

How can power-to-ammonia be robust?

Optimization of an ammonia synthesis plant powered by a wind turbine considering operational uncertainties.

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Abstract

The increasing share of wind energy induces a strain on the electricity network. To unburden the transmission system operators from this strain, the dispensable wind energy can locally be stored in an energy carrier, e.g. ammonia (NH_3). Existing work considers fixed operational parameters during design optimization to represent real-life conditions of the Power-to- NH_3 system. However, uncertainties significantly affect real-life performances, which can lead to suboptimal plants. To provide a robust design—least sensitive to uncertainties—we considered the main operational uncertainties during design optimization and illustrated the contribution of each uncertainty on the systems NH_3 production. This work presents the optimization under uncertainty of the Power-to- NH_3 process and a global sensitivity analysis

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on the optimized designs. The results revealed a design trade-off, where a *productive* design produces 3.2 times more NH_3 on average, but is 2.6 times less robust (higher standard deviation) than the *robust* design. A global sensitivity analysis on the most robust design showed that the temperature fluctuation of the NH_3 reactor dominates the average NH_3 production by 99.7%. The same sensitivity analysis on the most productive design showed that the wind speed measurement error and the temperature variation are both influencing the ammonia production by respectively 75.4% and 22.5%. Accordingly, an accurate anemometer and improving the temperature control over the NH_3 reactor are the most effective actions to make the most productive design more robust. However, a robust plant can be obtained by decreasing the load size of the plant. It suffices to improve the temperature control over the NH_3 reactor to make this design (adopted from the trade-off) less sensitive to the noise. Future investigations involve analyzing the dynamic operations of the robust Power-to- NH_3 pathway and analyze the impact of uncertainties on its levelized cost.

Keywords: Power-to-ammonia, Robust design optimization, Haber-Bosch synthesis, Seasonal hydrogen storage, Energy storage system

1. Introduction

The erratic nature of renewable sources requires a higher degree of flexibility of the electricity grid [1]. To avoid this requirement, an energy storage system is necessary to regulate the supply of this non-dispatchable energy, removing its intermittent effect on the grid. The primary purpose of the storage system is to capture the excess energy at any time and inject it back

7 into the network to compensate for variability between supply and demand
8 without relying on fossil fuels while improving the security of electricity sup-
9 ply in a sustainable way [2, 3]. For significant power levels, the production
10 of chemicals can be employed to store the energy in an electrochemical en-
11 ergy carrier. This energy carrier could subsequently fuel a power production
12 system for power generation; balancing the electricity network for prolonged
13 power disruptions and reducing the need for a flexible grid [4].

14 The hydrogen-based Power-to-Power (PtP) concept enables the storage
15 of large-scale (up to GW) power via water electrolysis, but realizing it in
16 practice is proven difficult. Still, the declining cost in renewable technolo-
17 gies promoted the creation of numerous research and demonstration projects
18 across Europe [5–8]. However, storing pure H_2 in a compressed or cryogenic
19 (below $-253^\circ C$) container for several months provides low PtP efficiencies
20 (between 34% and 38%) and includes higher storage costs [9]. Besides, the
21 storage of this substance introduces safety issues due to its invisible, odorless
22 and flavorless properties, making it hard to detect leaks and increases the
23 risk of explosion [10, 11].

24 A more viable and safer way for the implementation of this hydrogen-
25 based energy storage system is by converting the electrolytic H_2 to ammonia
26 (NH_3), using the industrially mature Haber-Bosch Synthesis (HBS) process
27 [12]. The HBS process consists of synthesizing a mixture of H_2 and nitrogen
28 gas (N_2) to form NH_3 in the presence of a catalyst at an operational temper-
29 ature between $350^\circ C$ and $550^\circ C$ and a pressure ranging from 150 bar to 250
30 bar [13–15].

31 NH_3 gained a significant role during recent years in the application of

32 large-scale H_2 storage, but also for its potential utilization as a maritime fuel
 33 and sustainable nitrogen-based fertilizer [16–20]. Morgan et al. [13] devel-
 34 oped an analytic model to determine in which circumstances this Power-to-
 35 Ammonia (PtA) concept can be economically viable in addition to a diesel-
 36 fueled generator for a geographic islanded case. A more extensive analysis by
 37 Bañares-Alcántara et al. investigated the potential use of NH_3 -based energy
 38 storage in electric islanded cases [14]. Later on, the Institute for Sustainable
 39 Process Technology (ISPT) presented a feasibility study for implementing
 40 this renewable NH_3 concept of storing the abundance of wind energy for
 41 local farming and power generation in the Netherlands by considering eco-
 42 nomic and industrial competitive scenarios [9]. The studies of Sánchez et al.
 43 [21, 22] investigated the optimal scaling of each subprocess (differentiating
 44 between air separation units and ammonia synthesis reactors), providing a
 45 relation between NH_3 production and investment cost linked to the renew-
 46 able energy supply mix to the PtA plant. The studies carried out by Allman
 47 et al. [23], Beerbühl et al. [24] and Palys et al. [25] incorporated the capacity
 48 sizing and energy scheduling of the PtA plant, while considering the vari-
 49 ability of solar and wind energy into the design optimization. Pilot plants of
 50 such an ammonia-based energy storage system are built in two locations in
 51 the world, namely at the Rutherford Appleton Laboratory (RAL) in the UK
 52 and the Fukushima Renewable Energy Institute - AIST (FREA) in Japan.
 53 The goal of the PtA plant at RAL is improving the plants’ commercial possi-
 54 bilities for providing a market-flexible energy carrier [18], while the research
 55 objective of the demonstration plant at FREA is to enhance the HBS process
 56 with the development of new Ruthenium catalysts, which enables the NH_3

57 synthesis at a low-pressure and low-temperature environment [26]. The pres-
58 ence of uncertainties is however observed by Reese et al. on the operations
59 of a small-scale ammonia synthesis pilot plant located in Minnesota in the
60 form of temperature and pressure fluctuations in the reactor [17]. Although
61 each study included a sensitivity analysis of the electrolyzer’s operation and
62 the HBS process, no investigation has been done on the identification and
63 quantification of operational uncertainties influencing the performance of the
64 entire storage system.

65 This paper provides the modeling of the NH_3 -based energy storage to-
66 gether with the identification of reported operational uncertainties from lit-
67 erature, which was combined to perform a design optimization under un-
68 certainty. We performed the modeling of an electrolyzer operating with an
69 alkaline electrolyte, a Pressure Swing Adsorption (PSA) to obtain nitrogen
70 from the air, and a Haber-Bosch Synthesis (HBS) plant to synthesize NH_3
71 in Aspen Plus. In addition to the chemical modeling in Aspen Plus, a Wind
72 Turbine Generator (WTG) is created in Python to convert wind speed into
73 electric power. These models were assembled and optimized with a Multi-
74 Objective Genetic Algorithm (MOGA) to establish a set of optimized designs.
75 This energy model was then combined with the identified operational uncer-
76 tainties of each subsystem to establish an optimization under uncertainty by
77 the use of an Uncertainty Quantification (UQ) algorithm. With the MOGA
78 and UQ approach, a set of optimized designs was determined, which were
79 least sensitive to the effect of these uncertainties while maximizing the NH_3
80 production. This so-called Robust Design Optimization (RDO) approach
81 improves the design of the plant in the presence of parametric uncertainties.

82 The RDO process consisted of combining the Nondominated Sorting Genetic
 83 Algorithm (NSGA-II) [27] and the Polynomial Chaos Expansion (PCE) tech-
 84 nique [28], which ultimately evolved the defined decision variables towards a
 85 better performance while taking into account the implemented uncertainties.

86 **2. Modeling the storage of wind energy through ammonia synthesis**

87 This section presents the design of each process necessary to store wind
 88 energy in the energy carrier NH_3 . The first subsection provides the wind
 89 speed data used to power the storage system. This power is determined by the
 90 model of a wind turbine in Python. Each following subsection presents the
 91 modeling of an Alkaline Water Electrolyzer (AWE), a PSA and the HBS in
 92 Aspen Plus. The description and integration of the operational uncertainties
 93 are included for the wind turbine model, the AWE and the HBS at each
 94 corresponding subsection.

