



UNIVERSITÉ CATHOLIQUE DE LOUVAIN

**Noncontact Dimensional Metrology
by Triangulation under Laser Plane Lighting**

Development of New Field Instruments

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Ph. D. Thesis

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Table of Contents

Table of Contents	i
List of Figures	vii
List of Tables	xi
Acknowledgements	xiii
1 General Introduction	1
1.1 Context and Motivation	2
1.2 Brief Description of the Method	3
1.3 Philosophy of the Thesis	3
1.4 Outline of the Dissertation	5
1.5 Personal Publications	5
I Theory	9
2 Camera Model	11
2.1 Introduction	12
2.2 Camera and Lens Models	12
2.2.1 The thin lens model	13
2.2.2 The pinhole model	14
2.3 Vocabulary and Notations	15
2.4 Camera Parameters	16
2.5 Passage Equations	17
2.6 Correction of the Distortion	19
2.7 Considerations on the Focalization Lens	20
2.7.1 Focusing	20
2.7.2 Chromatic aberration	21

3	Laser Triangulation under Structured Lighting	23
3.1	Introduction	24
3.2	Principle	24
3.2.1	Laser triangulation	24
3.2.2	Structured lighting	25
3.3	Typical Configuration	28
3.4	Parameters and Equation of the Laser Plane	28
3.5	Link between the Image Plane and the Scene	30
4	Hardware	33
4.1	Introduction	34
4.2	CCD Cameras and Lenses	34
4.2.1	CCD cameras	34
4.2.2	Camera lenses	36
4.3	Laser Diodes and Optics	37
4.4	Interference Filters	39
4.5	Video Capture Boards	41
5	Image Processing	43
5.1	Introduction	44
5.2	Image Acquisition	45
5.3	Preprocessing	46
5.3.1	Subtraction	46
5.3.2	Thresholding	47
5.3.3	Multi-level thresholding	49
5.4	Segmentation	50
5.5	Object Feature Determination	51
5.6	Object Selection	52
5.6.1	Amount of pixels	52
5.6.2	Height-to-width ratio	52
5.6.3	Distance from central column	53
5.7	Postprocessing	53
5.7.1	Subpixel location of a laser curve	55
5.7.2	Speckle filtering of a laser curve	58
5.7.3	Curve smoothing	62
5.7.4	Correction of the distortion	62
6	Calibration of the Devices	65
6.1	Introduction	66
6.2	Camera Calibration	66
6.2.1	In Practice	66
6.2.2	Performances	68
6.3	Laser Plane Calibration	69
6.3.1	Positioning of the Problem	69
6.3.2	Gradient Descent	72

6.3.3	In practice	73
6.3.4	Performances	74
7	Accuracy Analysis	77
7.1	Introduction	77
7.2	Sampling Errors	77
7.2.1	Accuracy on the y coordinate	78
7.2.2	Accuracy on the z coordinate	79
7.2.3	Accuracy on the x coordinate	80
7.3	Speckle	81
7.4	Calibration Errors	83
7.4.1	Error due to a bad estimation of e	83
7.4.2	Error due to a bad estimation of f	83
7.4.3	Error due to a bad estimation of δ	84
7.5	Summary	84
8	Some Existing Ambulatory Devices	87
8.1	Introduction	88
8.2	The Biris Range Sensor	88
8.3	An Instrument to Measure the Size of Skin Wounds	90
8.4	A Mars Landing System Using Structured Lighting	92
8.5	Pipe Inspection Using a Laser-Based Transducer	92
II	Our Applications	97
9	Diameter Measurement of Cylindrical Objects	99
9.1	Introduction	100
9.1.1	Initial context: measurement in forest surveying	100
9.1.2	Generalization to the diameter measurement of cylindrical pieces	101
9.1.3	Organization	102
9.2	Case of a Cylinder Transversal to the Camera Plane	103
9.3	Image Processing	105
9.4	Radius Calculation: the “Three-Tangent Method”	106
9.5	Justification of the “Three-Tangent Method”	108
9.6	Error Made if the Cylinder Tilting is not Taken into Account	110
9.6.1	Preliminaries	110
9.6.2	Methodology	112
9.6.3	Case 1: $\theta \neq 0$ and $\varphi = 0$	112
9.6.4	Case 2: $\theta = 0$ and $\varphi \neq 0$	113
9.6.5	Analysis of the relative error	114
9.7	Generalization to a Randomly Tilted Cylinder	115
9.8	Equation of the Laser Curve in the General Case	116

