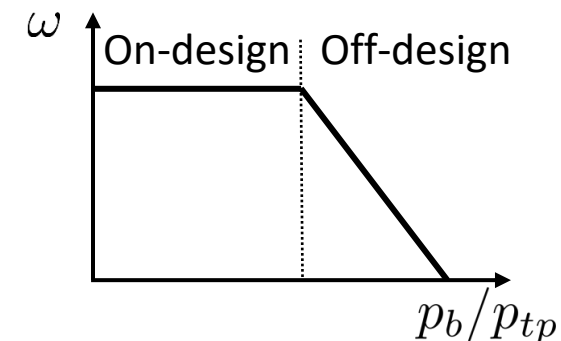
# What is an ejector?



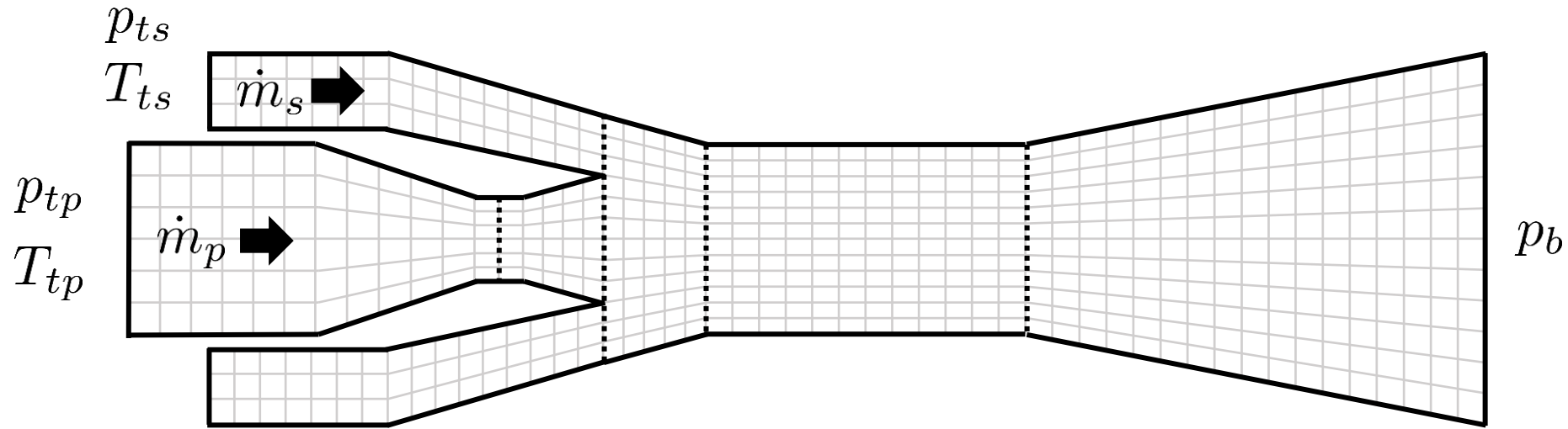
The back pressure  $p_b$  determines the entrainment ratio  $\omega = \dot{m}_s / \dot{m}_p$

The mixed flow is choked in the on-design regime

$$\dot{m}_p, \dot{m}_s = f(p_{tp}, T_{tp}, p_{ts}, T_{ts}, p_b)$$



# What are the modelling options?



## 0D: global balances

- ✓ Fast
- ✗ Only global information
- ✗ Calibration

## 1D: a compromise

- ✓ Local information
- ✓ Fast
- ✗ Calibration (2D effects)
- ✗ Complex

## 2/3D: classic CFD

- ✓ Detailed flow field
- ✓ No calibration
- ✗ Computational cost
- ✗ Meshing and modelling

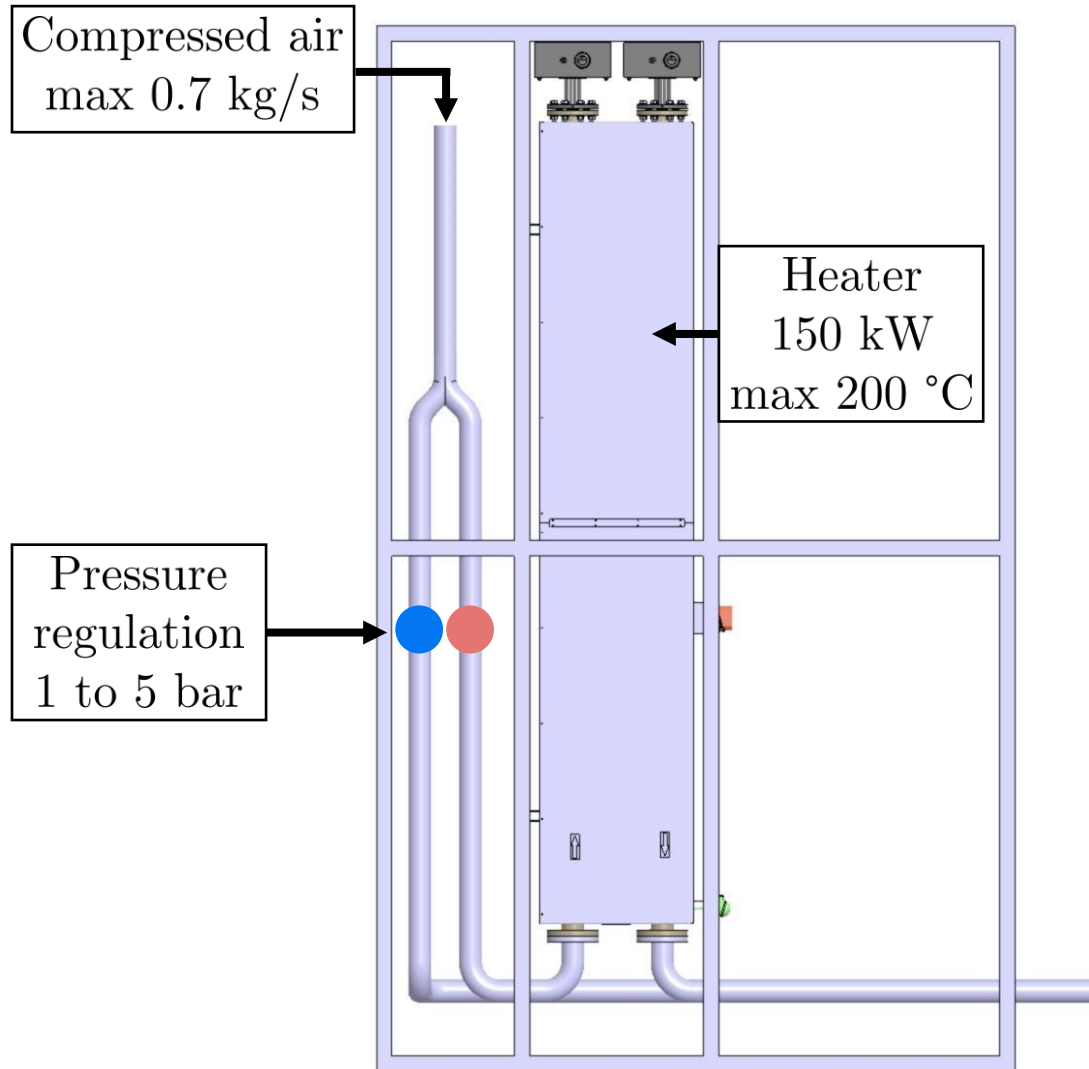
Fast models require data and calibration tools!