95 *2.1. Wind power generation*

96 We incorporated the hourly wind speed measurement data of a wind
 97 turbine park located in Galicia (Spain) and sequentially sorted the data in
 98 a wind speed frequency distribution with a step size of 1 m/s [29]. Through
 99 the integration of a power curve of a typical wind turbine model, this wind
 100 speed data is converted into electric power. We based this power curve on the
 101 design of the Vestas V112 onshore wind turbine and integrated this curve in
 102 Python through Equation 1 to calculate the generated wind power (P_{WTG}):

$$P_{\text{WTG}} = \frac{1}{2} \rho A C_P v^3 \quad [\text{W}], \quad (1)$$

where ρ is the density of air in kg/m^3 (at sea level and at 15°C , $\rho = 1.22$ kg/m^3), A is the area of the rotating blades in m^2 , C_P is the power coefficient and v is the wind speed in m/s .

In the adopted model, the maximum power output was adjusted to 3 MW at a rated wind speed of 11 m/s while assuming a constant power coefficient of 37%. We performed this adaptation to correlate the wind speed and electric power between the cut-in and rated wind speed with the cubic relationship (Equation 1) without considering the dependency of C_p on the wind speed. The original and adopted design specification are provided in Table 1.

Table 1: Wind turbine generator design specifications, constraints and wind speed measurement uncertainty.

Design specification		Reported value [30]	Adopted value
C_P	[W/W]	$C_P(v)$	37.0
A	[m^2]	9852.0	9852.0
Constraints			
$v_{\text{cut-in}}$	[m/s]	3	3
v_{rated}	[m/s]	12	11
$v_{\text{cut-out}}$	[m/s]	25	25
Uncertainty		Integrated value [31]	
$e_{\text{measurement}}$	[-]	$\pm 1\%$	

Wind turbines are inherently influenced by a variety of uncertainties, providing ambiguous prospects for start-up wind turbine parks. These uncertainties have a direct effect on the profitability of these projects, which are mainly based on wind speed measurements or estimations to forecast the

116 capacity factor [32] or the Annual Energy Production (AEP) of a location
 117 [33]. Lackner et al. categorized a variety of uncertainties influencing this
 118 AEP in four categories, which consists of: wind speed measurement uncer-
 119 tainty, historical wind speed data, wind resource modeling variability, and
 120 lastly, the site assessment uncertainty [33]. Because the wind speed measure-
 121 ments for one year are used in this design optimization study (not the power
 122 production of an actual wind turbine), only the first category of Lackner et
 123 al. (the wind speed measurement error) is applied to the design of the WTG
 124 and considered in the UQ analysis. Kaganov et al. designated the wind speed
 125 measurement error of rotational measurement devices between 1% and 6%
 126 [31]. We integrated a wind speed measurement uncertainty of 1% to consider
 127 the most accurate wind speed measurement in the wind turbine design. A
 128 Gaussian distribution characterizes this uncertainty in the UQ analysis be-
 129 cause the real distribution of the wind speed measurement error is unknown
 130 in this context [33]. The UQ analysis assesses the uncertainty propagation
 131 for each design on the considered objective. The following expression enables
 132 the implementation of this uncertainty (Equation 2):

$$v_{\text{measurement}} = v_{\text{data}}(1 - e_{\text{measurement}}) \quad [\text{m/s}], \quad (2)$$

133 where $v_{\text{measurement}}$ is the measured wind speed in m/s resulting from the input
 134 wind data (v_{data}) and the error of the device ($e_{\text{measurement}}$) in %. During the
 135 robust design optimization process, the measured wind speed ($v_{\text{measurement}}$)
 136 replaces the wind speed (v) in Equation 1.

137 2.2. Alkaline water electrolyzer

138 An Alkaline Water Electrolyzer (AWE) was selected because of its proven
 139 reliability in industrial applications and a multitude of commercially avail-
 140 able technologies on the market, allowing the AWE to operate commercially
 141 at MW scale [15, 34, 35]. The AWE process was modeled in Aspen Plus for
 142 one electrolytic cell (Figure 1). To resemble the real operation of an AWE
 143 and determine the hydrogen production when applying electric power to the
 144 electrolyzer stack, the electrolyzer model of Ulleberg [36] is integrated with
 145 a FORTRAN calculator in the ‘Electrolytic cell’ block (Figure 1). Ullebergs
 146 electrolyzer model consists of two empirical equations: a voltage-current (U -
 147 I) relationship and the characterization of the Faraday efficiency (η_F).

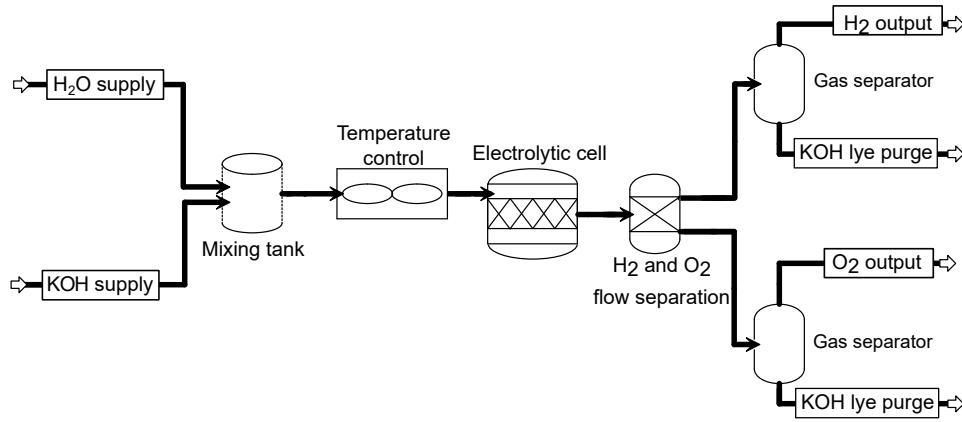


Figure 1: In the Aspen model of the electrolyzer, KOH lye dissolves in a tank with water, where its exothermic reaction increases the temperature of the mixture and is controlled by a heat exchanger before entering the electrolytic cell. The block components of one electrolytic cell and the product separation creates the H_2 and O_2 flows. The gas separation blocks separate the H_2 gas and KOH mixture.

148 The applied voltage U on the electrolytic cell is determined by the re-

versible voltage U_{rev} of the electrolytic reaction, the current I flowing through the electrolytic cell and T the operational temperature of the electrolytic cell. This relationship is defined with the following expression [36]:

$$U_{\text{real}} = U_{\text{rev}} + (r_1 + r_2 T) \frac{I}{A} + (s_1 + s_2 T + s_3 T^2) \log \left((t_1 + t_2/T + t_3/T^2) \frac{I}{A} + 1 \right) \quad [\text{V}], \quad (3)$$

where r_i are the parameters related to the ohmic resistance of the electrolyte (for $i = 1, 2$), s_i and t_i are the coefficients for overvoltage on the electrodes (for $i = 1, 2, 3$) and A the surface area of the electrodes in m^2 . Ulleberg determined the value of these parameters (r_i , s_i and t_i) by a non-linear regression deterministic process (see Table A.5) [36].

Faraday's law determines the amount of hydrogen produced by the electrolyzer. This law states that the molar flow rate of the produced hydrogen ($\dot{n}_{\text{H}_2}$) depends on the total number of electrolytic cells N and the transfer rate of electrons (Equation 4) [36]:

$$\dot{n}_{\text{H}_2} = \eta_{\text{F}} \frac{NI}{zF} \quad [\text{mol/s}], \quad (4)$$

where η_{F} is the Faraday efficiency of the electrolytic reaction. This Faraday efficiency expresses the ratio of the flow rate of hydrogen that is produced by the alkaline electrolyzer, over the theoretical production rate. This ratio is expressed by the second empirical formula with Equation 5 [36]:

$$\eta_{\text{F}} = f_1 \exp \left(\frac{f_2 + f_3 T}{I/A} + \frac{f_4 + f_5 T}{(I/A)^2} \right) \quad [-], \quad (5)$$

where f_i (for $i = 1, \dots, 5$) are the parameters defining the evolution of the

166 Faraday efficiency, determined by the same non-linear regression process used
167 in Equation 3 at an operational pressure of 7 bar (Table A.5) [36].

