

Design, Fabrication, Modeling and Characterization of a Polyimide-Based Membrane for High Strain Studies in Microfabricated Devices

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Abstract—This paper reports the design, integration, modeling and characterization of single crystalline (c-Si) resistors on a 3.6 μm -thick and 2.7 mm-diameter polyimide MEMS membrane. We propose a straightforward *top-down* fabrication scheme to integrate any microfabricated devices onto a flexible membrane. A *bulge-test* setup is assembled to measure the deflection of the membrane under a white light interferometer. In addition, a finite elements method (FEM) model is introduced to predict the behavior of the membrane under increasing pressure up to 80 kPa. The parameters of the FEM simulation are tuned with the deflection results to extract the strain tensor, showing a maximal biaxial strain of 0.37% at 80 kPa in the 300 nm-thick c-Si devices. Raman spectroscopy is finally employed to confirm the FEM results by comparing the estimated Raman peak-shift with actual Raman measurements. The shift predicted using phonon-deformation potential (PDP) theory shows excellent agreement with the experimental validation, giving confidence in the FEM model.

Index Terms—Flexible MEMS, polyimide membrane, strain, *comsol*.

I. INTRODUCTION

STRAIN engineering of micro-fabricated devices is a very active and ever-growing scientific enquiry. Be it in the field of performance improvement of devices [1], [2], sensing [3] or in the world of material science [4].

A popular choice for strain induction, is to rely on the mismatch between two material's thermal expansion coefficient generating stress during the fabrication process [5], [6]. This approach lead to the development of MEMS-based techniques allowing strain studies to be carried out up to the mechanical limits of the material [7], [8]. However, those techniques do not provide a dynamical control of the induced strain. Different devices, tailored to reach various strains, must be fabricated to cover a large range of deformation with sufficient step resolution. This leads to process and design complications as well as device-to-device variation in the measurement.

Received 15 January 2025; revised 5 March 2025; accepted 31 March 2025. Date of publication 3 April 2025; date of current version 24 April 2025. This work was supported by the joint PDR / Suisse FRS-FNRS / SNF Project between the EPFL (École polytechnique fédérale de Lausanne) in Switzerland and the UCLouvain in Belgium. The review of this article was arranged by Editor Philip Feng. (*Corresponding author: Loïc Lahaye.*)

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Digital Object Identifier 10.1109/TMAT.2025.3557763

Another approach is to actively induce strain in a material or device via an external actuation mechanism. One technique is to rely on a bulge or blister test using a micro-fabricated membrane subject to increasing pressure. One way to do so is to use a thin, stress compensated, oxide based, membrane carrying the device or material of interest. While this approach has been extensively studied, as reported in [9], [10], it is generally used for pressure sensing rather than for inducing high strain. Indeed, those membranes are prone to breaking and typically allow to reach strain of up to 0.04% as in [11]. Other fabrication processes, like Silicon-on-Nothing (SON), can be used to build the membrane but they face similar challenges while only reaching 0.036 % of strain [12].

A promising path to reach higher strain levels is to build the membrane out of a polymer. The lower Young's modulus of polymers allows for more bulging and deformation of the membrane before fracture, which enables to induce a higher strain in the device or material of interest. A first example comes from [13] which integrates a 2D-layer of MoS_2 onto PDMS and reaches between 2 and 3 % of strain during the blister test. Another one, from [14], reports the integration of 10 nm-thick silicon resistors on a polyimide (PI) membrane. They demonstrate the induction of 3.5 % of strain in the silicon resistors [14].

While the use of PDMS or polyimide allows to reach high strain in the studied material, the practice comes with some drawbacks. The first one is bound to the use of soft plastics that exhibit poor resistance to heat or strong chemicals [15]. This renders them incompatible with many conventional processing techniques. The integration of electronic devices or material must be done via either a direct low temperature deposition, like in [15], or complex transfer and subsequent alignment of electronic layers, like in [14]. Other examples of flexible electronic processing, that illustrate their complex nature, are otherwise well described in the literature, including [16], [17], [18], [19]. A further issue is the lack of fundamental understanding of the mechanics governing the behavior of these flexible media. While conventional MEMS membranes benefit from a rich literature allowing to predict both the behavior of the membrane and the strain induction in the device under test [20], [21], [22], [23], [24], this is not the case for complex polymeric stacks. Furthermore, the strain field in the active material layer is often