# Contents

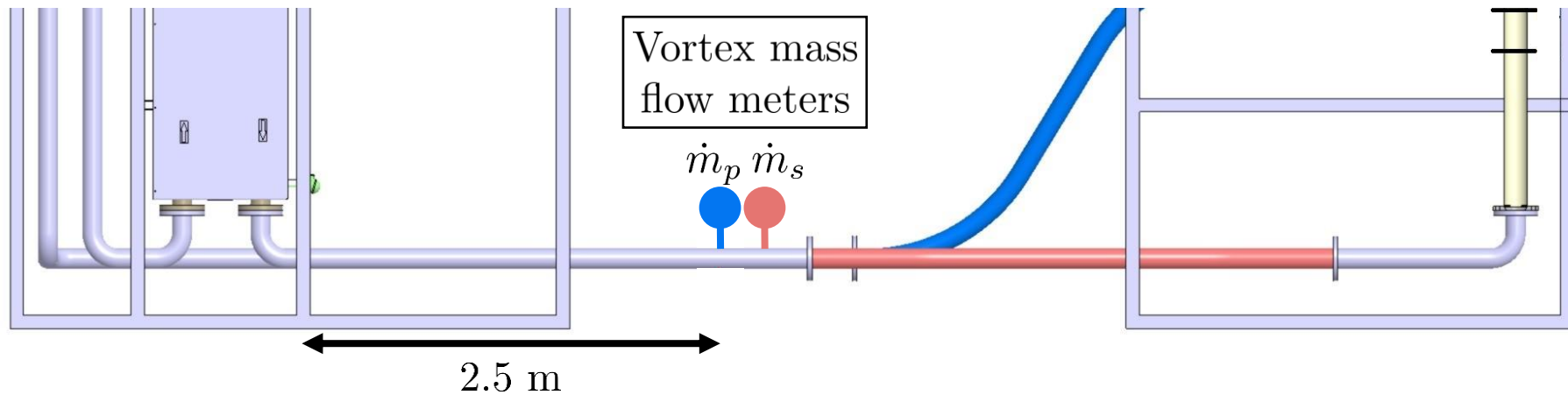
- **Experimental campaign: data**
- Calibration of a 1D ejector model: tools
- Conclusion



# Experimental facility



# Experimental facility





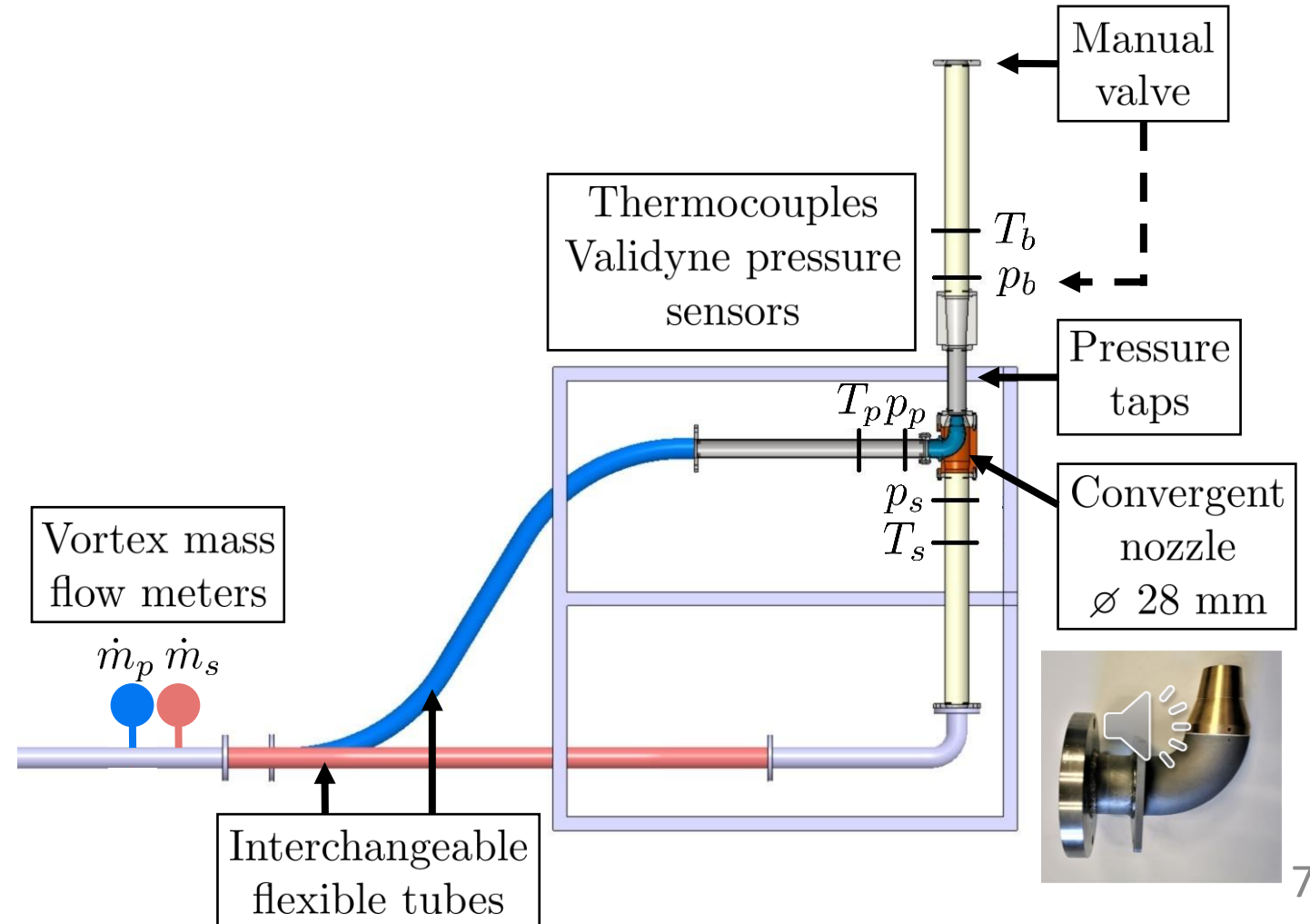
# Experimental facility



(not included here)

Data consists of:

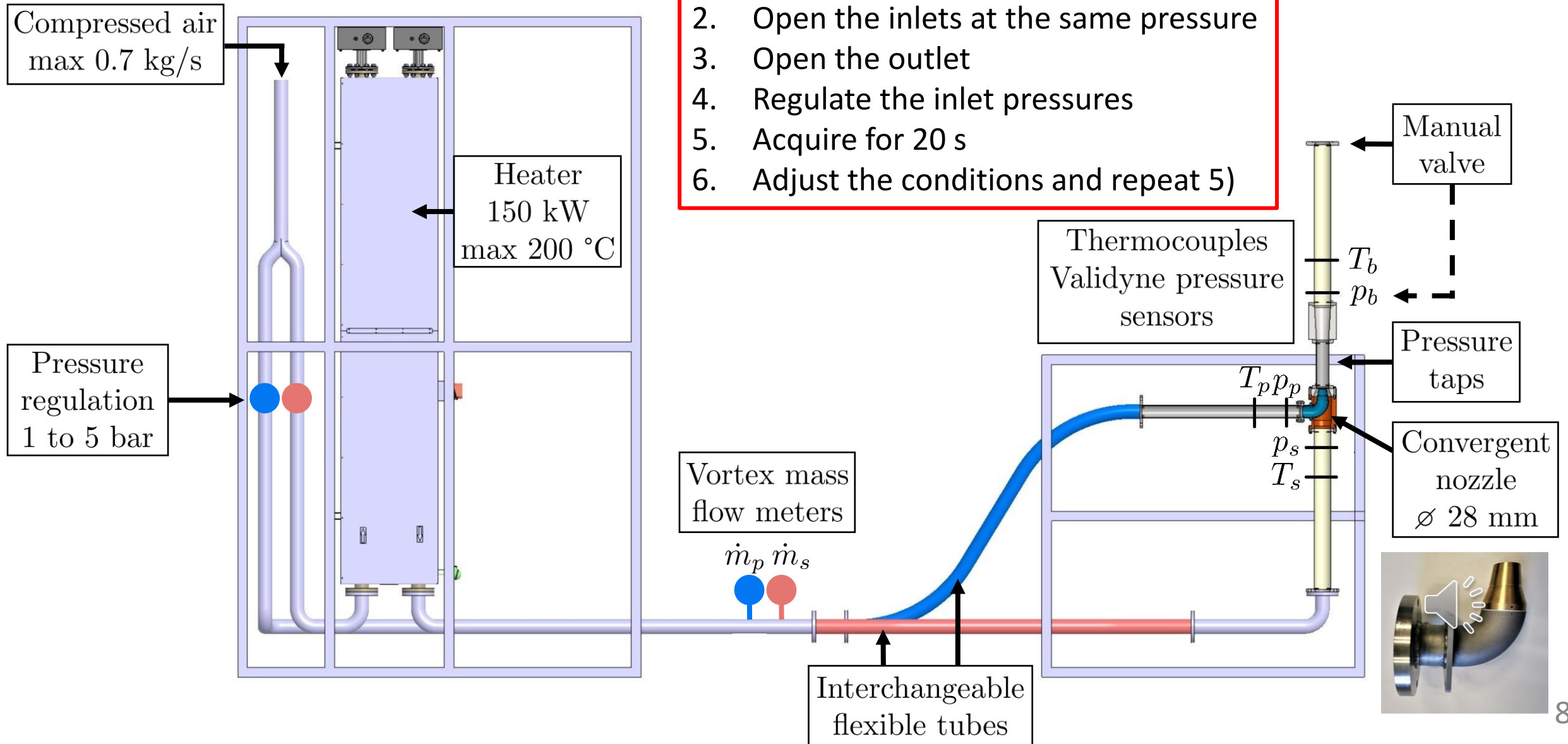
$$\dot{m}_p, \dot{m}_s = f(p_{tp}, T_{tp}, p_{ts}, T_{ts}, p_b)$$



