

# Analysis of uncertainties in the Self-Heating Extraction by RF technique in FD-SOI Transistors

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**Abstract:** This work provides a deep assessment of RF technique for self-heating (SH) extraction in advanced FD-SOI MOSFETs focusing on the uncertainties introduced by the extraction procedure. Particularly, we investigate the impact of i) choice of thermal resistance,  $R_{th}$  formula and ii) extraction of drain current variation with temperature,  $g_t = dI_D/dT$ . We show that the two valid output conductance  $g_{ds}$ -based formulations for thermal resistance, when applied to experimental data, exhibit discrepancies that increase at higher gate voltages and shorter gate lengths. Extracted uncertainty ranges from  $\sim 3\%$  for 100 nm device to  $\sim 22\%$  for the shortest lengths, underlining the importance of both consistent formulation and accurate  $g_t$  extraction at aggressively scaled nodes.

**Introduction and Method:** Enhanced self-heating in FD-SOI MOSFETs, w.r.t. their bulk counterparts, originates from the buried oxide (BOX) enhanced thermal isolation, and the higher power densities at advanced technology nodes [1]. The RF technique proved its advantages for SH extraction in advanced devices [1]. It extracts  $R_{th}$  from  $g_{ds}$  difference at high and low frequency:  $g_{ds,sh} - g_{ds,iso}$ , combined with  $g_t$  computation (Figure 1) [2]. Depending on whether  $g_t$  is taken from  $I_D$  vs  $T_{amb}$  or  $T_{ch}$ , four  $R_{th}$  formula can exist (Figure 2(a)). We show that only two of the proposed formula,  $R_{th,F1}$  and  $R_{th,F2}$ , originally derived in [2], are mathematically correct. Confusion in the definition of  $g_t$  or  $g_{ds}$  may lead to using incorrect forms  $R_{th,F1p}$  and  $R_{th,F2p}$ , as mentioned for  $R_{th,F1p}$  in [3]. In this work, we combine experimental results with analytical modeling to validate the correctness of  $R_{th,F1}$  and  $R_{th,F2}$ , and to quantify the relative uncertainty in  $R_{th}$  arising from  $g_t$  extraction and formula selection.

**Results and Discussion:** DC and RF S-parameters measurements were carried out on 28FD-SOI nMOSFETs with gate lengths  $L$  from 30 to 100 nm,  $T_{amb}$  from 298 to 353 K, and  $V_{DS} = 1$  V. The characterized devices are considered representative of the typical 28FD-SOI device behavior. The validity of the  $R_{th}$  formulas is evaluated in Figure 2(b) using a simple transistor model with a user-specified  $R_{th}^{user}$ . As shown, only  $R_{th,F1}$  and  $R_{th,F2}$  correctly recover  $R_{th}^{user}$ , whereas the alternative  $R_{th,F1p}$  and  $R_{th,F2p}$  formulas introduce errors of up to 7%. Figure 2(c) illustrates  $R_{th}W$  values extracted using four formulas for experimental 40 nm-long device, together with error bars reflecting the  $g_t$  uncertainty (given by assumption of linear  $I_D(T)$  dependence). From the experimental data, even if  $R_{th,F1}$  and  $R_{th,F2}$  do not coincide exactly, they remain the closest pair. The observed separation between  $R_{th,F1}$  and  $R_{th,F2}$  exceeds the uncertainty associated with  $g_t$  extraction, showing that  $g_t$  uncertainty:  $\sigma_{gt}$  alone cannot explain the deviation. We therefore examine how this deviation ( $R_{th,F1} - R_{th,F2}$ ) evolves with  $L$  and  $V_{GS}$ , to gain further insight into its physical origin. We define  $R_{th,mean} = (R_{th,F1} + R_{th,F2})/2$ , and use  $\sigma_{formula} = |R_{th,F1} - R_{th,F2}|/2$  as a measure of uncertainty due to formula choice. As shown in Figure 3(a),  $\sigma_{gt}$  rises sharply near  $V_{ZTC} \approx 0.65$  V, where  $g_t \rightarrow 0$ , while  $\sigma_{formula}$  increases with  $V_{GS}$ . Figure 3(b) shows that both contributions grow as the channel length decreases, with  $\sigma_{tot}$  increasing from  $\sim 3.5\%$  at  $L = 100$  nm to  $\sim 11\%$  for the shortest device, where  $\sigma_{gt}$  and  $\sigma_{formula}$  become comparable. The increase of  $\sigma_{formula}$  with higher  $V_{GS}$  and shorter  $L$  strongly suggests that enhanced self-heating amplifies the discrepancy between  $R_{th,F1}$  and  $R_{th,F2}$ . A plausible explanation is that  $R_{th}$  is temperature-dependent [2], an effect that was not included in the model. Finally, Figure 3(c) shows that using an incorrect formula (i.e.  $R_{th,F1p}$  or  $R_{th,F2p}$ ) significantly increases the relative uncertainty, reaching up to 20% for the shortest gate lengths 30-40 nm).