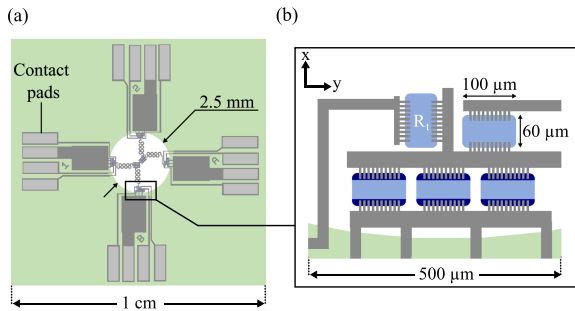


Fig. 1. Design schematics: (a) Layout showing a $1 \times 1 \text{ cm}^2$ die featuring a 2.5 mm-diameter circular membrane. (b) Zoom on a subset of devices located on the membrane edge. R_t stands for transversal resistor regarding the orientation of its electrical connections relative to ε_{xx} in local coordinate. The x and y axis are shown as black arrows. The aluminium lines are in gray, the pad openings in light gray, the membrane in white and the die in light green. NPN devices and other resistors are visible on the layout but out of the scope of this work.

simplified and treated as uniaxial or biaxial, like in [14], without formal validation which might prove detrimental in experiments requiring precise knowledge of the strain field components.

This work proposes both a simplified processing scheme for straightforward fabrication of flexible membrane for high-strain studies and a complete study of the mechanical behavior of the stack. The presented process integrates single crystal silicon (c-Si) devices with electrical connections on a $3.6 \mu\text{m}$ -thick and 2.7 mm -diameter PI membrane, without process limitation or complex layer transfer. In addition, a finite element method (FEM) model is built to study both the evolution of the membrane deflection and the strain field induced in the active silicon. In this study, the complete strain tensor is extracted from the FEM simulation, without assuming a particular shape of the strain field. To check the validity of our FEM model, a compact bulge test setup is introduced to pressurize the membrane and study its behavior both under a white-light interferometer and a Raman spectrometer.

II. FABRICATION

A. Design

Fig. 1(a) represents the layout of a die carrying a 2.5 mm-diameter circular membrane. Each die features four sets of two c-Si p-type resistors and four NPN junctions positioned alongside the membrane's perimeter to maximise the amount of induced strain [10], [12]. All devices share the same $60 \mu\text{m}$ by $100 \mu\text{m}$ dimensions as visible in Fig. 1(b). Electrical connections are made by $1 \mu\text{m}$ -wide aluminium fingers and $20 \mu\text{m}$ -wide aluminium traces that extend from the die onto the released membrane. $500 \mu\text{m}$ by $1500 \mu\text{m}$ contact pads are visible in light gray on the figure. The study carried out in this work is performed on R_t which stands for transversal resistor. It is defined by the current flowing perpendicularly to the direction of the ε_{xx} strain component in local coordinate. All other structures visible on the layout are out of the scope of this paper.

B. Process

The integration of p-type silicon resistors on a thin polyimide membrane is illustrated in Fig. 2. The process starts in Fig. 2(a)

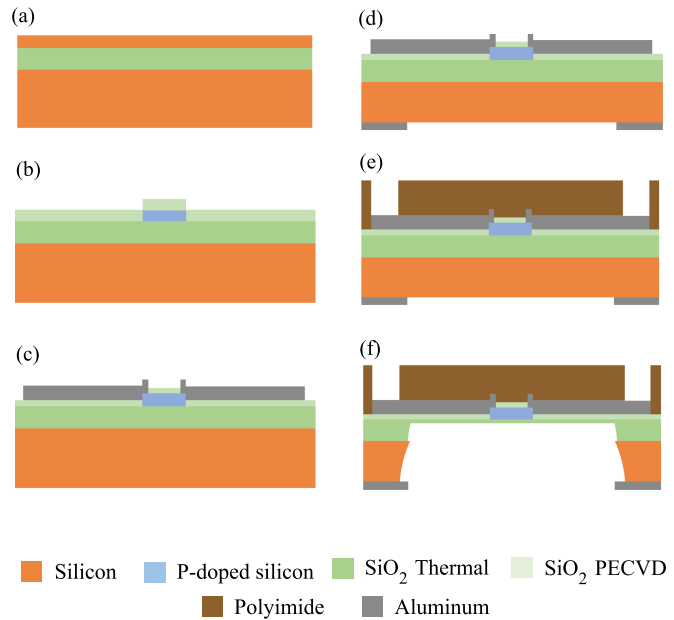


Fig. 2. Process flow schematics: Summary of the fabrication process used to integrate silicon resistors on a large, free standing, polyimide membrane. (a) Initial (100) SOI wafer with a top 300 nm c-Si layer, 1050 nm buried oxide (X) and c-Si substrate. (b) ICP-RIE patterning, doping and passivation with 180 nm of PECVD silicon dioxide of the top silicon to pattern $60 \mu\text{m}$ by $100 \mu\text{m}$ p-type c-Si mesas. (c) Electrical contacts deposition by sputtering a 600 nm-thick Al/Si layer, patterned with dry etching. (d) Back grinding of the c-Si substrate and definition of a 300 nm-thick aluminium mask. (e) Spin coating of a $3.6 \mu\text{m}$ -thick polyimide layer and contact pads opening by laser etching. (f) Release of the polyimide membrane by an isotropic XeF_2 dry etch of the c-Si substrate and isotropic BHF wet etch of the BOX.