# Experimental facility

## Procedure for an operating curve

1. Close the outlet
2. Open the inlets at the same pressure
3. Open the outlet
4. Regulate the inlet pressures
5. Acquire for 20 s
6. Adjust the conditions and repeat 5)

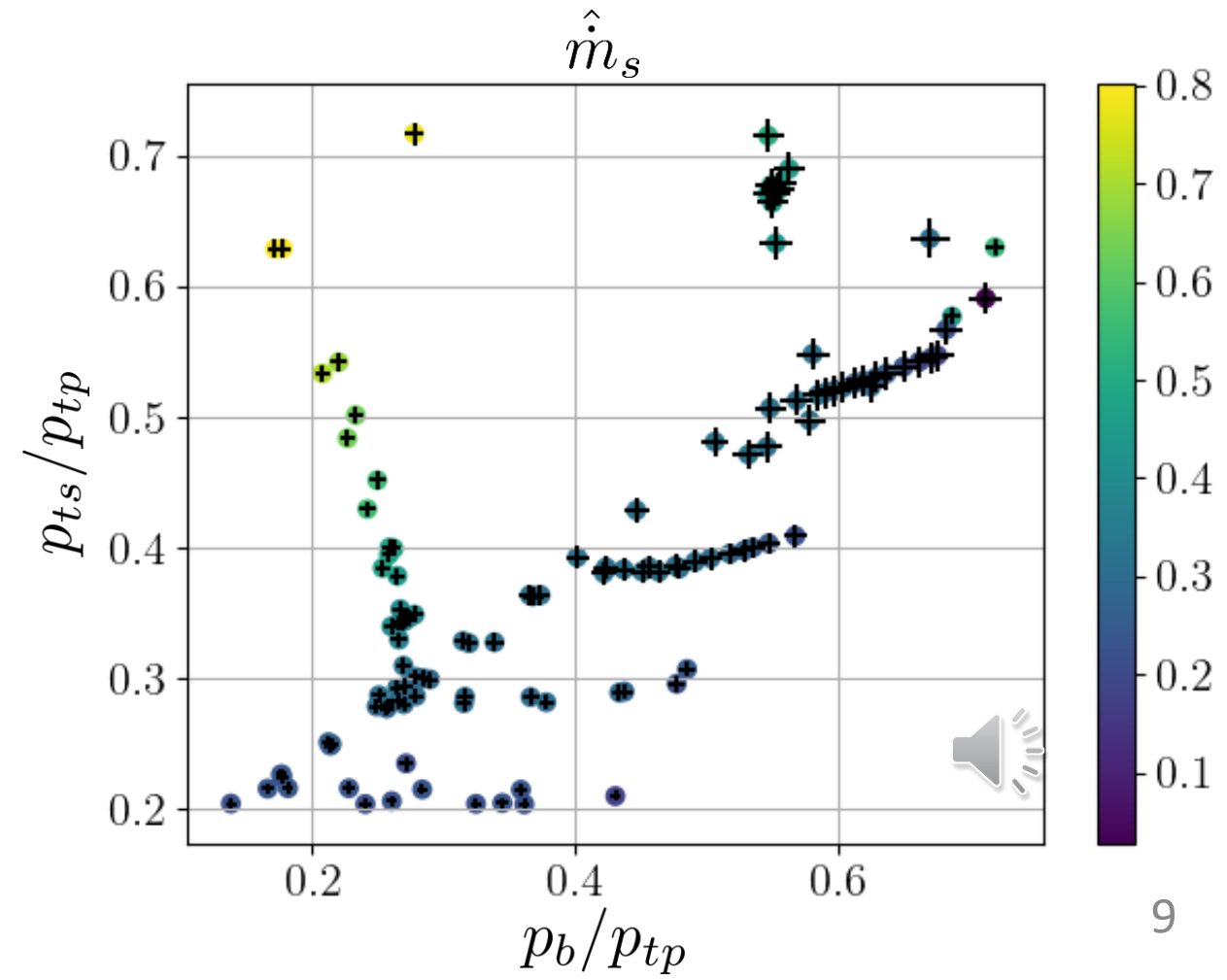
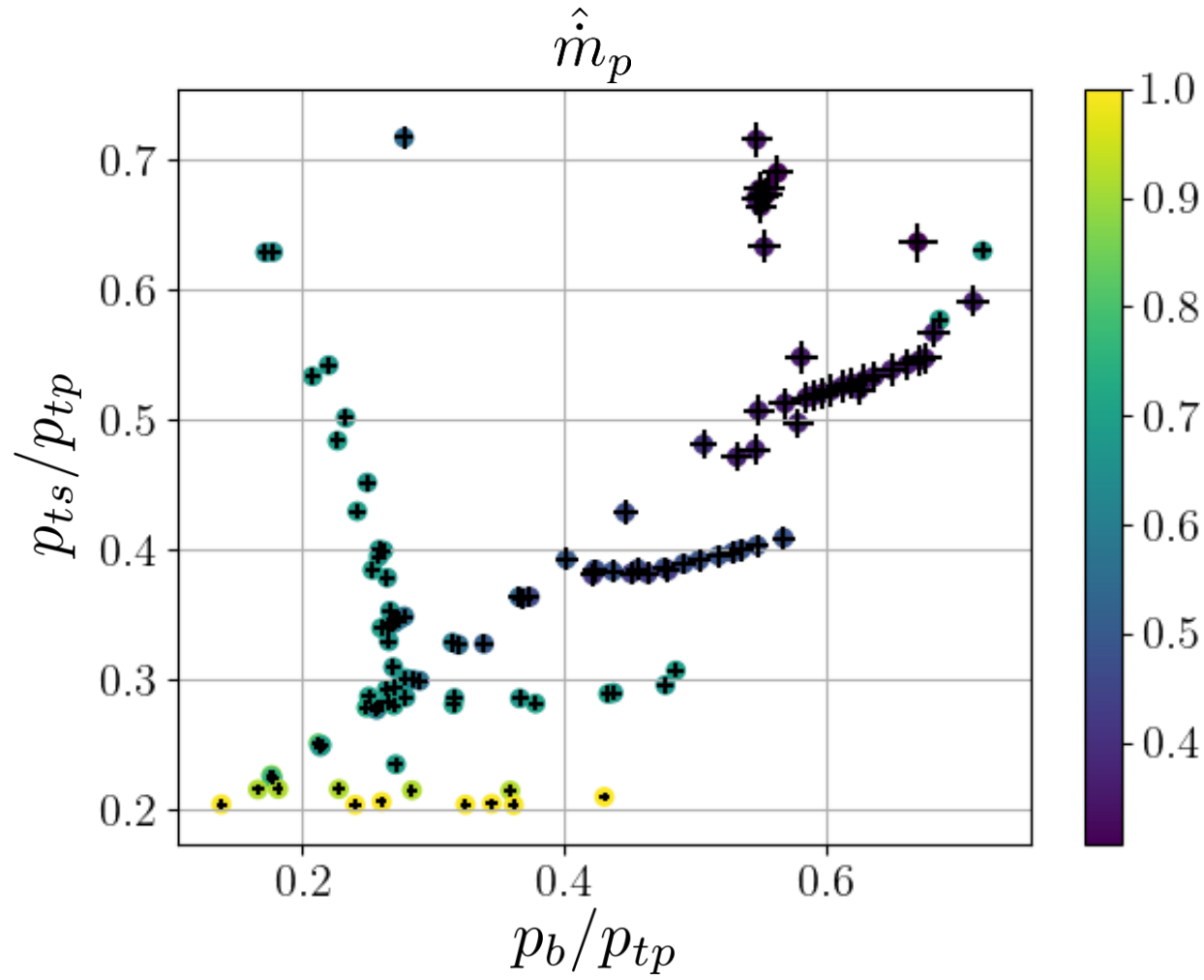