168 Mori et al. studied the steady-state operations of an alkaline electrolyzer,
169 where a sinusoidal behavior of the cell temperature is observed. This tem-
170 perature varied with a range of $\pm 3^\circ\text{C}$ from the desired temperature [37].
171 The study acknowledged that the heat exchanger controlling the tempera-
172 ture causes this variation in temperature. When implementing this variation
173 in the temperature control block of the AWE Aspen Plus model, the Faraday
174 efficiency (Equation 5) and cell current (through the U - I relationship defined
175 with Equation 3) are affected by this uncertainty, resulting in a variance of
176 hydrogen production (Equation 4). This operational uncertainty is treated as
177 a measurement error, affecting the control of the electrolytic cell temperature,
178 which is included during the global sensitivity analysis and the robust design
179 optimization within this study. Like the wind speed measurement error, the
180 nature of the temperature measurement distribution is unknown, for which a
181 Gaussian distribution is applied to the model. The UQ analysis assesses the
182 effect of the variation of the cell temperature for each GA-generated design
183 on the investigated output.

184 2.3. Pressure swing adsorption

185 The Pressure Swing Adsorption (PSA) process is selected to obtain ni-
186 trogen from the air. Frattini et al. proposed a simplified model of the PSA
187 process in Aspen Plus, where the design incorporates a single-stage compres-
188 sor, to pressurize the airflow (consisting of 75.5 wt% N_2), and a separation
189 block, to obtain nitrogen [15]. The same philosophy has been used in Morgan
190 et al. for a mathematical model of a wind-powered ammonia plant in steady-

191 state operations [13]. The nitrogen production depended in both cases on
 192 the delivered power to the PSA compressor, which can be expressed with
 193 the following relationship between the power P_{PSA} and the air mass flow rate
 194 $\dot{m}_{\text{air}}$ [13]:

$$P_{\text{PSA}} = \frac{\dot{m}_{\text{air}}}{\eta_{is}\eta_{\text{mech}}} \left(\frac{k}{k-1} \right) T_{\text{in}} R \left[\left[\frac{p_{\text{out}}}{p_{\text{in}}} \right]^{\frac{(k-1)}{k}} - 1 \right] \quad [\text{W}], \quad (6)$$

195 where η_{is} is the isentropic efficiency ($\eta_{is} = 0.75$ [13]), η_{mech} the mechanical
 196 efficiency ($\eta_{\text{mech}} = 0.95$ [13]), T_{in} the inlet temperature in K, R the gas
 197 constant of air in J/kgK, k the heat capacity ratio ($k = 1.4$), p_{out} the outlet
 198 pressure in bar ($p_{\text{out}} = 7$ bar), and p_{in} the inlet pressure in bar ($p_{\text{in}} = 1$
 199 bar). The mass flow of air ($\dot{m}_{\text{air}}$) is split into a pure mass flow of nitrogen
 200 and a residual flow of O_2 and Ar by a separation block in Aspen Plus. The
 201 compressor and separator block in Aspen Plus uses the PENG-ROB property
 202 method, which is based on the Peng-Robinson cubic equation of state [15].

203 2.4. Haber-Bosch synthesis process

204 An ammonia synthesis design is adopted from the paper of Frattini et
 205 al. to replicate the Haber-Bosch Synthesis (HBS) process performance [15].
 206 In the first stage of modeling the ammonia process, the block specifications
 207 provided by the paper are implemented in Aspen Plus (Figure 2) [15]. In
 208 the subsequent step, we simplified the Haber-Bosch synthesis loop to reduce
 209 the computational cost while creating a single link between the generated
 210 wind power and the performance of the HBS process. This model reduction
 211 enabled us to govern the process by a single control parameter. To reach this
 212 necessary simplification, several adaptations were applied to the HBS loop of

213 Frattini et al. [15]. Frattini et al. initially integrated pressure losses through
 214 the use of the tube-and-shell designs in the integrated heat exchangers ((3)
 215 and (5) in Figure 2) [15]. These pressure losses were discarded from the
 216 model. Hence, the reactor compressor (6), which compensated for these
 217 pressure losses, could be excluded from the model. The model reduction
 218 resulted in the exclusion of the power consumption for this compressor. A
 219 second modification on the adopted model is the removal of the conditioning
 220 block (1), where water particles from the air or the electrolyzer are cleansed
 221 from the flow entering the synthesis loop (Figure 2). Because of the absence
 222 of water in both flows, we excluded this condition block from the model.
 223 We considered as well pure hydrogen and nitrogen flow rates from the AWE
 224 and PSA processes to avoid dealing with the catalyst poisoning caused by
 225 the presence of oxygen in both streams, which is a well-reported problem
 226 for iron-based catalysts [38]. In industrial processes, a purity of 99.9999% is
 227 required with the help of an additional purification system to overcome the
 228 deactivation of the ammonia synthesis catalyst [38].

229 These modifications resulted in the use of a single control parameter,
 230 namely the direct control over the operational pressure within the synthesis
 231 loop through the loop compressor ((2) in Figure 2). This loop compressor is
 232 sequentially governed by the power supply to this component, as is expressed
 233 with Equation 7 for a three-stage compressor.

$$P_{\text{HBS}} = \frac{\dot{m}_{\text{mix}}}{\eta_{\text{is}}\eta_{\text{mech}}} \sum_{i=0}^2 \left(\left(\frac{k}{k-1} \right) T_i R \left[\left[\frac{p_{i+1}}{p_i} \right]^{\frac{(k-1)}{k}} - 1 \right] \right) \quad [\text{W}] \quad (7)$$

234 In this expression, P_{HBS} presents the delivered power to Haber-Bosch

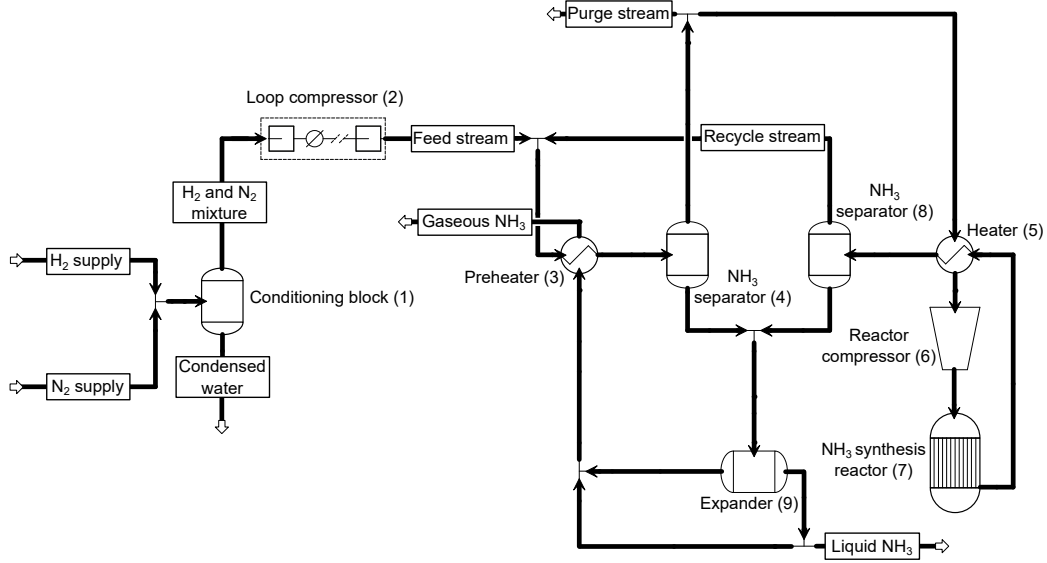


Figure 2: Frattini et al. modeled the Haber-Bosch Synthesis (HBS) loop in Aspen [15]. In this HBS, the loop compressor (2) pressurizes a mixture of H_2 and N_2 , where the NH_3 synthesis reactor (7) converts this mixture to NH_3 . The ammonia is extracted from the loop through condensation ((4), (8) and (9)).