with a silicon-on-insulator (SOI) wafer from *SOITEC* featuring a top 300 nm-thick (100) oriented c-Si layer, a buried oxide (BOX) of 1050 nm and a bulk c-Si substrate of $725 \mu\text{m}$.

To define the resistors, $60 \mu\text{m}$ by $100 \mu\text{m}$ silicon mesas are patterned in Fig. 2(b) by photolithography and anisotropic CHF_3 inductively coupled plasma reactive ion etching (ICP-RIE from *Corial*). The top silicon layer is thermally oxidized as a preparation step for ion implantation resulting in a 27 nm-thick silicon dioxide layer. A boron implantation step is performed to obtain p-type resistors. The implantation was performed by *Ion Beam Service (IBS)* with a requested dose of 4.2×10^{13} atoms/ cm^2 at an energy of 10keV. Doping atoms are then activated by a 30-minutes-long annealing at 850°C to complete the implantation phase. The final boron atom concentration in the silicon is estimated using a Silvaco Athena simulation to reach a maximal value of $3.5 \times 10^{18} \text{ cm}^{-3}$. A 180 nm-thick silicon dioxide layer is then deposited by plasma-enhanced chemical vapour deposition (PECVD by *Oxford Instruments*) to passivate the doped silicon resistors after stripping of the top 27 nm-thick thermal oxide used for the implantation process.

Fig. 2(c) deals with the electrical contacts definition. Access to the silicon mesas are first opened in the top silicon dioxide layer by a photolithographic step and a buffered HF ($\text{HF} + \text{NH}_4\text{F}$ in a 1:7 ratio) isotropic wet etch. The electrical connections are then built by sputtering (using a machine from *VST*) a 600 nm layer of Al/Si (99% aluminium and 1% silicon) next defined by photolithography and ICP-RIE BCL_3 anisotropic dry etch.

A 432° C thermal annealing under a flow of forming gas is finally performed to obtain an ohmic contact between the p-doped silicon and the aluminium.

Fig. 2(d) summarizes the preparation required for the release of the membrane. The wafer is first back-grinded from 725 μm to 280 μm in order to reduce the time needed to release the membrane. A 300 nm-thick aluminium mask is deposited by thermal evaporation (evaporator from VST) and patterned by photolithography and H_3PO_4 isotropic wet etch on the back side of the wafer to define the membrane geometries.

Polyimide is chosen as flexible substrate, as in [14], [25], and its integration as the last layer is done by spin coating a PI precursor as shown in Fig. 2(e). A commercial solution from HDMicroSystem, PI2545 [26], is used along with VM652, an adhesion promoter [27] from the same company. After priming of the wafer top surface with VM652, PI2545 is spun at a speed of 1500 rpm and cured at 350°C during one hour [26]. A final cured PI thickness of 3.6 μm is measured by ellipsometry. Access to the contact pads is then opened with a maskless picosecond-laser etching step (by Oxford Instruments). At this stage the wafer is diced to form 1 cm by 1 cm dies. As illustrated in Fig. 1(a), each die carries one 2.5 mm-diameter membrane.

Fig. 2(f) illustrates the membrane release which was done in two consecutive steps. A dry isotropic XeF_2 etch of the back c-Si is done (machine from Xatic), resulting in a slight 100 μm over etch and a final membrane of 2.7 mm-diameter.

Finally, the BOX is thinned by a timed isotropic BHF wet etch. A residual silicon dioxide layer of around 200 nm-thick is left to avoid the BHF to enter in direct contact with the silicon devices on the membrane's back side. Fig. 3(a) shows a picture of a released membrane.

We believe that the proposed method represents a potential simplification compared to [14] since it relies on a *top-down* integration scheme instead of a transfer of the active layer.

III. MATERIALS AND METHODS

A. Simulation Framework

Due to the radical differences between the presented membrane stack which uses a low Young's modulus polyimide and a conventional silicon bulk micro-machined or stress compensated MEMS membrane, the behavior of our platform could not be predicted by usual analytic models like in [20], [22]. Furthermore, preliminary experimental tests, informed us that the stack enters in a plastic deformation regime passed a certain pressure level. This renders the use of analytical models for large deflection membranes like the ones of [28], [29], [30] impossible as well. A FEM simulation framework that takes into account plastic deformation has been developed using *Comsol Multiphysics* and is used to predict the deflection profile of the membrane and the evolution of the strain field in the c-Si resistors as a function of the applied pressure.