# Experimental results

$$\dot{m}_p, \dot{m}_s = f(p_{tp}, T_{tp}, p_{ts}, T_{ts}, p_b) \quad (1.5 \% \text{ uncertainty})$$

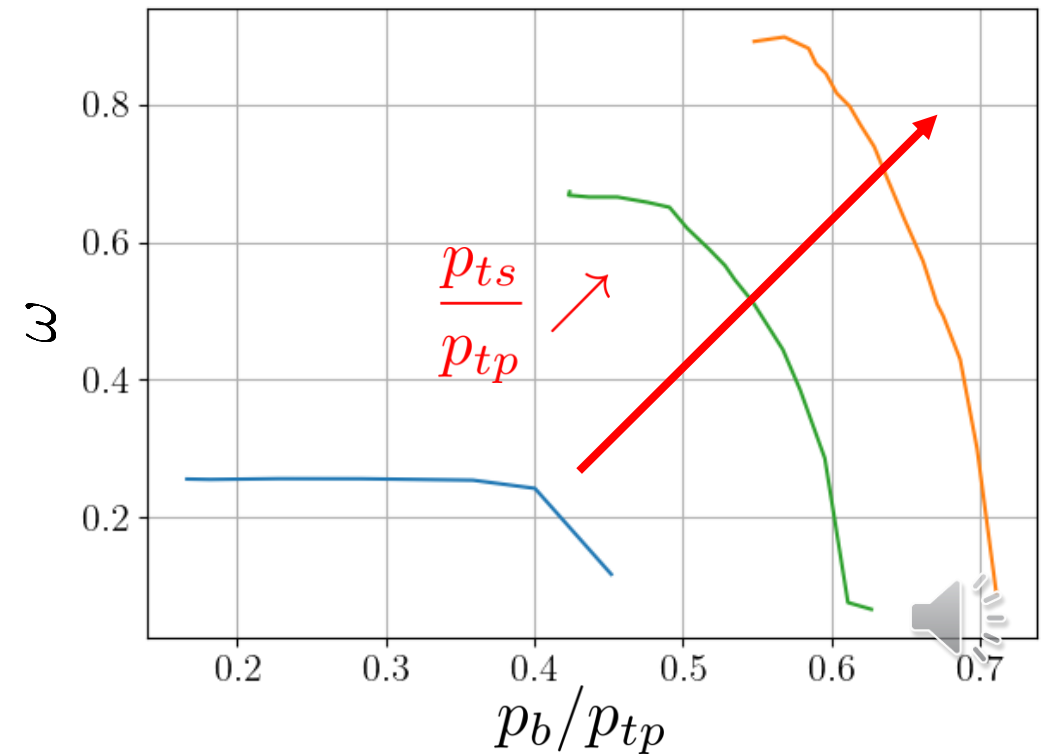
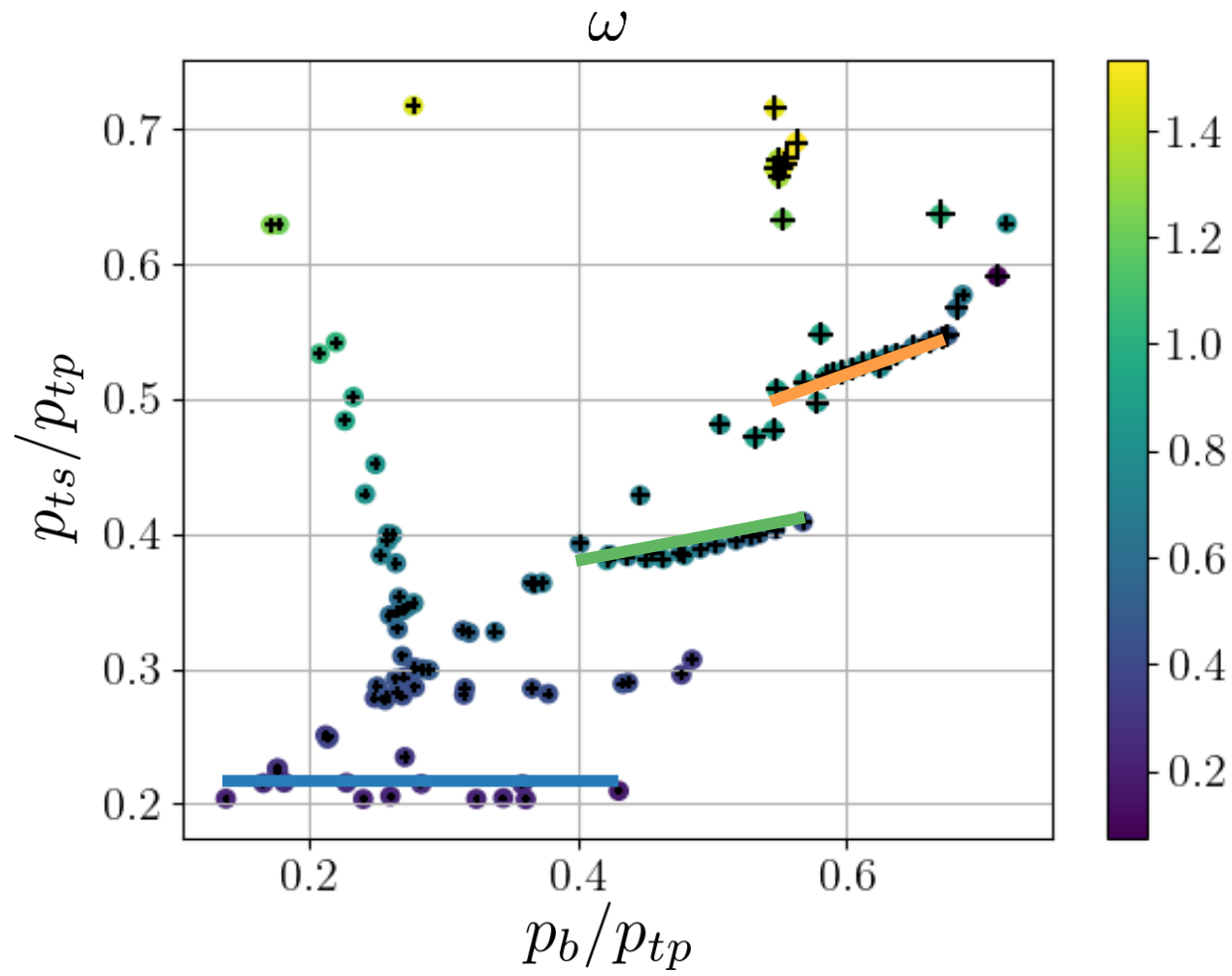
→ dimensionless:  $\hat{m} = \dot{m} / \dot{m}_{p,max}$



# Experimental results

$$\dot{m}_p, \dot{m}_s = f(p_{tp}, T_{tp}, p_{ts}, T_{ts}, p_b) \quad (1.5 \% \text{ uncertainty})$$