235 compressor in W, $\dot{m}_{\text{mix}}$ the mass flow of gas mixture in kg/s, η_{is} isentropic
 236 efficiency, η_{mech} the mechanical efficiency, $T_{\text{in},i}$ inlet temperature of stage i in
 237 K (for $i = 0$ to 2), R the gas constant of mixture in J/kgK, k the heat capacity
 238 ratio, $p_{\text{in},i}$ the inlet pressure in kPa at stage i in kPa (for $i = 0$ to 2) and $p_{\text{out},i+1}$
 239 the outlet pressure in kPa at stage i in kPa (for $i = 0$ to 2). Frattini et al.
 240 provided the decision variables of the loop compressor, which is modeled with
 241 an MCompr block in Aspen Plus based on the isentropic compressor model
 242 [15]. We compared the HBS power consumption of this simplified process
 243 to the described ammonia synthesis loop in the study of Morgan, where this
 244 study reported that 5.49% of the total power consumption of an ammonia
 245 plant goes to the ammonia synthesis loop [39]. In comparison with our

246 modeled HBS loop, we observed that the loop compressor consumes 4.44%
247 of the total power provided to the ammonia plant. This similar result proves
248 that the applied simplifications are in agreement with another reported PtA
249 energy model.

250 Operational uncertainties and instability phenomena in the ammonia syn-
251 thesis process are described in the literature [17, 40]; therefore, disturbances
252 are inherently present in this part of the energy storage model. The paper
253 of Reese et al. acknowledged the presence of uncertainties in practice for a
254 wind-powered ammonia synthesis plant [17]. Although the plant integrated
255 a control system to govern the operations, the measurements of a three-day
256 operation of this plant showed temperature and pressure fluctuations during
257 the steady-state process. The paper interpreted this variability due to the
258 undamped nitrogen supply of the PSA system and the occasional absence of
259 hydrogen coming from the electrolysis process. However, these reported tem-
260 perature fluctuations are essentially present during the operations and reach
261 up to 50°C [17] without proper identification or analysis of disturbance. The
262 mathematical model of an ammonia synthesis reactor and a heat exchanger
263 of Jinasena et al. also showed temperature oscillations of this process where a
264 temperature fluctuation of 10°C is present [40]. We included the same reactor
265 temperature fluctuation of $\pm 10^\circ\text{C}$ with a Gaussian distribution within the
266 proposed energy storage model. The cause of this variability is linked to the
267 temperature measurement noise affecting the heat exchanger at the reactor
268 inlet. For this reason, we chose the Gaussian distribution to represent this
269 noise. This uncertainty is introduced into the operational temperature of the
270 reactor (7) of the Aspen Plus model. Although pressure fluctuations were

also reported in [17], these variations manifested due to erratic flow supply of hydrogen and nitrogen towards the synthesis process, where the origins of the temperature variations were unsubstantiated.

3. Optimization methodology

In this section, the optimization objectives are defined and discussed. The following two subsections designate the design search space and constraints to locate the global optimum within the model constraints. The final part of this section describes the applied MOGA to find these global optimum and the chosen UQ analysis, which collectively create the RDO approach. This approach is deemed necessary to maximize the performance of the plant while minimizing the sensitivity of the noise factors on this performance, i.e. robustifying the PtA process.

3.1. Optimization objective

The optimization objectives of this paper were chosen in function of the considered approach (deterministic or robust design optimization). In the Deterministic Design Optimization (DDO) process, the search algorithm maximizes the storage of wind energy while conceiving a design able to continuously operate, i.e. maximizing the plants' load factor, which provides a higher energy efficiency and ultimately achieve a better economic return on investment [41]. This load factor (L_F), chosen as the second objective, is expressed by the ratio of average consumed power over time (P_{average}) and the plants maximum consumed power ($P_{\text{plant,max}}$) and formulated with Equation 8:

$$L_F = \frac{\sum_{i=1}^t P_{\text{plant}}(i)}{P_{\text{plant,max}}t} = \frac{P_{\text{average}}}{P_{\text{plant,max}}} \quad [-], \quad (8)$$

where P_{plant} is the power consumed by the total plant at a certain time in W and t the time in hours.

In the robust design optimization, the robustification of the ammonia production is opted as the final objective to make it less sensitive to the noise propagation incorporated in the subsystems. We focused on this objective to provide a design that can capture the highest amount of wind energy and store it through the production of the studied energy vector while being less influenced by operational uncertainties. This objective is split into two parts, where the average ammonia production needs to be maximized and, secondly, the sensitivity on the ammonia production is minimized. The ratio of the standards deviation (σ) over its average value (μ) of the concerned output characterizes this sensitivity, which is defined in literature as the Coefficient of Variance (CoV). This CoV is expressed in Equation 9 when applied on the ammonia production:

$$\text{CoV} = \frac{\sigma_{\text{NH}_3}}{\mu_{\text{NH}_3}} \quad [-]. \quad (9)$$

3.2. Design search space

The optimization method enhances the energy storage model according to a sorted wind speed data set (the design parameter) while finding the best performing plant design corresponding to the chosen objectives. This best performing design can be reached by searching the optimized set of decision variables within the defined search space. For attaining this optimized set,

specific decision variables were selected to optimize the flow of power to each subsystem (AWE, PSA and HBS) according to the wind speed occurrence of the location in Galicia (Spain).

To control the amount of energy captured and converted by the ammonia plant, the simulation disposes of a part of the generated wind power by means of peak shaving; taking the total plant power size as the first decision variable ($\%_{\text{plantsize}}$ in Figure 3). This captured power is then subdivided into three fractions, where a proportion of power is supplied to the AWE ($\%_{\text{AlkalineWaterElectrolyzer}}$), another part to the PSA ($\%_{\text{PressureSwingAdsorption}}$ and the residual power to the Haber-Bosch compressor to pressurize the ammonia synthesis process (Figure 3). To define the necessary decision variables and attain an optimized configuration, each subsystem generates hydrogen, nitrogen and ammonia at an individual flow rate. The power sizing of the AWE and PSA are therefore considered as the two successive decision variables, while the power supplied to the HBS compressor is employed as a control parameter (Figure 3). However, a single electrolytic cell can consume a maximum power of 2.1 kW [36], so the stack sizing of the electrolyzer has to be taken into account to predict the required installed capacity for a specific design. The number of electrolyzers (N) is therefore selected as the fourth and final decision variable. The candidates generated by the optimization algorithm for this decision variables have continuous values during the design optimization, allowing the GA to determine the electrolyzer capacity sizing (through the evaluation of the electrolyzer cells in series). In the discussion of the results (Section 4), these decision variable values were rounded up to the nearest integer, which provided a slightly higher annual ammonia production

339 comparing when rounding this decision variable down (absolute difference of
 340 0.01 tonne NH_3). For the load factor (L_F), these results were not altered by
 341 this design choice.

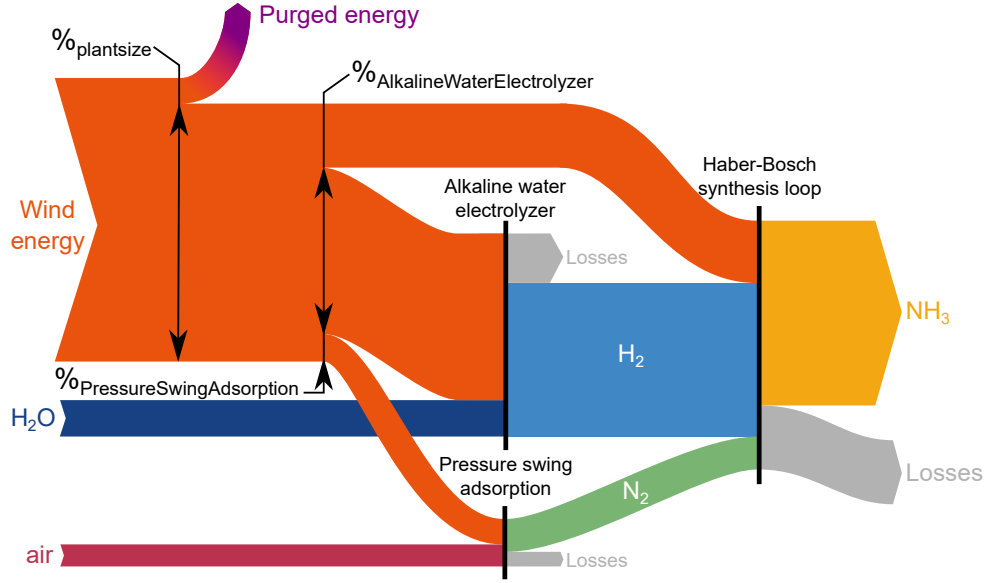


Figure 3: The wind turbine transforms the wind speed into electric power, which powers, according to a certain ratio, the electrolyzer, the air separation and the Haber-Bosch process. These processes produce H_2 , N_2 and, finally, NH_3 , respectively. The power ratio towards the individual processes, the plant load size and the numbers of electrolyzers are decision variables.