The model is built according to the real dimensions of the as-fabricated membrane to take into account the process non-idealities such as the over-etch. The simulation model is made out of a stack comprising a 200 nm-thick thermal silicon dioxide layer, the active 300 nm-thick patterned c-Si, the 180 nm-thick

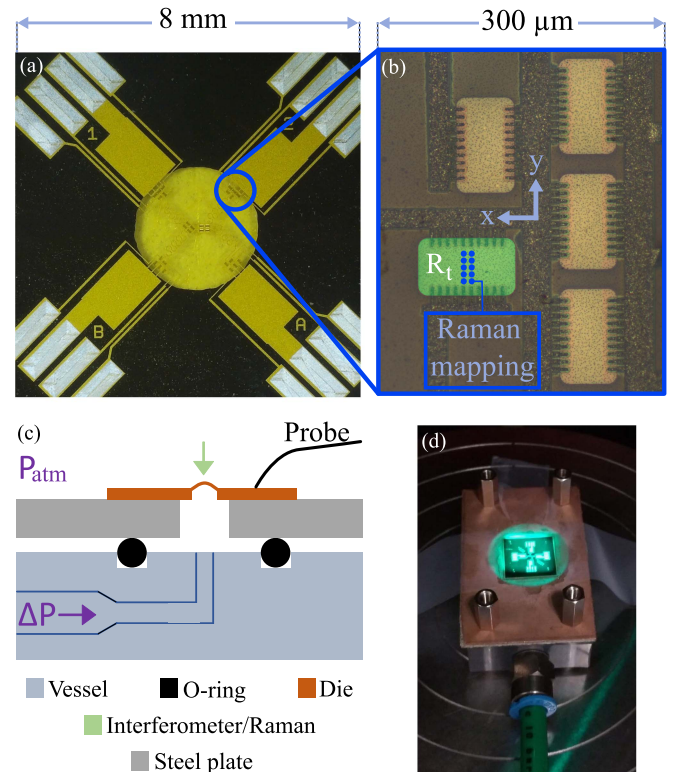


Fig. 3. Sample and instrumentation setup: (a) Top view of a 3.6 μm -thick and 2.5 mm-wide polyimide membrane. (b) Zoom on a subset of devices positioned along the membrane's edge. The device highlighted in green is a p-type resistor arranged in a transverse configuration regarding the direction of the current relative to the direction of the strain. The blue dots represent the 10 mapping points measured by the Raman spectroscopy. Uncolored devices are out of the scope of this paper. (c) Pressurisation setup with a die featuring a membrane glued on a steel plate fixed to a pressure vessel. Air tightness is ensured by an O-ring. A pressure generator is connected at the inlet ΔP . This setup can be set under a Michelson interferometer or a Raman spectroscopy. The devices are electrically contacted by probes mounted on micromanipulators. (d) Picture of the experimental bulge test setup.

PECVD silicon dioxide layer and a 3.6 μm -thick polyimide layer similar to the one presented in Fig. 2. A 2.7 mm-diameter circular membrane with c-Si devices located around its perimeter is simulated. The materials Young's moduli are set to 87 GPa [31] and 2.7 GPa [26] for the SiO_2 and PI, respectively. The stiffness matrix of silicon, \mathbf{C}_{Si} , is used to take into account the material anisotropy [32], [33]. In our case, the principal strain components, ε_{xx} and ε_{yy} , are along $\text{Si}_{\langle 110 \rangle}$.

To simulate the mechanical behavior, the *Solid Mechanics* module from Comsol is used to compute the stress, strain and displacement of each node in the mesh. All implemented equations are describe in the software technical documentation [34].

Regarding the plastic behavior of the stack, the following *Swift* model is implemented into *Comsol* to compute the actual stress and stain levels in the plastic regime [35]:

$$\sigma_{\text{eff}} = \sigma_{y,\text{eff}} \left(1 + \frac{\varepsilon}{\varepsilon_{0,\text{eff}}} \right)^{n_{\text{eff}}} \quad (1)$$

σ and ε are the actual stress and strain while $\sigma_{y,\text{eff}}$, $\varepsilon_{0,\text{eff}}$ and n_{eff} are respectively the effective yield stress, reference strain and hardening coefficients to be fitted on experimental data.