→ entrainment ratio:  $\omega = \dot{m}_s / \dot{m}_p$

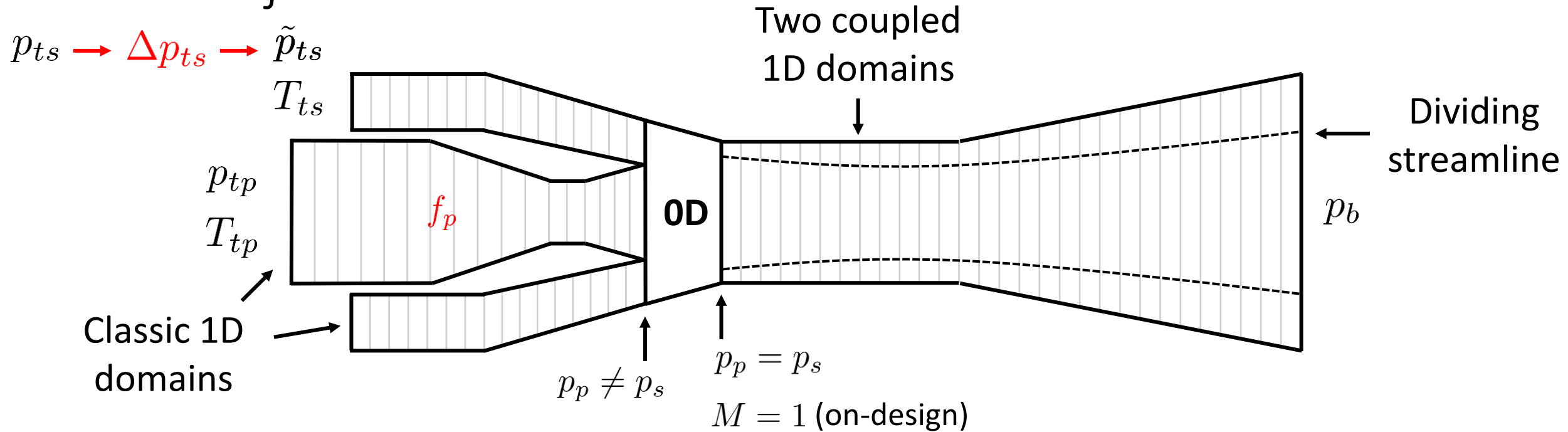


# Contents

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# A 1D ejector model



Euler equations in the primary nozzle:

$$\begin{cases} d_x(\rho_p A_p V_p) &= 0 \\ d_x(\rho_p A_p V_p^2) &= -A_p d_x p_p - \frac{1}{2} f_p \rho_p V_p^2 l_w \\ d_x(\rho_p A_p V_p h_{t,p}) &= 0 \end{cases}$$

All remaining losses are lumped in a single pressure loss at the inlet:

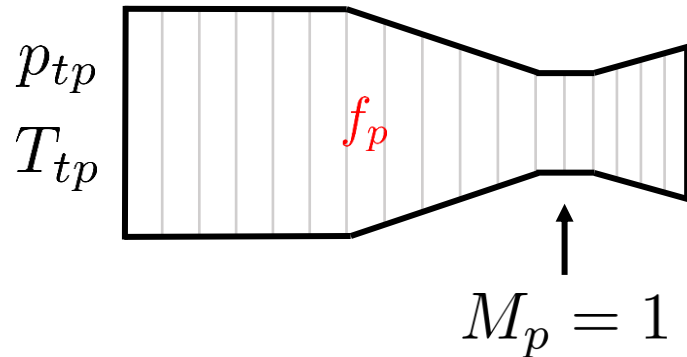
$$\Delta p_{ts} = p_{ts} - \tilde{p}_{ts}$$

How do the losses change with the operating conditions?

# Calibration procedure

## Primary friction coefficient

Nozzle always choked (normal operation)