342 The design search space bounds each decision variable by a minimum
 343 and maximum value, so an optimized set of decision variables can be located
 344 (Table 2). For the plant sizing ($\%_{\text{plantsize}}$), the proportion of power flowing
 345 to the total ammonia plant can range between 0.001% and 100% according
 346 to the 3 MW power capacity of the WTG. This range allows the algorithm
 347 to decide which quantity of wind power can be captured by the NH_3 plant.
 348 The boundaries of the power proportion of the AWE and PSA ($\%_{\text{AWE}}$ and

349 %_{PSA}) are selected based on a sensitivity analysis of the Aspen Plus model.
 350 The analysis shows that the proportion of power to the AWE varies between
 351 91% and 95% at optimal/stoichiometric conditions (HBS loop pressure of 250
 352 bar and a H₂/N₂ ratio of 3 mol/mol). For the PSA, this parameter varies
 353 between 0.9% and 1.6%. We chose a range from 1 to 2600 electrolytic cells to
 354 assure the ability of the AWE to perform at an operational power of 3 MW.

Table 2: Ranges of the decision variables (power allocation to the main and subprocesses, number of electrolyzer cells) chosen by the NSGA-II algorithm, where each design is assessed if none of the three model constraints are violated (Haber-Bosch loop pressure, H₂/N₂ ratio and current density for one electrolytic cell).

Decision variables		Range		Model constraints		Range	
		min	max			min	max
% _{plantsize}	[%]	0.001	100	I/A	[mA/cm ²]	f(η_{thermal})	300
N	[-]	1	2600	p _{HBS}	[bar]	100	250
% _{AWE}	[%]	91	95	H ₂ /N ₂	[-]	1.5	4.5
% _{PSA}	[%]	0.9	1.6				

355 3.3. Constraints

356 Based on the declared restraints by the manufacturer of the alkaline elec-
 357 trolyzer and safety regulations of the ammonia synthesis loop, we constrained
 358 three output parameters of the total energy storage model (Table 2). These
 359 three parameters are the current density of the electrolytic cell, the H₂/N₂
 360 ratio entering the HBS compressor and its outlet pressure.

361 Each electrolytic cell is bounded by a maximum current density of 300
 362 mA/cm² [36]. The minimum current density depends on the thermal effi-

363 ciency (η_{thermal}) which is expressed by Equation 10:

$$\eta_{\text{thermal}} = \frac{U_{\text{tn}}}{U_{\text{real}}} \quad [-] \quad (10)$$

364 where U_{tn} is the thermoneutral voltage in V [36].

365 When the thermal efficiency of the electrolytic cell is higher than 100%,
 366 the system requires heat to operate. Because the AWE is a low-temperature
 367 electrolyzer, the cell is unable to operate at this point; leading to the elimi-
 368 nation of these decision variables from the set of solutions (Figure 4).

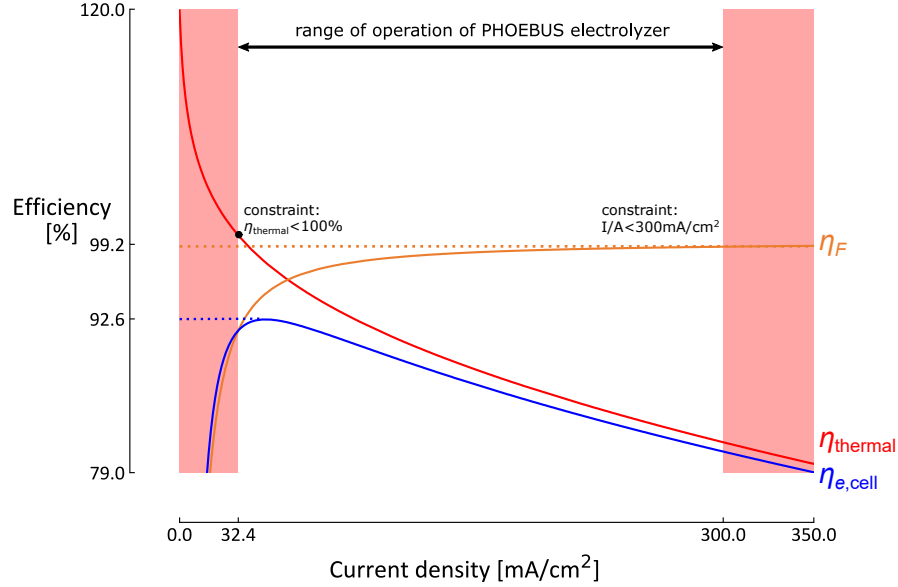


Figure 4: Thermal (η_{thermal}), Faraday (η_F) and energy ($\eta_{e,\text{cell}} = \eta_{\text{thermal}}\eta_F$) efficiency of the alkaline electrolyzer in function of the current density at a temperature of 80°C. A peak in the energy efficiency indicates the most optimal point of operation for the electrolyzer to produce H_2 . The operational range of the electrolyzer is bounded by a minimum and maximum current density.

369 The flow towards the Haber-Bosch compressor should consist of a H_2/N_2

ratio between 2 and 3 [39, 42] while the operating pressure lies between 100 and 250 bar [43] (Figure 5). When either of the three parameters of the model exceeds a limit, the to be maximized objectives are penalized with a numerical value of 10^{-9} and the minimized outputs (the CoV in the RDO phase) with 10^9 . Assigning these numerical values drives the genetic algorithm away from the generated design points and uses the more potent sets of decision variables to evolve towards the best results.

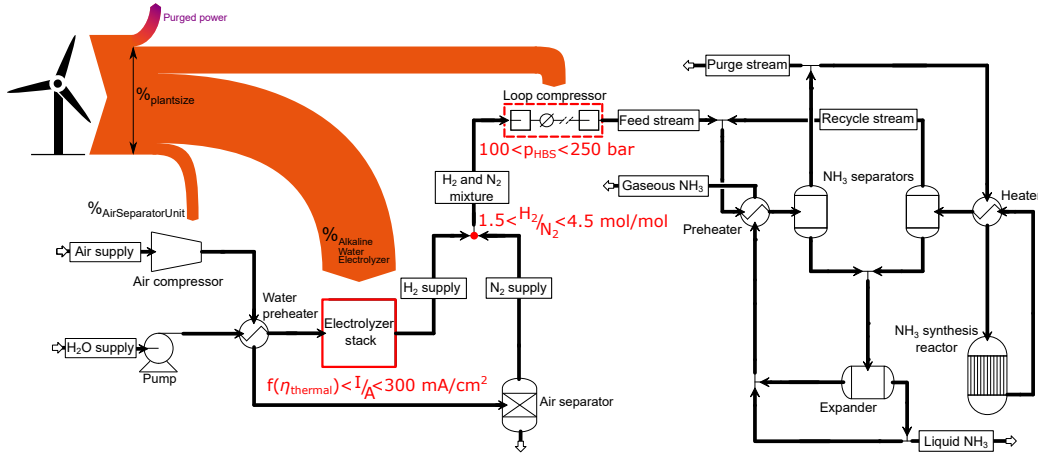


Figure 5: After the optimization algorithm defines the decision variables, a model simulation is executed, and a constraint check is performed to exclude the designs which exceeds one of the imposed constraints, i.e. minimum and maximum current density of the individual alkaline electrolytic cell, the H_2/N_2 ratio or the output pressure of the Haber-Bosch loop compressor.