B. Bulge Test Setup

An instrumentation setup is designed to allow the pressurisation of the PI membrane and induce strain in the silicon devices. The setup, illustrated in Fig. 3(c) and (d), is made out of a pressure vessel with a device mounted on top. The die to be tested is first glued on a steel plate with M-bond 200 [36]. The steel plate is pierced to allow the pressure to be transferred to the membrane. The sub-assembly is then mounted on the pressure vessel by four screws while an O-ring ensures proper sealing between the plate and the vessel.

The pressure vessel in itself is made out of a machined acrylic block to allow the connection of a pressure generator at the inlet ΔP . The pressure generator is a KAL-100 from *Halstrup Walcher*, allowing the production of controlled pressure in the 0 to 100 kPa range with a 0.05% accuracy [37]. In this study, the maximum applied pressure is of 80 kPa. The whole assembly is compact enough to be placed under a white light interferometer or a Raman spectrometer as shown in Fig. 3(d).

C. Deflection Measurement

The measurement of the deflection is carried out by a white light interferometer from *Polytec* [38]. This non-destructive measurement allows to obtain the local deflection profile of our bulged membrane [39].

A die carrying a 2.7 mm-diameter membrane is mounted on the bulge test setup and the deflection profile of the membrane is measured. The additional pressure above atmospheric, ΔP , ranges from 1 to 80 kPa by steps of 1 kPa up to 22 kPa, 2 kPa up to 40 kPa and 4 kPa up to 80 kPa. The pressure is then lowered following identical steps down to 1 kPa. The 0 kPa pressure point is not measured because the released membranes do not always have a flat profile due to residual stress in the stack inducing buckling. The 1 kPa deflection level is taken as reference.

Raw measured Polytec profiles are leveled to remove the die inclination and fitted by a second-order least-square method. The maximal deflection points are detected and plotted as a function of the pressure for each bulged profile.

Measuring the evolution of the membrane maximal deflection as a function of the pressure is done to calibrate the simulation parameters. The $\sigma_{y,\text{eff}}$, $\varepsilon_{0,\text{eff}}$ and n_{eff} parameters from the *Swift* model [35] are to be fitted on the data point from the white light interferometer to tune the simulation.

D. Strain Field Raman Validation

In order to properly validate the strain field results obtained from the simulator, a Raman spectroscopy experiment was designed using a LabRAM HR from *Horiba Scientific* equipped with a 514 nm laser. This non-destructive measuring technique allows to obtain Raman spectra which are specific to every material since they depend on their structural configuration [40].

At rest, the Raman spectrum of (100) silicon is made out of one longitudinal optical (LO) mode centered around 520.7 cm^{-1} [41]. Upon straining of the c-Si devices, the modification of the crystal lattice will result in a measurable shift of the Raman peak position which will be used to validate our simulation model [42].

Similarly to the deflection setup, the peak shift is measured for pressures ranging from 0 to 80 kPa with steps as described in Section III-C. The measurement is made using a 514 nm laser that first penetrates through the 3.6 μm -thick PI layer. The PI layer does not interfere with the experiment since polyimide features a low absorbance coefficient for green light [43] and only features Raman peaks far from the one of c-Si, at above 1000 cm^{-1} [44].

A 10-point mapping is done at each pressure step by measuring the Raman response of the silicon device at 10 different locations of R_t as illustrated in Fig. 3(b). This mapping leads to noise and mismatch measurement reduction and allows the extraction of the average peak-shift value induced by strain in the silicon mesa.

Data processing starts by first averaging the 10 Raman spectra of each pressure point. The averaged peak is then normalized relative to its own maximum and the obtained data points are fitted by a Lorentzian function [40]. In the case of a (100) top plane c-Si, only the longitudinal optical mode is observable [45]. The maximum value hence corresponds to this LO peak which is detected around the initial 520.7 cm^{-1} resting position. Doing this for each pressure step provides us with an experimental measurement of the peak shift as a function of the pressure.

No strong hypothesis can be made regarding the shape of the strain field induced in our c-Si devices. To validate our simulation results, we solve the eigen-value problem of [46] based on the secular matrix (2) shown at the bottom of this page. It is used to compute the pressure-peak shift variation $\hbar\omega_i$ of the three Raman optical modes based on the full non-linear strain tensor given by the FEM simulation. Solving the eigenvalue's problem allows to find the three λ_i and then the shifts using $\hbar\omega_i = \sqrt{\lambda_i - \omega_0^2}$ with $\hbar\omega_0 = 520.7 \text{ cm}^{-1}$. Three parameters (p , q and r) called the phonon deformation potential (PDP) coefficients are used. In this work, coefficients reported by [47] and [48] are used. Solving the eigenvalue problem based on (2) using the *Comsol* strain tensor will provide us with a theoretical estimation of the strain/peak-shift relation that will be compared with the actual Raman experimental data.