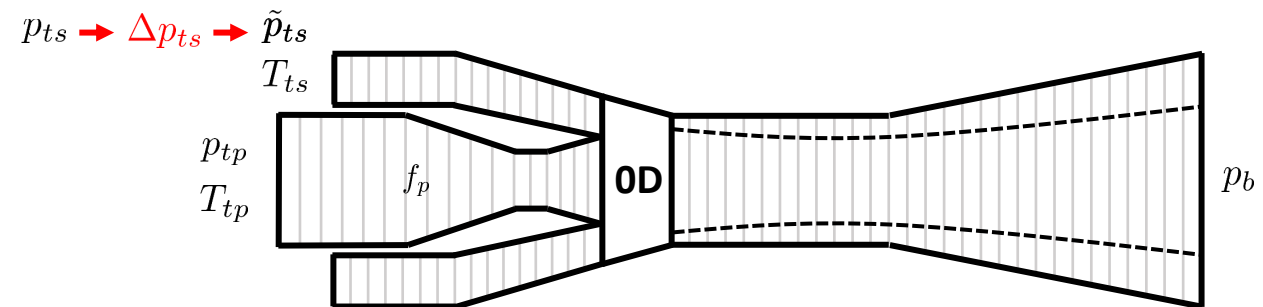


1. Isolate the nozzle
2. Calibrate  $f_p$  to minimize the error on  $\dot{m}_p$  on the **complete** dataset:

$$J(f_p) = \sum_i \left( \dot{m}_{p,i} - \tilde{\dot{m}}_{p,i} \right)^2$$

## Secondary pressure loss

Goal: link the pressure loss to the conditions

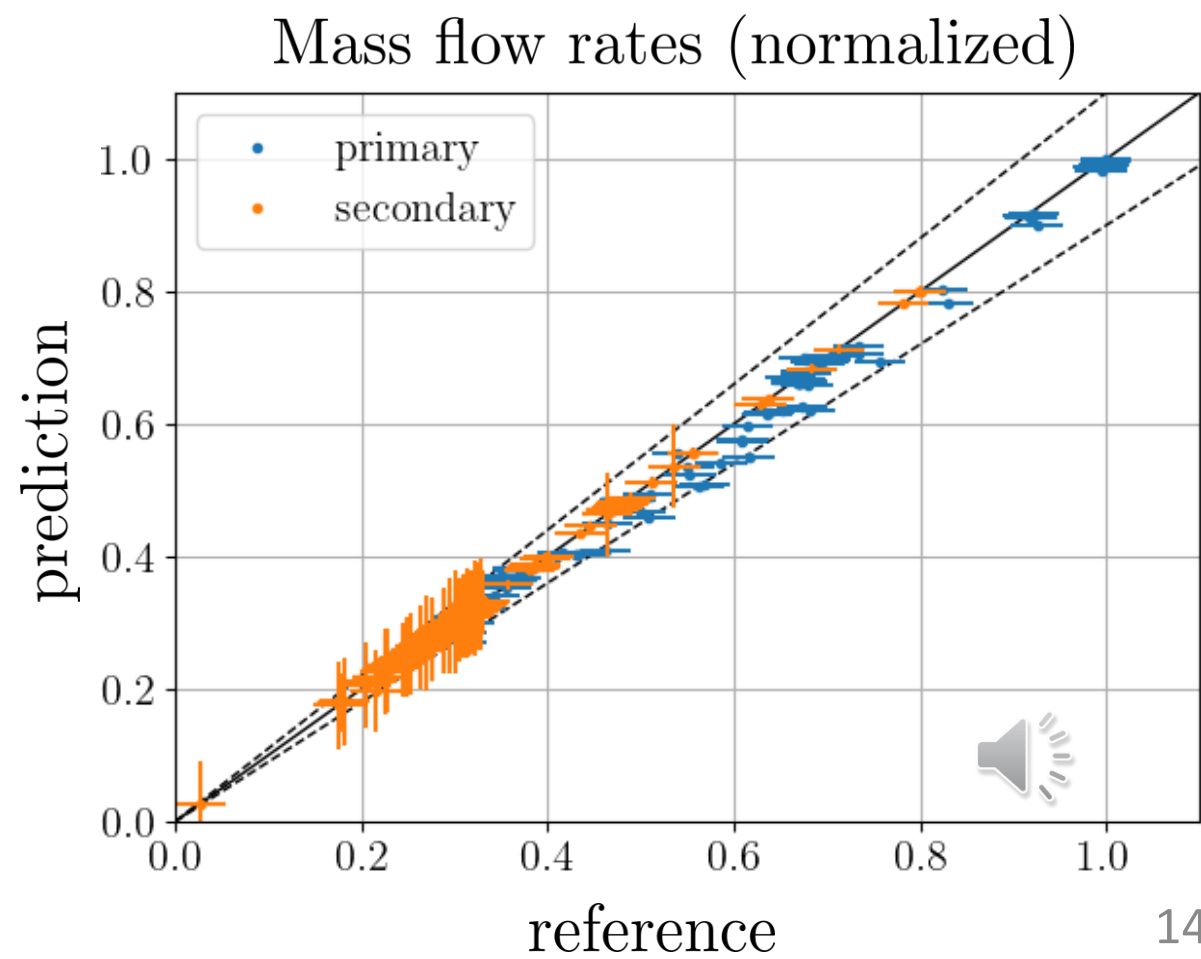
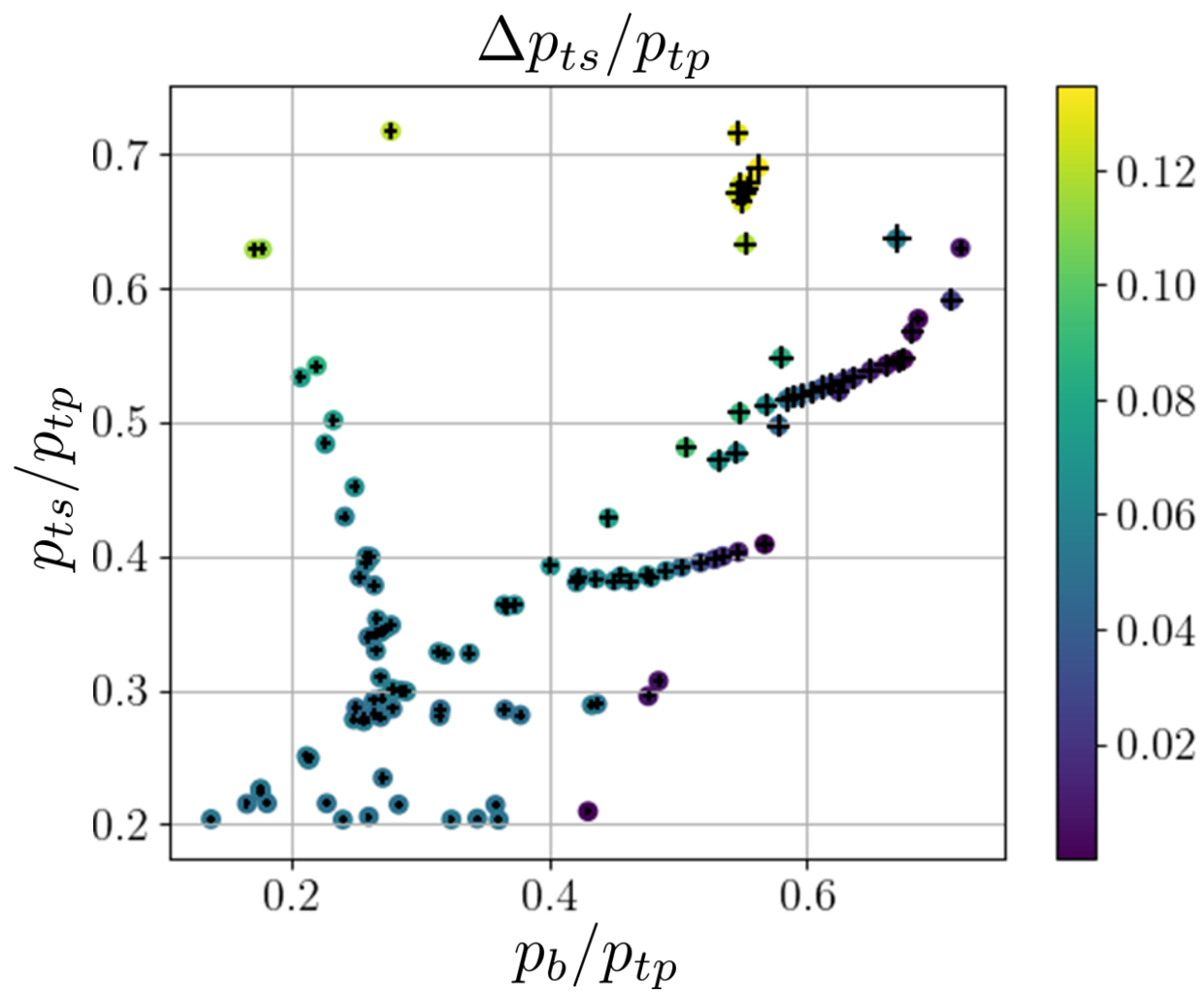