3.4. Optimization algorithm

To determine the optimal set of design samples for the system model, we implemented the multi-objective Nondominated Sorting Genetic Algorithm (NSGA-II) [27]. First, the algorithm produces an initial set of design samples

381 (n samples) through Latin Hypercube Sampling [44]. Out of this initial de-
 382 sign sample set, the algorithm creates a second sample set based on crossover
 383 and mutation, with an equal number of samples n . After characterizing both
 384 sets of design samples, each design sample is implemented in the system
 385 model and evaluated, leading to $2n$ values for each objective. Thereafter,
 386 the samples are sorted based on their dominance on the objectives and the n
 387 samples with the highest dominance define the second generation of design
 388 samples. This iterative process is repeated until a predetermined number
 389 of generations is achieved or the simulation converged towards a solution.
 390 Depending on the relation between the multiple objectives, the optimal set
 391 of design samples can converge to a single optimal design sample (i.e. non-
 392 conflicting objectives) or a set of design samples (i.e. conflicting objectives).
 393 In such a set of optimal design samples, each sample dominates every other
 394 sample in at least one objective (i.e. Pareto frontier).

395 3.5. *Uncertainty quantification method*

396 To propagate the uncertainties of the input parameters through the sys-
 397 tem model, we implemented the Polynomial Chaos Expansion (PCE) algo-
 398 rithm [45, 46]. This technique provides a computationally efficient alterna-
 399 tive for the robust Monte Carlo Simulation technique for a small stochastic
 400 dimension (< 10). To quantify the mean and standard deviation of the ob-
 401 jective efficiently, the PCE algorithm creates a surrogate model $\hat{M}(\boldsymbol{\xi})$ of the
 402 physical model $M(\boldsymbol{\xi})$ based on multivariate orthogonal polynomials Ψ_i and
 403 corresponding coefficients u_i :

$$\hat{M}(\boldsymbol{\xi}) = \sum_{i=0}^P u_i \Psi_i(\boldsymbol{\xi}) \approx M(\boldsymbol{\xi}). \quad (11)$$

404 When P in Equation 11 is infinite, the surrogate model is an exact rep-
 405 resentation of the physical model. In practice, the series is truncated up to
 406 a value depending on the complexity of the input-output relation (related to
 407 the polynomial order p) and the stochastic dimension d [28]:

$$P + 1 = \frac{(p + d)!}{p!d!}. \quad (12)$$

408 When the PCE surrogate model is constructed, the mean μ and standard
 409 deviation σ follow analytically out of the coefficients:

$$\mu = u_0, \quad (13)$$

$$\sigma^2 = \sum_{i=1}^P u_i^2. \quad (14)$$

410 Next to the statistical moments of the objective, the contribution of each
 411 input parameter to the objective variation can be quantified through Sobol'
 412 indices. The first-order Sobol' indices (i.e. no input parameter interaction
 413 considered) are defined as:

$$S_i = \frac{D_i}{D} = \frac{\text{Var}[M(\xi_i)]}{\text{Var}[M(\boldsymbol{\xi})]}. \quad (15)$$

414 Similar to the mean and standard deviation, these first-order Sobol' in-
 415 dices can be quantified analytically via the PCE coefficients:

$$S_i^{PC} = \sum_{\alpha \in A_i} u_\alpha / D \quad A_i = \alpha \in A : \alpha_i = 0, \alpha_{j \neq i} = 0. \quad (16)$$

416 4. Results and discussion

417 This section presents the results and discussion of the DDO and RDO ap-
418 proaches, applied to the power-to-ammonia energy storage system. A global
419 sensitivity analysis applied to the DDO results shows the effect of the un-
420 certainties on the performance of two deterministic optimums. To minimize
421 the effect of the uncertainties on the performance, the RDO approach takes
422 them into account and find a design that can minimize their effects on these
423 results. Again, a global sensitivity analysis is performed on the most relevant
424 designs to show which uncertainties have the most impact on the robustified
425 designs. Finally, we proposed different measures to further reduce the effect
426 of these uncertainties on the RDO results.

427 4.1. Deterministic design optimization

428 The deterministic design optimization with a population (n) of 24 samples
429 resulted in a collection of optimized solutions when maximizing the annual
430 NH_3 production and the plants' load factor. The NSGA-II algorithm con-
431 verged to this set of solutions –or Pareto points– after 33 iterations due to
432 the conflicting objectives: maximizing $m_{\text{NH}_3, \text{total}}$ and L_F . This Pareto front
433 consists of two designs, each configured with two unique decision variables,
434 which enables the optimized performance for a particular objective (Table
435 3). These two extreme cases are named ‘Most NH_3 ’ and ‘Best L_F ’. Each
436 intermediate set of decision variables between those extremities provides a
437 combination of maximizing both output objectives with a certain weight.
438 The results of the UQ analysis on the two cases show the dominance of the
439 wind speed measurement and the ammonia reactor temperature (Figure 6).

Table 3: Set of decision variables and results of the two extremities of the Pareto front. An increase in the NH_3 plant size ($\%_{\text{plantsize}}$) increases the amount of electrolyzers (N) and the power distribution to the AWE ($\%_{\text{AWE}}$). This small increase in power distribution to the AWE relates to the non-linear behavior of the electrolyzer model.

Decision variable		Case	
		Most NH_3	Best L_F
$\%_{\text{plantsize}}$	[%]	92.4	6.58
N	[-]	2500	954
$\%_{\text{AWE}}$	[%]	91.8	91.6
$\%_{\text{PSA}}$	[%]	1.60	1.60
Result			
$m_{\text{NH}_3, \text{total}}$	[tonne]	491	122
L_F	[%]	22.4	73.5

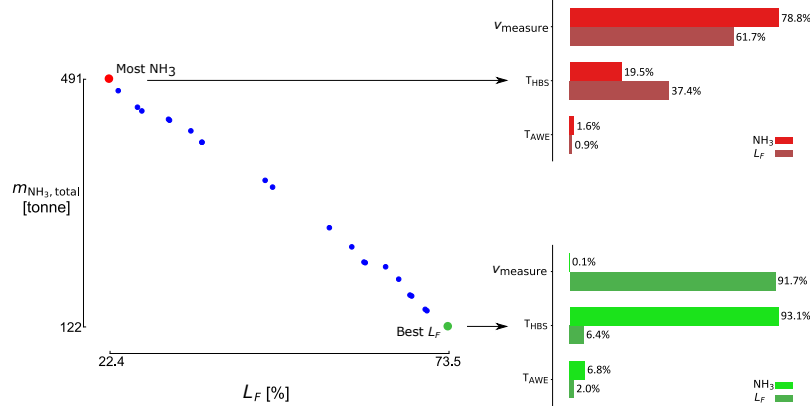


Figure 6: The DDO algorithm provided a design trade-off when maximizing the annual NH_3 production and the load factor (L_F). A global sensitivity analysis shows the dominance of the wind speed measurement influencing the load factor and the NH_3 production in the ‘Most NH_3 ’ design. In the best L_F design, the reactor temperature dominates the NH_3 production.