IV. RESULTS AND DISCUSSIONS

A. Deflection Results

Deflection results of a 3.6 μm -thick and 2.7 mm-diameter polyimide membrane are presented in Fig. 4. A subset of five raw deflection profiles is illustrated in the figure's inset. A gradient of color from light to dark green is used to represent increasing

$$\begin{pmatrix} p\varepsilon_{11} + q(\varepsilon_{22} + \varepsilon_{33}) & 2r\varepsilon_{12} & 2r\varepsilon_{13} \\ 2r\varepsilon_{12} & p\varepsilon_{22} + q(\varepsilon_{33} + \varepsilon_{11}) & 2r\varepsilon_{23} \\ 2r\varepsilon_{13} & 2r\varepsilon_{23} & p\varepsilon_{33} + q(\varepsilon_{11} + \varepsilon_{22}) \end{pmatrix} \quad (2)$$

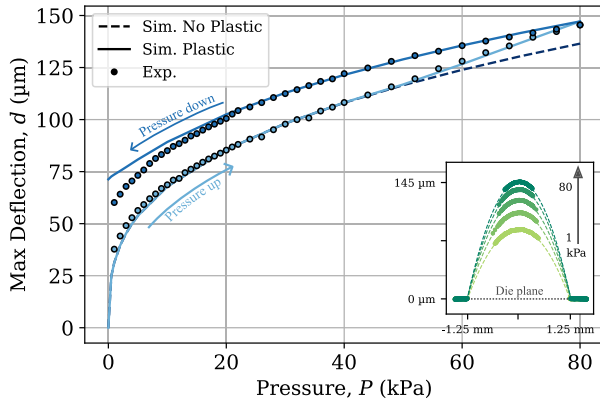


Fig. 4. Deflection measurement of a $3.6 \mu\text{m}$ -thick 2.7 mm -diameter circular polyimide membrane: The inset shows a selection of local deflection profiles under increasing pressure at 10, 20, 40, 60 and 80 kPa taken by a white light interferometer. The main plot shows the maximum of each raw deflection curve for pressure ranging between 1 and 80 kPa and then 80 to 1 kPa. Light and dark blue circles are used for experimental data point for the up and down pressure cycle, respectively. The plain lines represent the simulation considering plasticity for both the up and down pressure cycles with the same color code. The dashed line represents a simulation that does not consider plasticity.

pressure levels at 10, 20, 40, 60 and 80 kPa. Green dots are used to represent the experimental data while dashed lines represent the least-square error approximation of a second-order polynomial. The membrane bulge increases with the pressure to reach a maximal deflection of $145 \mu\text{m}$ relative to the die plane at 80 kPa.

The main plot reports the maximal deflection measured at each intermediary step. Measurements are being displayed as light and dark blue dots for increasing and decreasing pressure, respectively, while plain lines are used to display the simulation results using the same color code. The dashed line is a simulation of our stack but without using the *Swift* model.

Upon pressurisation, the maximal deflection of the membrane follows a non-linear cube-root trend as expected for large deflection scenarios [29], [30]. The deflection curve follows this trend, which is perfectly modelled by both simulation models up to 50 kPa. Passed this point, both the plastic simulation and the experimental data start to diverge from the non-plastic simulation. The deflection continues to increase up to the reported maxima at 80 kPa.

When the pressure starts diminishing, both the simulated and measured maximal deflections start to decrease. The two curves follow a trend parallel to the dashed line which simulates the expected non-plastic behavior of the stack. This relaxation profile is expected and well documented in literature [49]. Once a material entered in a plastic deformation regime, when stress is released, the stress-strain curve follows a linear trend and reaches a permanently-strained final state, which is the case here at 1 kPa at the end of the bulge test. The final relaxed state features a permanently strained shape with a residual deflection of $60 \mu\text{m}$.

The final fitted values of the *Swift* model parameters are $\sigma_{y,\text{eff}} = 450 \text{ MPa}$, $\varepsilon_{0,\text{eff}} = 0.0025$ and $n_{\text{eff}} = 0.05$. Those effective parameters allow to simulate the plastic behavior of our specific stack and geometry. The model also allows to estimate