1. Use the calibrated  $f_p$
2. Calibrate  $\Delta p_{ts}$  to minimize the error on  $\dot{m}_s$  **point by point**:

$$J(\Delta p_{ts,i}) = \left( \dot{m}_{s,i} - \tilde{\dot{m}}_{s,i} \right)^2$$

# Calibration results

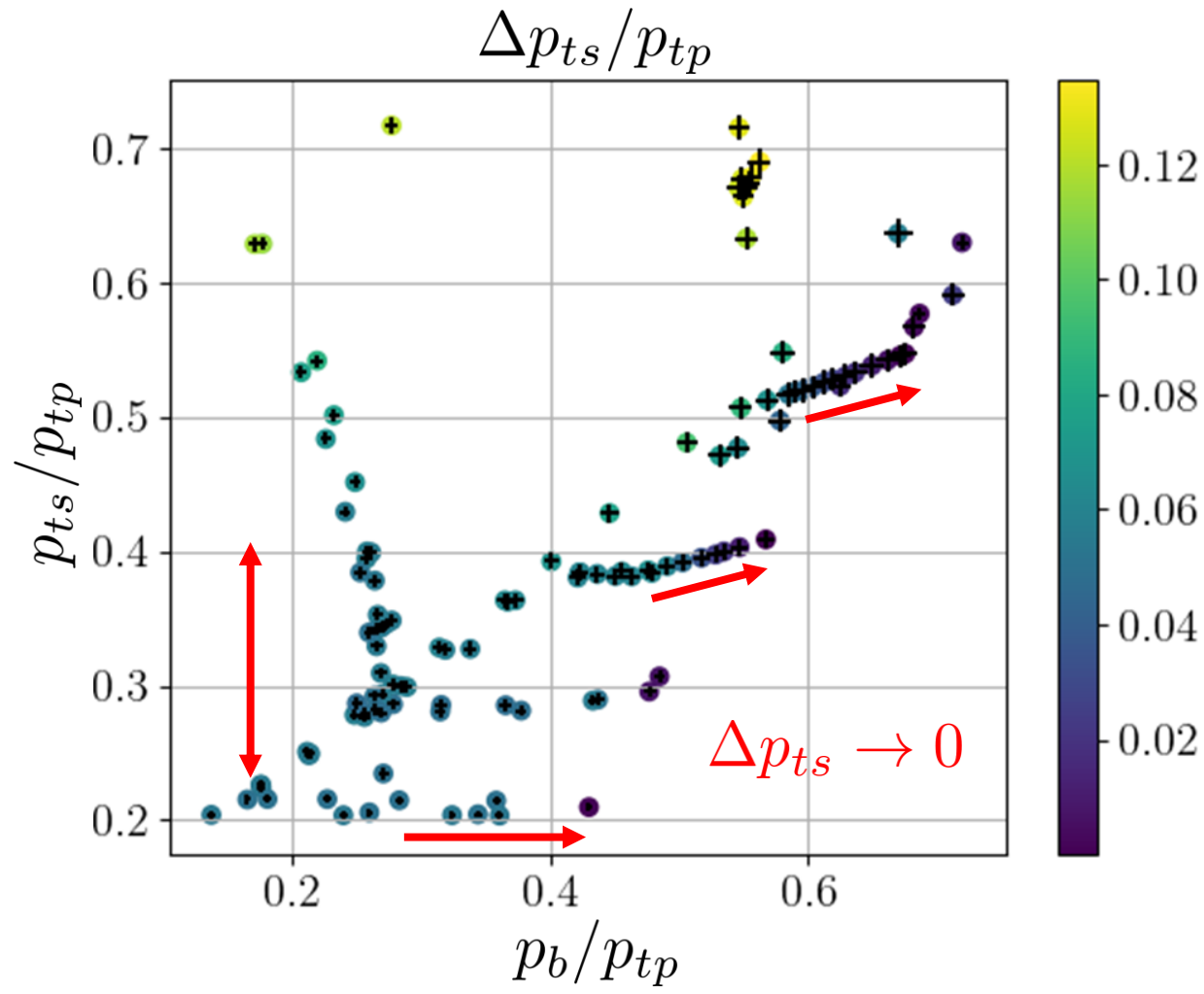
$$f_p = 0.0017$$





# Calibration results

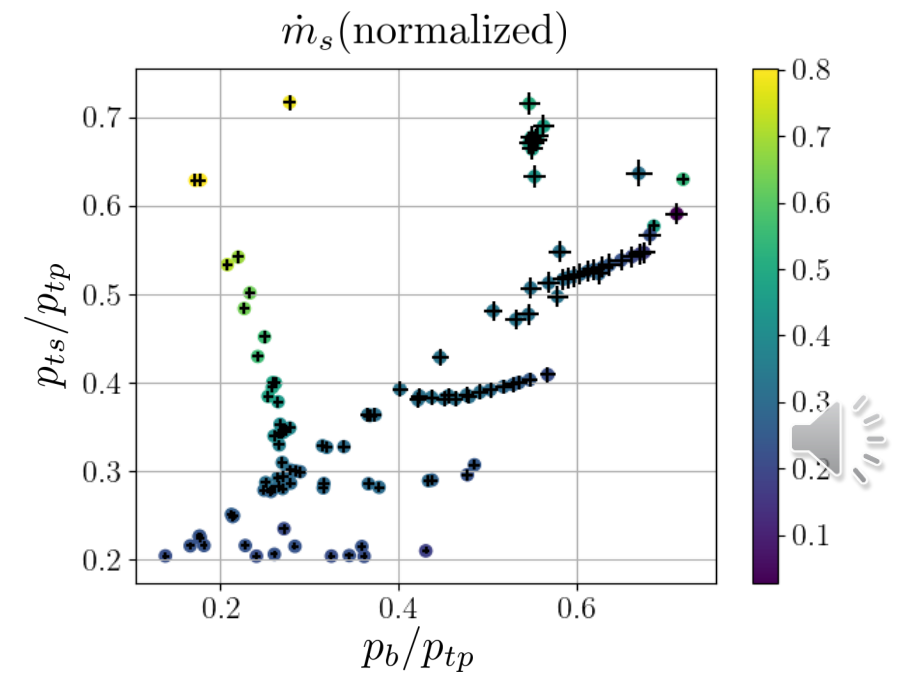
$$f_p = 0.0017$$



**Primary friction coefficient:** reasonable

**Secondary pressure loss:**

- Most sensitive to the back pressure
- Less sensitive to inlet pressure ratio
- Correlates with the secondary mass flow rate



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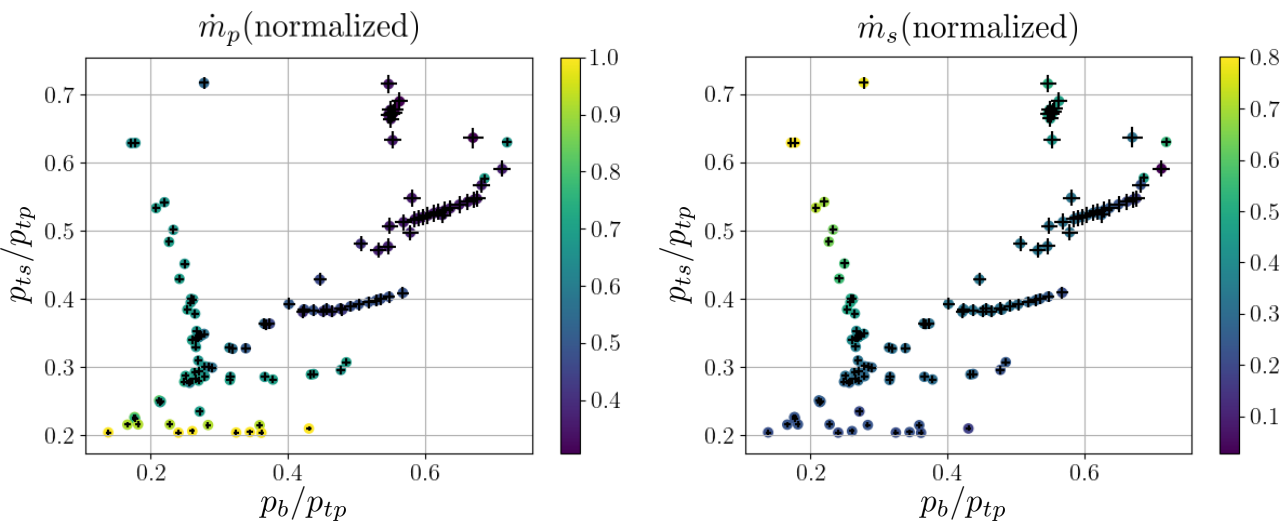
# Conclusion



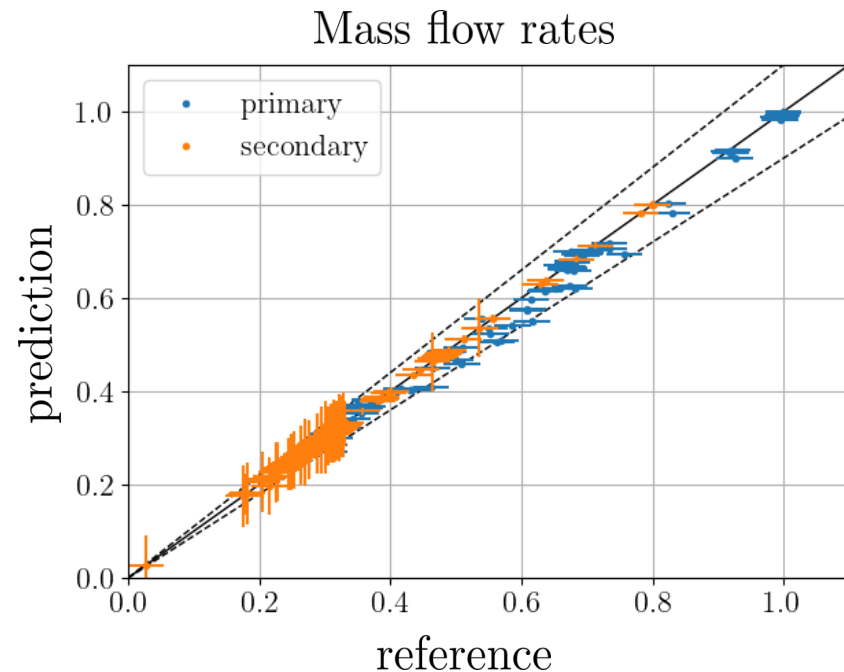
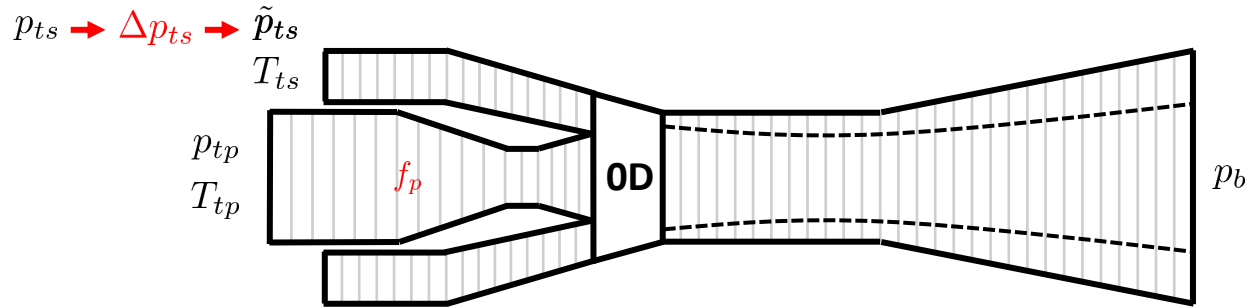
- Experimental campaign at aeronautical scale in various conditions