440 The ‘Most NH_3 ’ design enables the highest storage of available wind en-
 441 ergy to the energy carrier, ammonia. To obtain this most productive plant,
 442 a plant with a load of 2.77 MW (92.4% of the 3 MW WTG capacity) needs
 443 to be built, while it needs to be composed of an electrolyzer stack of 2500 in-
 444 dividual electrolytic cells. The number of alkaline electrolytic cells prevents
 445 the plant to capture the total wind turbine capacity of 3 MW. When the
 446 GA generates a larger plant size, and the same number of electrolyzers is
 447 incorporated, the plant would be unable to operate at lower wind power due
 448 to the minimum current density (Figure 4). This set of decision variables
 449 would result in lower annual ammonia production and therefore withdrawn
 450 from the set of optimal decision variables. The plant achieves a load factor of
 451 22.4%, which results in a low utilization rate of the total plant. However, for
 452 this design case, there is a potential to produce a large amount of ammonia
 453 that variates instantaneously with the wind speed. This would be an ideal
 454 way to capture the excessive power from the WTG. However, a commer-
 455 cial ammonia synthesis design is not adapted to this flexible functioning [9].
 456 The observed pressure variations are problematic, knowing that the ramp-up
 457 of the process is time-constrained (multiple hours to ramp-up the ammonia
 458 production) [23]. This could, although, be solved by accumulating hydrogen
 459 and nitrogen gas in storage tanks before the synthesis loop while supplying
 460 a constant mass flow of the mixture to the Haber-Bosch process. This makes
 461 the system less vulnerable to pressure changes if small fluctuations of power
 462 are guaranteed to this part of the plant.

463 For the design with the highest load factor ($L_F = 73.5\%$), the plant
 464 consumes 6.58% of the 3 MW WTG capacity (0.197 MW) while consisting

465 of 954 electrolytic cells. A sensitivity analysis of this design showed that
 466 the NSGA-II algorithm established a plant design with a stable ammonia
 467 production and an electrolyzer stack performing at the peak energy efficiency
 468 of 92.6% (Figure 4). This ‘Best L_F ’ design produces a steady low flow of
 469 ammonia, which is almost invulnerable to the variations of wind speed. This
 470 design type is the most common way to produce ammonia in combination
 471 with a grid connection to compensate for the absence of wind power [43],
 472 like the pilot plant in Minnesota [17]. Aside from the stable production, the
 473 amount of potential wind power discarded from the simulation (73.4% of the
 474 residual wind power) is unwanted when the principal use is equalizing the
 475 supply and demand of the electric grid. Complementary to the Haber-Bosch
 476 plant, the consumption of this residual excess energy, in this case, provides
 477 the necessity to install other flexible storage systems.

478 A global sensitivity analysis showed the effect of uncertainties applied
 479 to the two extreme cases, together with the corresponding Sobol’ indices
 480 (Figure 6). The UQ analysis provided a mean value for both objectives,
 481 which was lower than their deterministic counterparts due to the adverse
 482 effect of the uncertainties on the total performance. The analysis applied
 483 on the ‘Most NH_3 ’ design resulted in a relative decrease of 0.62% in the
 484 ammonia production ($\mu_{\text{NH}_3, \text{total}} = 488$ tonne NH_3) and a relative decrease in
 485 load factor by 6.63% ($\mu_{L_F} = 20.9\%$). The CoV of the NH_3 production and
 486 the load factor of the plant for the ‘Most NH_3 ’ case are respectively 1.57%
 487 and 7.46%. This result subsequently indicates that the load factor of this
 488 design is more affected by the variations of the uncertain parameters than
 489 the ammonia production. The UQ analysis of the ‘Best L_F ’ design presented

490 a relative decrease of 0.56% in NH_3 production and 0.03% for L_F between
 491 the mean and the deterministic result, where the CoV of both outcomes, in
 492 this case, are respectively 0.70% and 0.07%. These values show that the set
 493 of optimized decision variables for the best load factor design from the DDO
 494 analysis provides an ammonia plant that is insensitive to variations.

495 Regarding the Sobol' indices, the global sensitivity analysis shows the
 496 noise propagation due to the temperature variations in the NH_3 reactor and
 497 the electrolytic cell, and the wind speed measurement error in the two cases
 498 for each objective (Figure 6). The temperature variations in the electrolyzer
 499 have, in general, less effect on the overall variance of the objective (maximum
 500 6.8% of the total variance in the 'Best L_F ' design).

501 Different operational uncertainties influence the ammonia production in
 502 the two extreme cases (Figure 6). In the 'Most NH_3 ' case, the wind speed
 503 measurement error has a more significant effect on the noise propagation of
 504 the NH_3 production (78.8%) than in the 'Best L_F ' case (0.1%). The influence
 505 arises from the fact that the wind speed affects the generated power of the
 506 WTG, hence the consumed power by the ammonia plant. This correlation
 507 makes the design with the largest ammonia production capacity (consuming
 508 92.4% of the WTG maximum power) more dependable on the wind speed
 509 and its parameter variations. On the contrary, for the 'Best L_F ' case, this
 510 design is only using 6.58% of the WTG maximum power production, which
 511 results in a lower annual ammonia yield, but a higher resistance against wind
 512 speed measurement errors. However, the reactor temperature variations in
 513 this design dominate the ammonia production (93.1%), while this uncertainty
 514 influences the result in the other case with only 19.5% of the total variance.

515 This variation impacts the NH_3 production because of its effect on the equi-
516 librium conditions in the ammonia reactor; directly controlling the amount
517 of ammonia that is produced. The absence of the wind speed measurement
518 error results from the objective to attain a high load factor, which ensures
519 the continuous power flow to the plant; consequently minimizing the effect
520 of the wind speed variation on the NH_3 production. Because the influence of
521 the wind speed is absent in the ‘Best L_F ’ design, this temperature variation
522 will take over the dominant role of the most significant contribution to the
523 variation of the annual ammonia production.

524 In the case of the load factor, the global sensitivity analysis shows that the
525 wind speed variation has the most considerable contributions in both cases.
526 This equivalent influence emerges with the definition of the load factor as
527 the second optimization objective (Equation 8).

528 4.2. Robust design optimization

529 In the interest to find a design that enables the storage of wind power by
530 the production of ammonia while minimizing the impact of the uncertainties
531 on this production, a Robust Design Optimization (RDO) was performed on
532 the model. Combining the NSGA-II algorithm and the PCE method pro-
533 vides a strategy to inexpensively measure the sensitivity of the outcome –or
534 CoV– and progress towards a better set of decision variables, acquired by
535 the GA with a population size (n) of 24 samples in each iteration [46–48].
536 This approach optimized the wind-powered ammonia synthesis model to de-
537 termine a design that maximizes the mean NH_3 production while minimizing
538 the CoV of this production.

539 Similar to the DDO results, the RDO algorithm converged after 25 itera-

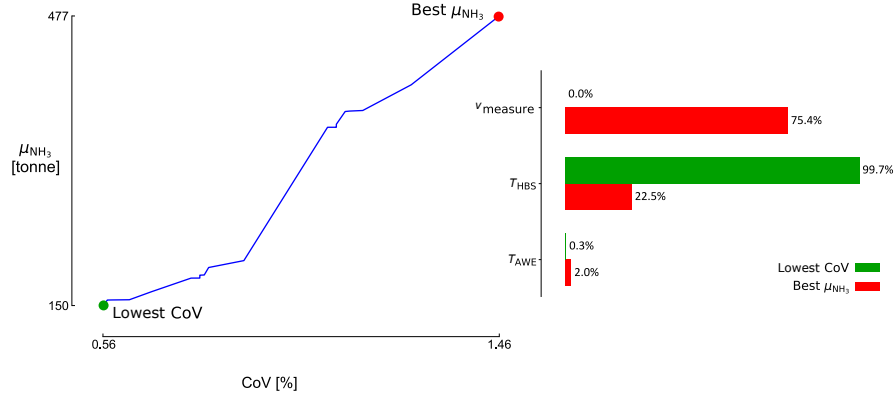


Figure 7: The RDO algorithm provided a design trade-off when maximizing the average NH_3 production and minimizing the Coefficient of Variance (CoV). In the ‘Best CoV’ case, the temperature variation dominates this average NH_3 production, while the wind speed variations dominate this production for the ‘Best μ_{NH_3} ’ design.