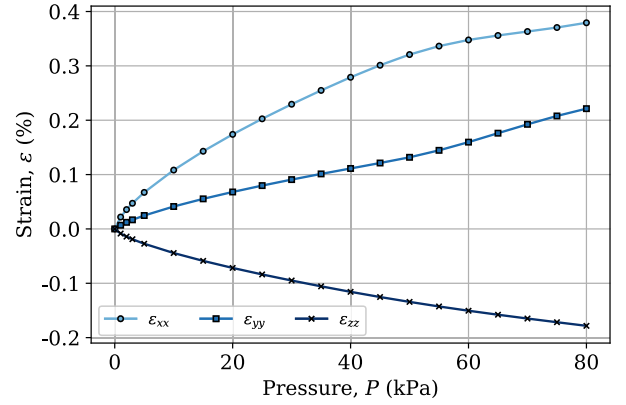


Fig. 5. Strain field simulation: Strain field inside a $0.3 \mu\text{m}$ -thick c-Si device on a $3.6 \mu\text{m}$ -thick 2.7 mm -diameter polyimide membrane under increasing pressure ranging from 0 to 80 kPa. Circles, squares and crosses are used to represent ε_{xx} , ε_{yy} and ε_{zz} , respectively.

the residual BOX thickness at around 160 nm. This is well in line with the process based estimation of 200 nm.

B. Strain Results

Fig. 5 depicts the simulated evolution of the strain field under increasing pressure in R_t . The plot only shows the main x , y and z components as the shear components are evaluated to be close to zero. As can be read on the graph, the strain field is a complex biaxial one. This is unlike what is obtained for small deflection setups where devices located on the edge of the membrane are expected to undergo uniaxial straining [11], [20]. Upon pressurisation of the membrane, both ε_{xx} and ε_{yy} are steadily increasing and follow a non-linear trend similar to the deflection. Again, this is unlike the linear evolution of strain with pressure reported by the literature for small deflection setups [20], [22].

The entry in the plastic regime of the stack, at around 50 kPa, is visible for both the x and y profiles with a decrease and increase of their respective slope. A maximum of 0.37% of deformation is obtained for ε_{xx} and 0.23% for ε_{yy} in R_t . ε_{zz} showcases a steady increase up to -0.18% . The plasticity of the deformation is not visible for ε_{zz} since it is a linear combination of both the x and y components of the strain tensor following:

$$\varepsilon_{zz} = -\nu_{\text{Si}} (\varepsilon_{xx} + \varepsilon_{yy}) \quad (3)$$

where $\nu_{\text{Si}} = 0.28$ is the Poisson ratio of silicon [33].

Those results demonstrate the capacity of our flexible PI based platform to induce reasonable strain levels of up to 0.37% in silicon. This level is more than one order of magnitude bigger than what is achievable with classical bulk micro-machined or stress-compensated membranes that typically only induce up to 0.04% of strain in the device under test [11], [12]. The here reported deformation level is however one order of magnitude lower to the 3.5% of strain reached by [14]. This is explained by both their thinner 10 nm-thick silicon layer and higher 213 kPa maximal induced pressure.

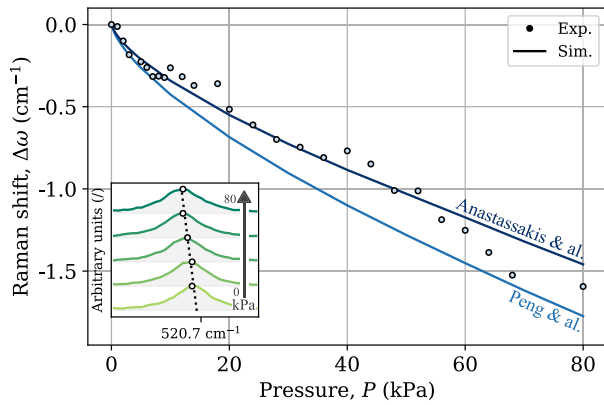


Fig. 6. Raman silicon peak shift: Raman peak shift measured into a $0.3 \mu\text{m}$ -thick c-Si resistor on a $3.6 \mu\text{m}$ -thick 2.7 mm -diameter polyimide membrane under increasing pressure levels. The inset represents the raw Raman spectrum of the silicon at pressures of 10, 20, 40, 60 and 80 kPa. The main plot shows the evolution of the position of the LO optical mode. Blue dots represent the experimentally obtained peak shifts. Plain light and dark blue lines represent the simulated peak shift obtained using the PDP coefficients from Peng and al. and Anastassakis and al. in R_t , respectively.

C. Raman Validation

Fig. 6 highlights the results of the Raman validation experiment. The inset provides a selection of raw Raman spectra at increasing pressure levels of 10, 20, 40, 60 and 80 kPa. The shift of the maxima can be seen in the inset.

The main plot reports the evolution of the silicon LO peak position as a function of the pressure between 0 and 80 kPa. The experimentally obtained data is represented as blue dots. The simulation of the Raman peak shift is provided by the plain blue lines. They are computed based on the simulated strain tensor for two different sets of p, q and r PDP coefficients provided by [47] and [48].