9.9	Radius Calculation: the Generalized “Three-Tangent Method”	120
9.10	Determination of the Cylinder Orientation	121
9.11	Expected Accuracy	123
9.12	Results	125
9.12.1	Introduction	125
9.12.2	Transversal cylinders	126
9.12.3	Empirical error committed if the cylinder slant is not taken into account	128
9.12.4	Randomly tilted cylinders	129
9.12.5	Limits of the instrument	131
9.12.6	Influence of the camera imperfections	134
9.13	Without a Refined Theory...	134
9.14	Conclusions	135
10	Diameter Measurement of Spherical Objects	137
10.1	Introduction	138
10.1.1	Context: grinding field and robotics	138
10.1.2	Organization	138
10.2	Description of the Instrument	139
10.3	Image Processing	140
10.4	Radius Calculation #1: the “Three Tangent Method”	141
10.5	Radius Calculation #2: the Gradient Descent Method	143
10.6	Expected Accuracy	144
10.7	Results	145
10.8	Without a Refined Theory...	148
10.9	Conclusions	148
11	Dimensional Measurements in the Building Sector	151
11.1	Introduction	152
11.1.1	Context: the building sector	152
11.1.2	Functions of the instrument	152
11.1.3	Building sector needs	152
11.1.4	Organization	153
11.2	Description of the Instrument	153
11.3	Image Processing	155
11.4	Principal Component Analysis	155
11.4.1	Determination of the equation of a plane	156
11.4.2	Quality index	158
11.4.3	Advantages and Limitations	159
11.4.4	Application to our instrument	159
11.5	Results	163
11.6	Without a Refined Theory...	166
11.7	Conclusions	168

12 Determination of the Road Surface Microtexture	171
12.1 Introduction	172
12.1.1 Context: road safety field	172
12.1.2 Positioning of the problem	172
12.1.3 Organization	173
12.2 Description of the Instrument	174
12.3 Determination of the Vertical Road Profile	176
12.4 Pre-prototype	176
12.5 Image Processing	177
12.6 Dealing with Speckle	178
12.7 Expected Accuracy	178
12.8 Calibration of the Instrument	180
12.9 Validation of the Method	182
12.10 Without a Refined Theory...	186
12.11 Development of an Ambulatory Instrument	187
12.12 Illustration on a Road Surface	190
12.13 Conclusions	190
Conclusions and Perspectives	193
Bibliography	197
Appendices	205
A Camera Calibration: Mathematical Developments	207
A.1 Introduction	208
A.2 Homography between the Model Plane and its Image	208
A.3 Constraints on the Intrinsic Parameters	208
A.4 Closed-form Solution	209
A.5 Dealing with Radial Distortion	210