540 tions to a trade-off between the two chosen objectives, where two extremities
 541 each secure a unique set of decision variables to reach a specific objective (Fig-
 542 ure 7). In the most robust case (‘Lowest CoV’), the energy storage system
 543 produces on average low quantities of ammonia (150 tonne of NH_3 annually),
 544 but consists of a CoV which is 2.6 times lower than the conflicting optimized
 545 design. This conflicting case (‘Best μ_{NH_3} ’) delivers a 3.18 times higher mean
 546 production (477 tonne of NH_3 on average) than the ‘Lowest CoV’ design.
 547 These two opposing designs have a key decision variable that determines
 548 this difference in production, namely the fraction of power allowed from the
 549 3 MW wind turbine (i.e. the power plant size). This crucial decision variable
 550 creates this trade-off of robustification (Table 4). In comparison with the
 551 obtained DDO decision variables (Table 3), the RDO decision variables have
 552 a similar design configuration with the ‘Most NH_3 ’ case of the DDO process.
 553 This shows that the exploration and exploitation of the Latin Hypercube

554 and NSGA-II algorithm reach the same results for the same objective in
555 the different optimization cases. The Gaussian uncertainties cause different
556 ammonia productions.

Table 4: Set of decision variables (number of electrolyzer cells, power allocation to the main and subprocesses) generated by the NSGA-II algorithm and results of the two extremities (‘Best μ_{NH_3} ’ and ‘Lowest CoV’) from the Pareto front established by the RDO process. The NH_3 plant size ($\%_{\text{plantsize}}$) is the key decision variable for composing a robust ammonia plant.

Decision variable		Case	
		Best μ_{NH_3}	Lowest CoV
$\%_{\text{plantsize}}$	[%]	85.7	11.4
N	[-]	2490	2339
$\%_{\text{AWE}}$	[%]	91.9	92.5
$\%_{\text{PSA}}$	[%]	1.59	1.23
Result			
μ_{NH_3}	[tonne]	477	150
CoV	[%]	1.46	0.56

557 A global sensitivity analysis of the NH_3 production applied on the two ex-
558 treme trade-off designs resulted in the individual variance of each operational
559 uncertainty presented through the Sobol’ indices (Figure 7). According to
560 these Sobol’ indices, a different operational uncertainty influences the ammo-
561 nia production of the two designs. In the ‘Lowest CoV’ (most robust) design
562 case, the temperature variations of the ammonia reactor dominate these re-
563 sults. This influence was also observed in the DDO results with the ‘Best
564 L_F ’ design, where the effect of the wind speed measurement error was (al-

565 most) nullified by changing the size of the ammonia plant (decision variable
 566 $\%_{\text{plantsize}}$). This results that the residual two uncertainties (T_{HBS} and T_{AWE})
 567 influence the average ammonia production. The temperature of the ammo-
 568 nia reactor has a direct effect on the ammonia production, which accounts
 569 for having the most significant impact on the sensitivity of the ammonia
 570 production (Figure 7). If the objective is to create a robust ammonia plant,
 571 the temperature variations of the reactor need to be smaller. Jinasena et al.
 572 already provided examples on how to stabilize temperature fluctuations by
 573 increasing the monitoring measurements of the heat exchanger that controls
 574 the incoming flow. These measurements consisted of analyzing the composi-
 575 tion of feed gases, feed flow rate, reactor inlet temperature and the pressure
 576 along the reactor [40]. In the other case ('Best μ_{NH_3} '), a plant design is ob-
 577 tained with a CoV of 1.46% and an annual mean ammonia production of 477
 578 tonne which is mostly influenced by the wind speed measurement error and
 579 (in smaller quantities) the temperature of the HBS reactor. Like in the 'Most
 580 NH_3 ' case of the DDO, this influence is directly linked to the sizing of the am-
 581 monia plant, where a large plant is subjected to wind speed fluctuations and
 582 therefore to the wind speed measurement errors. This relationship gives rise
 583 to a plant with high annual average ammonia production, but more sensitive
 584 to the wind speed measurement error than the robust design. The impact of
 585 the accuracy of the wind speed can be reduced by implementing a more ac-
 586 curate wind speed measurement device and a better calibration/positioning
 587 of the anemometer. As in the deterministic optimization, the temperature
 588 variations of the AWE have little effect on the performance of the ammonia
 589 plant, although 91.9% of the consumed power goes to the alkaline electrolyzer

590 for the production of H_2 .

591 5. Conclusion

592 This paper provided the steady-state modeling and optimization of an
593 NH_3 -based energy storage system in Aspen Plus based on the expected wind
594 power production from a designed WTG in Python. The integrated WTG
595 powered the AWE, PSA and HBS compressor in a certain ratio, so the stor-
596 age of wind energy through ammonia production could be optimized by the
597 applied multi-objective optimization approach, i.e. the NSGA-II algorithm.
598 Adjacent to the modeling of these subsystems, we identified and integrated
599 the wind speed measurement error, the temperature variation of the elec-
600 trolyzer and the NH_3 synthesis reactor as the operational uncertainties. The
601 PCE algorithm measured the uncertainty propagation of these operational
602 uncertainties when analyzing a certain objective. The multi-objective DDO
603 consisted of maximizing the ammonia production and the plants' load fac-
604 tor with the NSGA-II algorithm. In the RDO step, the optimization and
605 robustification of this ammonia production was requested from the NSGA-II
606 algorithm in combination with the PCE method.

607 The DDO step provided a Pareto front where its outer ends delivered
608 a productive and high load factor design. The power sizing of the storage
609 system and the number of electrolytic cells are the key decision variables
610 allowing a design to capture wind energy or a design able to operate con-
611 tinuously. A global sensitivity analysis on each objective showed that the
612 temperature variations of the ammonia reactor and the wind speed measure-
613 ment influence the load factor, while the NH_3 production is either dominated

614 by the wind speed measurement or by the temperature fluctuation in the am-
615 monia reactor. The integrated temperature variations in the AWE have little
616 influence on the noise on each DDO objective.

617 Similar to the DDO case, the robust optimization procedure delivered a
618 trade-off between a productive and a robust design. The key decision vari-
619 able for obtaining either one of the two designs lies within the sizing of the
620 total storage system. A larger sized storage system grants the opportunity
621 to produce higher amounts of ammonia, but is subjected to the uncertainty
622 of the wind speed measurement and the temperature fluctuation in the am-
623 monia reactor. In contrast to this productive design, the most robust design
624 provides lower quantities of ammonia, but is only subjected to the tem-
625 perature fluctuation of the ammonia reactor and in smaller proportion to
626 the temperature variation in the AWE. Implementing a more accurate wind
627 speed measurement device and increasing the monitoring measurements of
628 the heat exchanger that controls the incoming flow towards the HBS reactor
629 can decrease the CoV on the NH_3 production in both RDO cases. A future
630 investigation will involve analyzing the dynamic operations of the power-to-
631 ammonia pathway and robustifying its levelized cost.

632 **Acknowledgments**

633 The work has been performed in the scope of the GenComm project,
634 funded by Interreg North-West Europe. Aspen Plus was used under academic
635 license.

636 **Appendix A. Parameters alkaline water electrolyzer**

Table A.5: Model parameters of the AWE located in the PHOEBUS plant operating at a pressure of 7 bar and a temperature between 30 and 80°C [36].

U-I parameters		Value
r_1	$[\Omega\text{m}^2]$	7.33110^{-5}
r_2	$[\Omega\text{m}^2\text{ }^\circ\text{C}^{-1}]$	-1.1010^{-7}
s_1	$[\text{V}]$	1.58610^{-1}
s_2	$[\text{V }^\circ\text{C}^{-1}]$	1.37810^{-3}
s_3	$[\text{V }^\circ\text{C}^{-2}]$	-1.60610^{-5}
t_1	$[\text{m}^2\text{A}^{-1}]$	1.59910^{-2}
t_2	$[\text{m}^2\text{A}^{-1}\text{ }^\circ\text{C}^{-1}]$	-1.302
t_3	$[\text{m}^2\text{A}^{-1}\text{ }^\circ\text{C}^{-2}]$	421.310^2
A	$[\text{m}^2]$	0.25
η_F parameters		
f_1	$[\%]$	99.5
f_2	$[\text{m}^2\text{A}^{-1}]$	-9.5788
f_3	$[\text{m}^2\text{A}^{-1}\text{ }^\circ\text{C}^{-1}]$	-0.0555
f_4	$[\text{m}^4\text{A}^{-1}]$	1502.7083
f_5	$[\text{m}^4\text{A}^{-1}\text{ }^\circ\text{C}^{-1}]$	-70.8005

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