Contrary to what is usually found in literature, the exact strain tensor has been used to retrieve the shift of the Raman peaks with the strain. A typical use of Raman spectroscopy is to either rely on an empirical peak-shift/strain relationship as in [14], [50] or on a simplification of the full Ganesan matrix as in [51]. In both cases, an indirect approximation of the strain is achieved based on a measurement of the peak-shift and a set of hypothesis made on the shape of the studied strain field. In our case, the obtained Raman results are used to check our FEM simulation. This allows the use of the full strain tensor without a-priori knowledge on its shape and components. As visible in Fig. 6, a good agreement between the simulation and the measurement is obtained. Since the experimental peak shift is an expression of the impact of the complete non-linear biaxial strain field in silicon, this gives us strong confidence in the simulated strain tensor.

The deviation between the FEM model and the experimental measurement is explained by the angle of incidence of the Raman laser. The important deflection of the membrane leads to the inclination of the c-Si devices. An angle of 3.6° is reached at 5 kPa, 5.6° at 10 kPa and 9.6° at 80 kPa, relative to the die plane. This induces a Raman response from other phonon modes such as transverse optical (TO) ones. This additional contribution

to the Raman spectrum reduces the accuracy of the LO peak extraction [52], [53].

This validation, made on a canonical material like silicon, implies that our simulation framework is valid and could hence be used to predict the induction of strain in other materials without the need of a Raman measurement. This would be of particular interest for materials featuring complex, multi-peaks, Raman spectra for which empirical strain-shift relation are unknown.

Furthermore, the agreement between the simulated and experimental strain tensor demonstrates that fitting the simulation parameters on a measurement of the deflection of the membrane is sufficient to precisely estimate the strain in the electrical devices. It also demonstrates proper adhesion and hence stress transfer from the membrane to the c-Si device without slippage or delamination of the film.

V. CONCLUSION

This paper reports the integration of c-Si resistors on a $3.6 \mu\text{m}$ -thick and 2.7 mm -diameter polyimide MEMS membrane using a *top-down* processing scheme. A *Comsol Multiphysics* FEM model of the membrane stack is introduced and fitted on a measurement of the membrane deflection made with a white light interferometer. This allowed to recover effective mechanical properties of the membrane as-well as the strain field induced in the silicon device.

The strain field in the c-Si resistors is found to be non-linear and biaxial. A maximal strain of 0.37% is obtained in the silicon. This represents more than a 10-fold increase compared to the strain induced by a conventional bulk micro-machined or stress compensated membrane.

Finally, the validity of the simulated strain field was checked by Raman spectroscopy. An innovative technique based on the resolution of Ganesan's secular equation using the simulated strain tensor was used. Excellent agreement of the simulation and Raman experiment allows us to have strong confidence in the simulated strain field. This agreement also demonstrates that fitting the simulation parameters on a measurement of the membrane deflection is sufficient to properly predict the strain field in the electrical device. Our work hence proposes the following methodology to perform high-strain studies on any material without the need for in-situ strain measurement: (i) Fabrication of the device to be strained via conventional processing techniques, (ii) Integration on flexible substrate, (iii) Measurement of the membrane deflection under pressure, (iv) Fitting of the simulation parameters to obtain a complete pressure-strain field relation.

AUTHORSHIP CONTRIBUTION STATEMENT

Loïc Lahaye: Writing - review & editing, Writing – original draft, Visualization, Validation, Methodology, Investigation, Formal Analysis, Conceptualization, Data Acquisition. **Nicolas Roisin:** Review, Validation, Methodology, Formal Analysis, Conceptualization, Data Acquisition. **Nicolas André:** Review, Methodology, Resources. **Denis Flandre:** Review, Supervision, Funding acquisition, Conceptualization. **Jean-Pierre Raskin:** Review, Supervision, Funding acquisition, Conceptualization.

DECLARATION OF COMPETING INTEREST

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

DATA AVAILABILITY

Data will be made available on request.

ACKNOWLEDGMENT

The cleanroom Winfab (Wallonia Infrastructure for Nano Fabrication) as well as the characterization lab Welcome (Wallonia Electronics & Communication Measurements) was provided by the ICTTEAM department (Institute of Information and Communication Technologies, Electronics and Applied Mathematics) of the UCLouvain. Many thanks to Christian Renaux, Sébastien Faniel and Miloud Zitout, staff members of the Winfab cleanroom platform for their help and support throughout this research. A special thanks also goes to Benoît Hubert, technician in the Welcome characterization platform for his time, consideration and support.

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