**Conclusion:** This work analyzed various uncertainty sources in  $R_{th}$  extraction using the RF method. We analytically confirmed that  $R_{th,F1}$  and  $R_{th,F2}$  are the only mathematically correct  $g_{ds}$ -based formulations, while  $R_{th,F1p}$  and  $R_{th,F2p}$  introduce a systematic error. A residual  $R_{th,F1} - R_{th,F2}$  discrepancy is observed in measurements, increasing with both  $V_{GS}$  and  $L^{-1}$ , while the uncertainty in  $g_t$  extraction also grows with  $L^{-1}$ . Notably,  $\sigma_{formula}$  dominates over  $\sigma_{gt}$  for most geometries, except at  $L = 30$  nm where both contributions become comparable underlining the need for both consistent formula selection and accurate  $g_t$  extraction at the shortest nodes. Further studies, including temperature-dependent  $R_{th}$  characterization, are needed to fully clarify the origin of experimentally observed differences between  $R_{th,F1}$  and  $R_{th,F2}$ . This room-temperature analysis is only a first step toward a more complete temperature-dependent study, as those uncertainties are expected to exacerbate at cryogenic temperatures, where  $T_{amb}$  and  $T_{ch}$  differ much more strongly.

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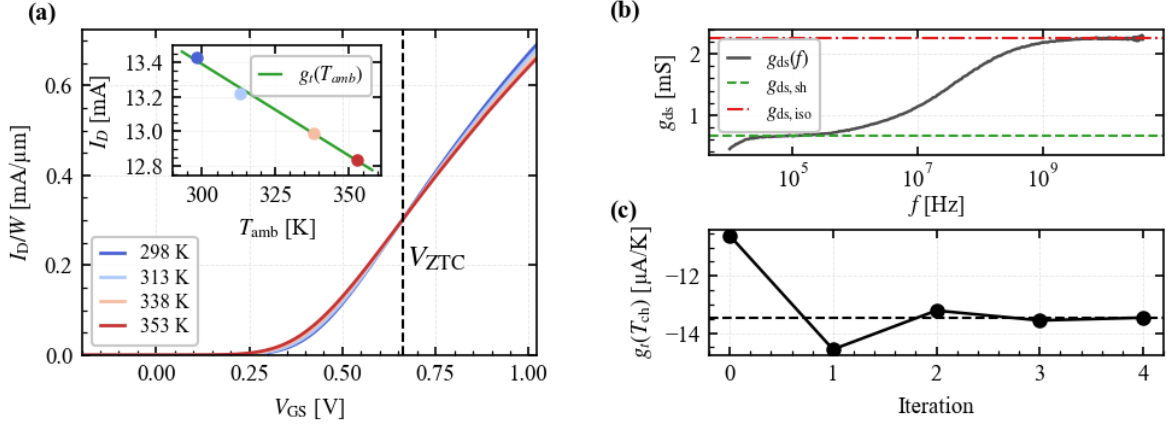


Figure 1 : (a)  $I_D/W$  vs  $V_{GS}$  at multiple  $T_{amb}$  ( $L = 40$  nm,  $V_{DS} = 1$  V). Inset:  $g_t(T_{amb})$  at  $V_{GS} = 1$  V from linear fit. (b) RF-extracted  $g_{ds}$  after open-short de-embedding and back-gate correction [4]. (c) Iterative convergence of  $g_t(T_{ch})$  at  $V_{GS} = 1$  V: starting from  $g_t(T_{amb})$ ,  $R_{th}$  and  $T_{ch} = T_{amb} + R_{th} V_{DS} I_D$ , update  $g_t(T_{ch})$ , repeat until convergence.