List of Figures

1.1	Definition of optomechatronic technology	3
2.1	Focalization lens, realistic model	13
2.2	Focalization lens, thin lens model	13
2.3	Focalization lens, pinhole model	14
2.4	Decentration for a simple lens	15
2.5	Vocabulary and notations. 3-D view	16
2.6	Camera parameters	18
2.7	y_{pix} determination. View in the (y, z) plane	18
2.8	Distorted image and its undistorted version	21
2.9	Chromatic aberration in a thin lens	22
3.1	Laser triangulation	25
3.2	Some of the available laser patterns for structured lighting	26
3.3	Illustrative application using structured lighting	27
3.4	One-to-one correspondence between the image plane and the scene	27
3.5	Configuration of the device. 3-D view	28
3.6	Geometry of the device	29
4.1	Pictures of the cameras	34
4.2	Pictures of the lenses	37
4.3	Pictures of the lasers	38
4.4	Picture of an interference filter	40
4.5	Pictures of a white wall under natural lighting hit by 3 laser planes	40
4.6	Pictures of the video boards	41
5.1	Typical image	45
5.2	Typical image with the laser diode off	46
5.3	Typical image after subtraction	47
5.4	Histogram of the typical image	48
5.5	Typical image after thresholding	49
5.6	Histogram of the a three-mode image	50
5.7	Mask of 2x2 pixels used for segmentation	51
5.8	Result of the segmentation for a 5x5 pixel portion of an image	52

5.9	Typical image after elimination of the objects composed of less than N_{pix} pixels	53
5.10	Typical image after elimination of the objects with a low height-to-width ratio	54
5.11	Typical image where only the object the closest from the image's central column is kept	54
5.12	Effects of quantization, saturation, DC offset and thresholding on the Gaussian intensity profile	56
5.13	Laser curve on the reference image after subpixel location . . .	58
5.14	3-D representation of the low-pass Gaussian 2-D FIR filter . . .	59
5.15	Example of speckle filtering on a sinusoidal laser curve	60
5.16	Error on the subpixel location of a sinusoidal laser curve affected by speckle	61
5.17	Laser curve on the reference image before and after smoothing . . .	62
6.1	Checker pattern used as model plane	67
6.2	Checker pattern. Camera capture	67
6.3	Checker pattern. Feature points detected	68
6.4	Repeatability of the camera calibration	70
6.5	Correction of the distortion: evaluation of the performances . .	71
6.6	Repeatability of the laser plane calibration, for e , δ and ϵ	75
7.1	Example of laser speckle. Close up on a laser stripe	81
8.1	Principle of the Biris sensor	89
8.2	Principle of cross section measurement for the wood volume estimation	89
8.3	Cross section of a typical ulcer	91
8.4	Change in area and volume of an ulcer over a five-month period . .	91
8.5	Illustration of the safe landing system based on structured lighting . .	93
8.6	3-D view of the experimental device	93
8.7	Example of image showing a pipe defect	95
9.1	Electronic caliper. Sliding-rule type	100
9.2	Electronic caliper based on ultrasonics	101
9.3	Configuration of the device. 3-D view. Case of a transversal aim . .	103
9.4	Distance and angular aperture measurement	104
9.5	Geometry of the device	105
9.6	"Three-tangent method." View in the camera plane	107
9.7	"Three-tangent method." View in the camera plane: geometry of the problem	107
9.8	Example of curve	109
9.9	Cylinder axis orientation	111
9.10	Relative error on the radius if the cylinder slant is not taken into account	115

9.11 Configuration of the device. 3-D view. Case of a randomly tilted cylinder	116
9.12 Geometry of the device in the generalized case	117
9.13 Ellipse. View in the camera plane	117
9.14 Cylinder axis orientation. Definition of the different coordinate systems	118
9.15 Determination of the cylinder orientation. 3-D view	122
9.16 α and β calculation. 3-D view	123
9.17 Quantities to measure on the laser curves	124
9.18 Photograph of the instrument	125
9.19 Example of observed scene	126
9.20 Histogram of the relative error for transversal cylinders	127
9.21 Results of measurements taken on a transversal cylinder	128
9.22 Error committed if the cylinder slant is not taken into account	130
9.23 Histogram of the relative error in the generalized case	131
9.24 Results of measurements taken on a cylindrical object at two distances, in the generalized case	132
9.25 Results of measurements taken on a cylindrical object at distances greater than 2 m	132
9.26 Results of measurements taken on cylindrical objects, the radii of which are smaller than 5 cm	133
10.1 Configuration of the device. 3-D view	139
10.2 "Three-tangent method." View in the (x_i, y_i) plane	142
10.3 Geometry of the two circles 1-2 and the sphere	142
10.4 Example of observed scene	145
10.5 Histograms of the relative error on the sphere radius	146
10.6 Results of measurements taken on a spherical object at various distances	147
11.1 Configuration of the device. 3-D view	154
11.2 2-D PCA example	156
11.3 Angle between two walls. Procedure	160
11.4 Absolute orientation of a wall. Procedure	160
11.5 Distance between two parallel walls. Procedure	162
11.6 Length of a segment. Procedure	162
11.7 Example of observed scene	163
11.8 Histogram of the relative error on the angle between two plane walls	164
11.9 Histogram of the relative error on the absolute angle of a plane wall	165
11.10 Histogram of the relative error on the distance between two parallel walls	166
11.11 Histogram of the relative error on the length of a plane segment	167