Obtain local data from pressure taps



# Conclusion



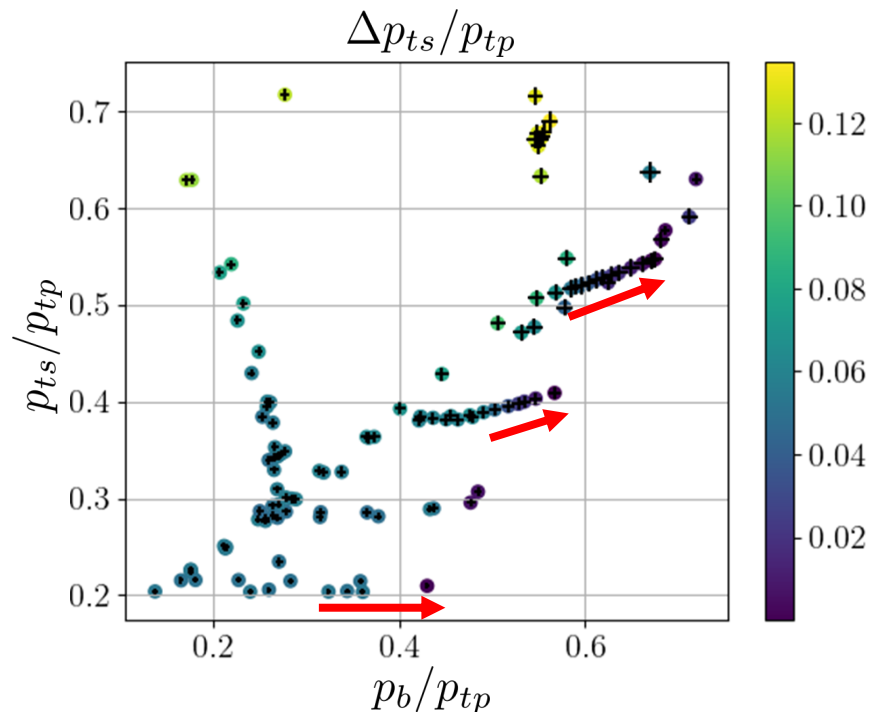
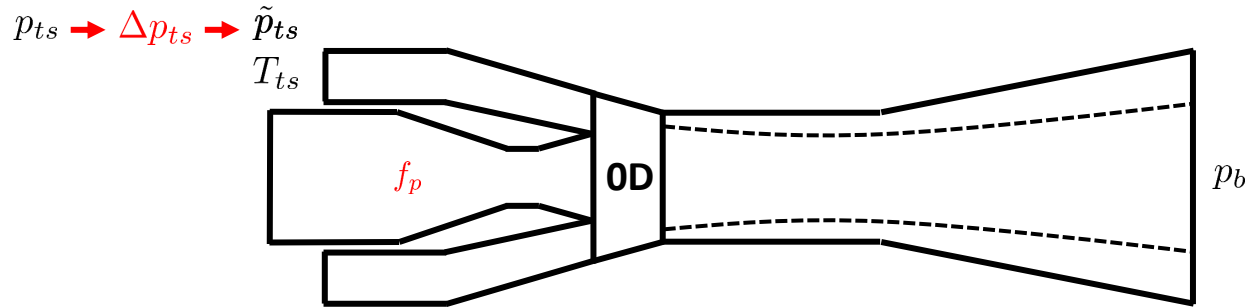
- Experimental campaign at aeronautical scale in various conditions

 Obtain local data from pressure taps

- Calibration of a 1D model, accuracy of 10 %



# Conclusion



- Experimental campaign at aeronautical scale in various conditions



Obtain local data from pressure taps

- Calibration of a 1D model, accuracy of 10 %
- The loss coefficient is most sensitive to the back pressure
- The loss coefficient correlates to the secondary mass flow rate



Localize losses, calibrate the shear force

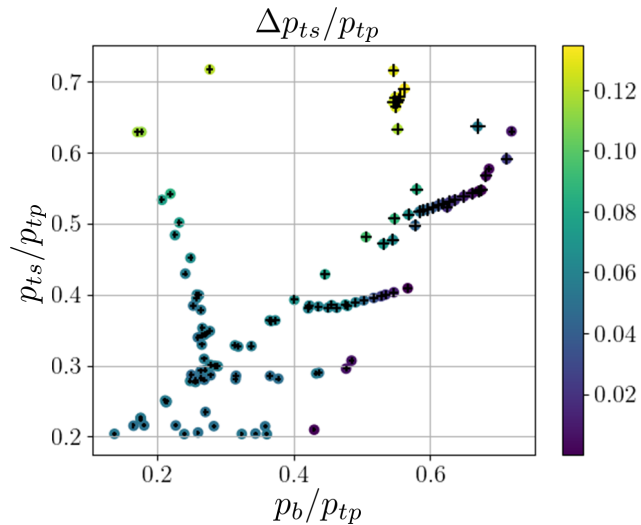


Link the closure to the state variables

# Ongoing work: regressing the closure coefficients with physics-constrained machine learning

## Physics-separated

1. Calibrate “manually”:  $\Delta \tilde{p}_{ts}$



2. Regress a function a posteriori

$$\Delta p_{ts} = g(p_b/p_{tp}, \dots; \mathbf{w})$$

$$J(\mathbf{w}) = \sum_i (\Delta p_{ts,i} - \Delta \tilde{p}_{ts,i})^2$$

## Physics-integrated

Calibrate the weights directly through the model:

$$J(\mathbf{w}) = \sum_i (\dot{m}_{s,i} - \tilde{\dot{m}}_{s,i})^2$$

The physical model acts as a constraint on the optimization

$$\frac{dJ}{d\mathbf{w}} = 2 \sum_i (\dot{m}_{s,i} - \tilde{\dot{m}}_{s,i}) \frac{d\dot{m}_{s,i}}{d\Delta p_{ts}} \frac{d\Delta p_{ts}}{d\mathbf{w}}$$

Calculating the sensitivity of the model can be avoided with **the adjoint method**



# References

1. K. Banasiak and A. Hafner. “1d computational model of a two-phase r744 ejector for expansion work recovery”, International Journal of Thermal Sciences, 50(11): 2235–2247, 2011.
2. J. Van den Berghe, B. R. Dias, Y. Bartosiewicz, M. A. Mendez. “A 1D model for the unsteady gas dynamics of ejectors”, Energy 267, 2023.





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# Uncertainty on the pressure ratios

Absolute uncertainty on the Validyne sensors (all pressures):  $\delta p = 1375 \text{ Pa}$

$$\Pi_1 = \frac{p_b}{p_{tp}}$$

$$\delta \Pi_1 = \sqrt{\left(\frac{\partial \Pi_1}{\partial p_b}\right)^2 \delta p^2 + \left(\frac{\partial \Pi_1}{\partial p_{tp}}\right)^2 \delta p^2} = \delta p \sqrt{\underbrace{\left(\frac{\partial \Pi_1}{\partial p_b}\right)^2}_{\frac{1}{p_{tp}^2}} + \underbrace{\left(\frac{\partial \Pi_1}{\partial p_{tp}}\right)^2}_{\frac{-p_b^2}{p_{tp}^2}}}$$

$$\delta \Pi_1 = \delta p \sqrt{\frac{1}{p_{tp}^2} \left[1 + \left(\frac{p_b}{p_{tp}}\right)^2\right]} = \frac{\delta p}{p_{tp}} \sqrt{1 + \Pi_1^2}$$

$O\left(\frac{1375}{5 \cdot 10^5} \sqrt{1 + 0.2^2}\right) = O(0.3\%)$

$O\left(\frac{1375}{1 \cdot 10^5} \sqrt{1 + 1^2}\right) = O(2\%)$