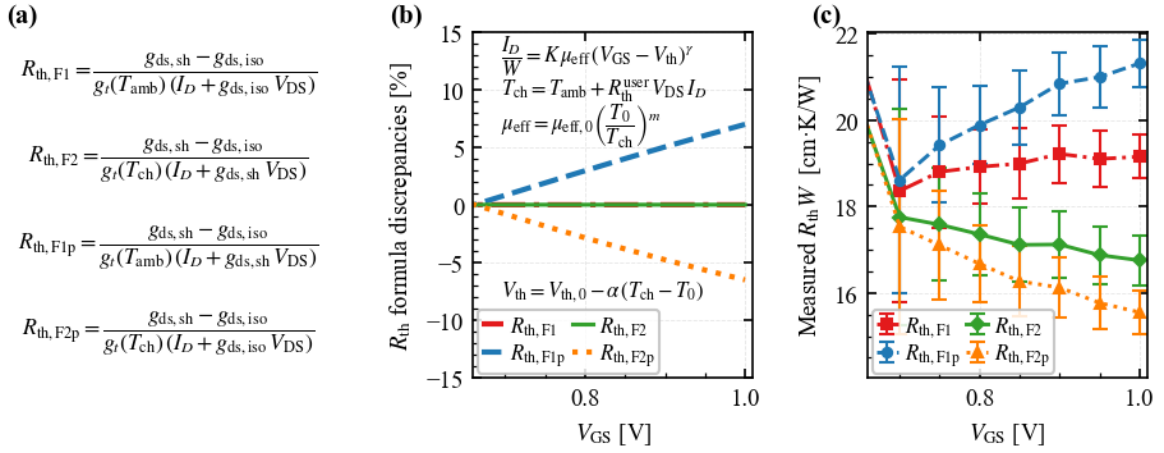


Figure 2 : Four  $R_{th}$  formula definitions (a),  $R_{th}$  formula verification using an analytical model with  $R_{th}^{user} = 18$  cm $\cdot$ K/W (b), measured  $R_{th}W$  versus  $V_{GS}$  for  $L = 40$  nm,  $V_{DS} = 1$  V (c).

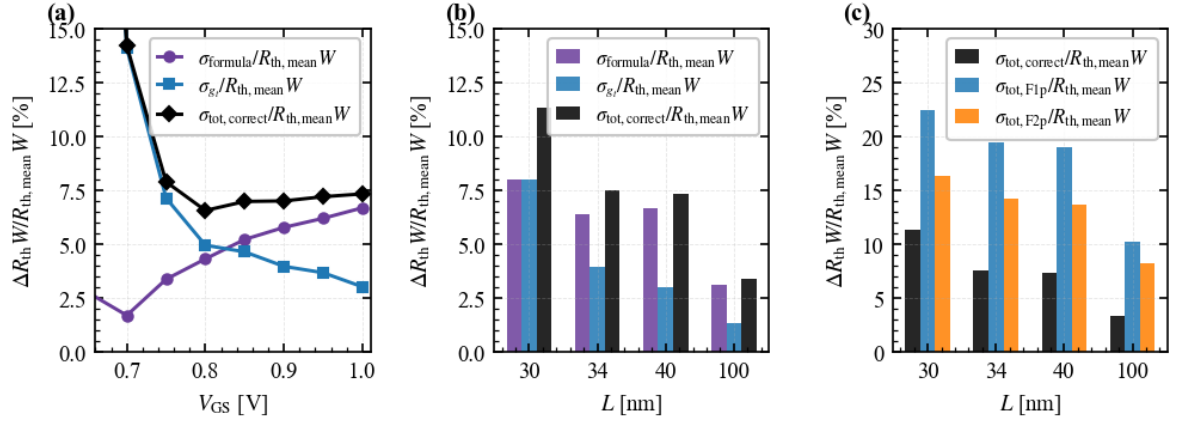


Figure 3: Extracted relative  $R_{th}W$  uncertainty versus (a)  $V_{GS}$  ( $L = 40$  nm) and (b)  $L$  ( $V_{GS} = 1$  V) showing  $\sigma_{formula}$ ,  $\sigma_{gt}$  and  $\sigma_{tot,correct}$  (total uncertainty:  $\sigma_{tot}^2 = \sigma_{formula}^2 + \sigma_{gt}^2$ ). (c) Total relative  $R_{th}W$  uncertainty if one uses  $R_{th,F1p}$  or  $R_{th,F2p}$  to extract  $R_{th}$  (total uncertainty:  $\sigma_{tot,F1p}^2 = |R_{th,F1p} - R_{th,mean}|^2 + \sigma_{gt,F1p}^2$  and  $\sigma_{tot,F2p}^2 = |R_{th,F2p} - R_{th,mean}|^2 + \sigma_{gt,F2p}^2$ ).

## References

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