12.1 Configuration of the device. 3-D view	175
12.2 Geometry of the device	175
12.3 Photograph of the instrument	177
12.4 Dealing with speckle	179
12.5 Photograph of the voltage-controlled calibrated piezoelectric actuator	181
12.6 Graph of the altitude of the piezoelectric actuator versus the applied voltage	182
12.7 Photographs of the whole parallelepipedic piece and a close-up on one of the furrows	183
12.8 Validation on a 1-mm-wide 146- μ m-deep furrow	184
12.9 Validation on a 1-mm-wide 630- μ m-deep furrow	185
12.10 3-D representation of the prototype	188
12.11 Photograph of the prototype	189
12.12 Photograph of the road, composed of bituminous aggregates . .	190
12.13 Macrotexture analysis, showing an amplitude range of approximately 3 mm	191
12.14 Microtexture analysis on one macrotexture peak	191
A.1 Camera calibration. Configuration of the coordinate systems . .	209

List of Tables

4.1	Specifications of the CCD Cameras	35
4.2	Specifications of the Camera Lenses	36
4.3	Specifications of the Laser Diodes and their Optics	38
4.4	Specifications of the Interference Filters	40
5.1	Statistical Figures of the Absolute Error on the Subpixel Location	57
5.2	Statistical Figures of the Absolute Error after Speckle Filtering	59
6.1	Values and Dispersions of the Camera Parameters	69
7.1	Value of the geometric parameters for two particular situations	79
7.2	x , y and z Ranges for two particular situations	79
7.3	Numerical Values of Δy and ρ_y for two Concrete Cases	79
7.4	Numerical Values of Δz and ρ_z for two Concrete Cases	80
7.5	Numerical Values of Δx and ρ_x for two Concrete Cases	80
7.6	Numerical Values of D_s for two Concrete Cases	82
7.7	Numerical Values of the Absolute and Relative Errors on x , y and z for two Concrete Cases	83
7.8	Numerical Values of the Absolute and Relative Errors Due to a Bad Estimation of e	84
7.9	Numerical Values of the Absolute and Relative Errors Due to a Bad Estimation of f	84
7.10	Numerical Values of the Absolute and Relative Errors Due to a Bad Estimation of $\tan \delta$	85
7.11	Numerical Values of the Absolute and Relative Errors Due to Image Sampling, Speckle and Calibration	85
9.1	Accuracy on P_1 , P_2 , P_3 , $P_{2'}$ and $P_{3'}$ coordinates	110
9.2	Recapitulative Figures for Transversal Cylinders	128
9.3	Recapitulative Figures in the Generalized Case	129
10.1	Recapitulative Figures for Both Methods	147
11.1	Instrument specifications according to the building sector needs	153

11.2 Recapitulative Figures: Angle	164
11.3 Recapitulative Figures: Absolute Orientation	165
11.4 Recapitulative Figures: Distance	166
11.5 Recapitulative Figures: Length	167
12.1 Performances of Optical Profilometers of Road Surfaces	173
12.2 Performances Achieved by our Instrument	188

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